



Determination of the strong coupling constant from inclusive jet cross sections

D. Britzger (DESY), **K. Rabbertz (KIT)**, G. Sieber (KIT),
D. Savoiu (KIT), M. Wobisch (Louisiana Tech)



Motivation

• Why $\alpha_s(M_Z)$?

- ▶ Among **least known** parameters of the standard model
- ▶ Important for **all processes** from hadron-induced collisions
- ▶ Needed for **QCD precision** comparisons

• How?

- ▶ Start with inclusive jet data
 - Wide kinematic range through abundant production of jets
 - Measured in many experiments
 - Well defined in fiducial volume of detectors
- ▶ Compare to theoretical prediction
 - Directly sensitive to $\alpha_s(M_Z)$
 - Available at NLO in QCD+EW
 - QCD @ NNLO is under way
 - Less ambiguous with respect to scale choice



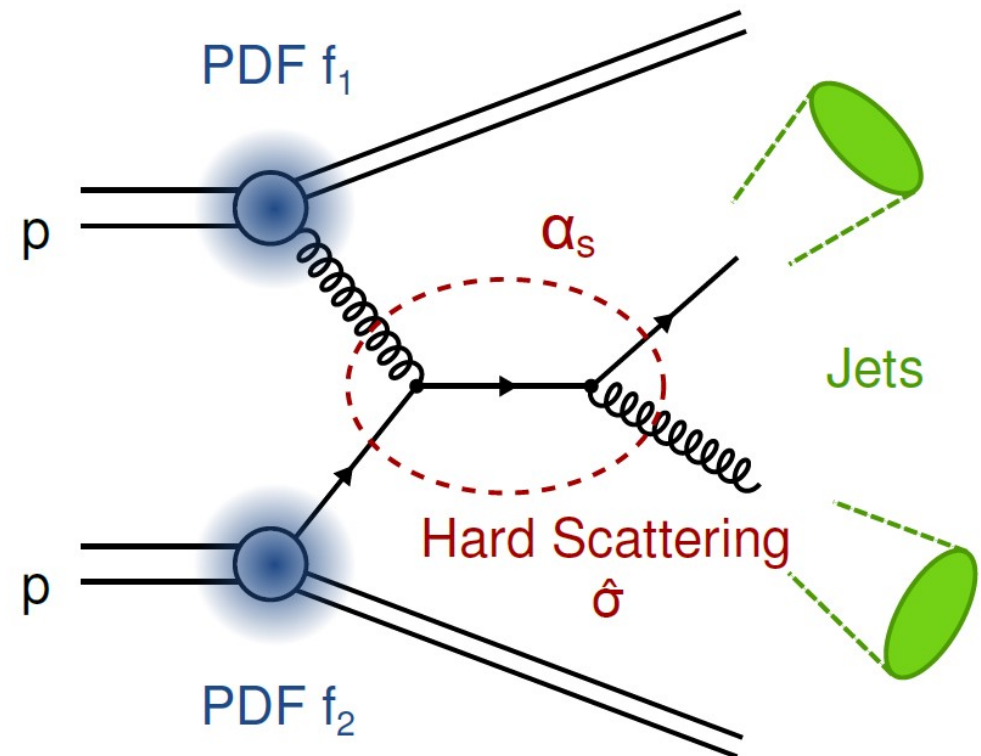
Main ingredients

Data

- Abundance of inclusive jet data from various experiments
 - ◆ ATLAS, CMS, CDF, D0, H1, ZEUS, STAR, ...
- **Inclusive jet measurement**
 - ◆ Phase space, experimental uncertainties, correlations

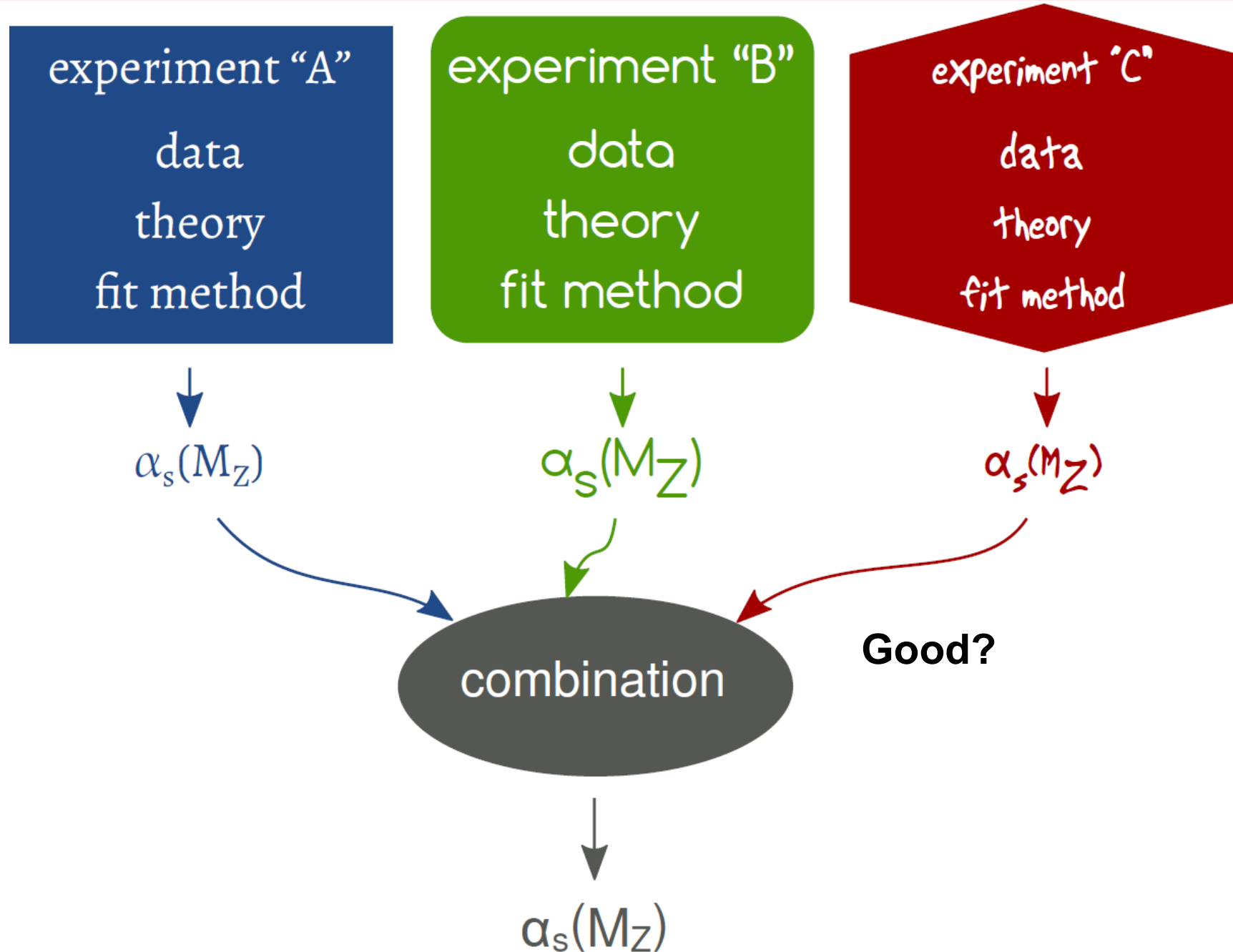
Theory

- **Partonic matrix element $\hat{\sigma}$**
 - ◆ Sensitive to $\alpha_s(M_Z)$
- **Convolution with PDFs**
 - ◆ Dependence on $\alpha_s(M_Z)$



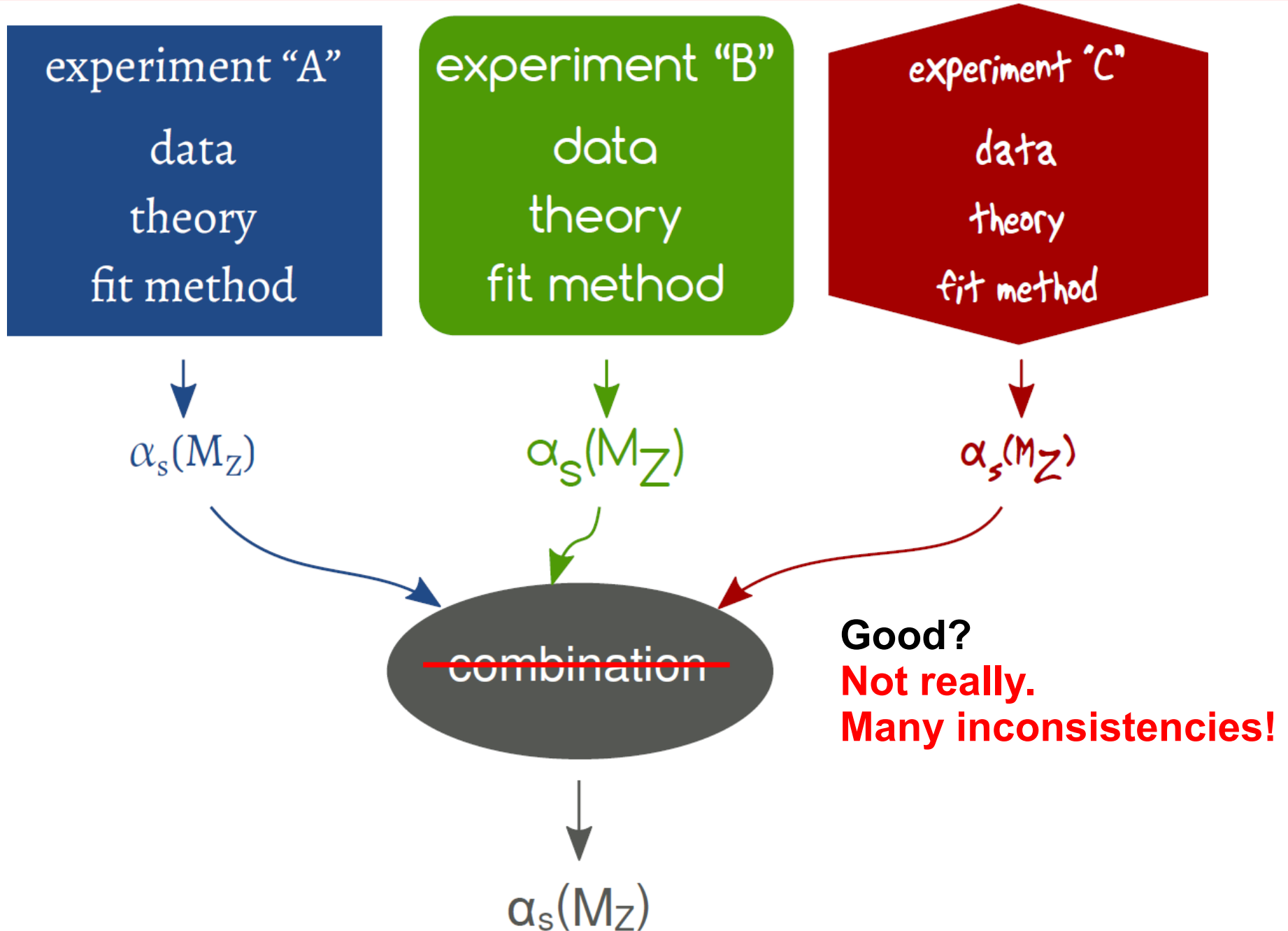


Strategy?





Strategy?





Better strategy

experiment "A"
data

experiment "B"
data

experiment "C"
data

unified theory
(N)NLO calculation ... non-perturbative corrections ... PDFs ... α_s evolution

common fit method
 χ^2 definition ... treatment of uncertainties on data, theory ... estimation of uncertainties on α_s



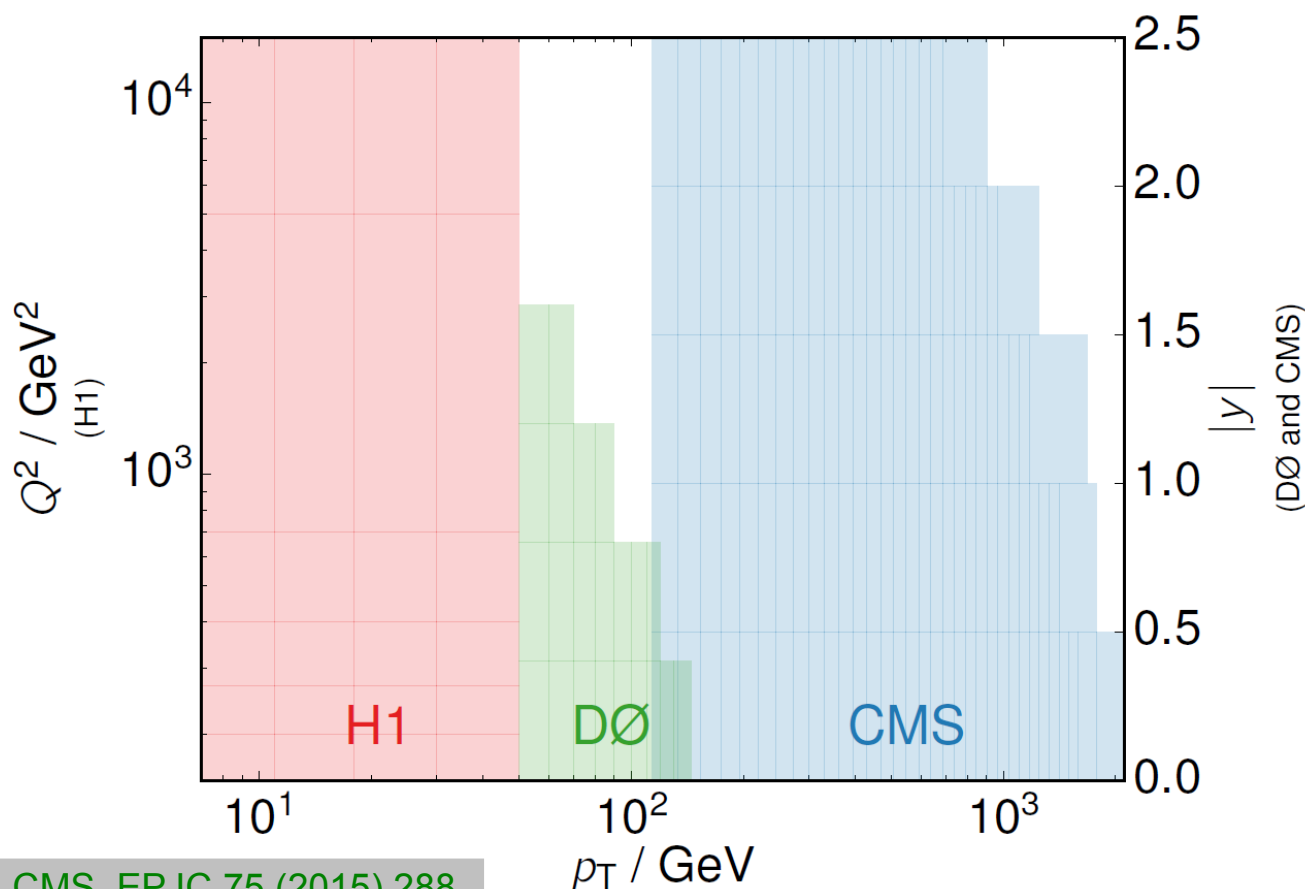
$$\alpha_s(M_Z)$$



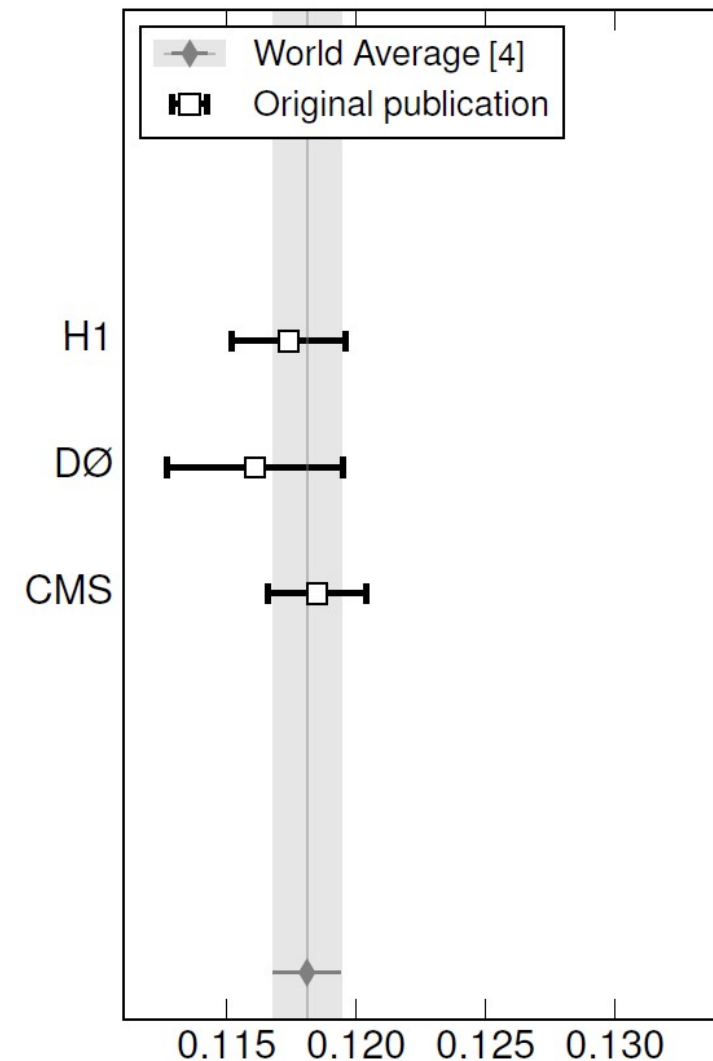
First look: $\alpha_s(M_Z)$ at CMS, D0, H1

Data

- ◆ $\alpha_s(M_Z)$ extractions by CMS, D0, and H1
- ◆ cover large and complementary phase space



CMS, EPJC 75 (2015) 288.
 D0, PRD 80 (2009) 111107.
 H1, EPJC 75 (2015) 65.



experimental uncertainty $\alpha_s(M_Z)$

[4] PDG, ChPC 40 (2016) 100001.



Comparison of fit setups

	H1	DØ	CMS
theory predictions	NLO	approximate NNLO	NLO
$\alpha_s(M_Z)$ extraction procedure	direct χ^2 minimization	direct χ^2 minimization	“indirect” χ^2 minimization (fit of parabola to discrete χ^2 points)
χ^2 definition	conventional χ^2 (log data – log theory) + relative uncertainties	modified χ^2 + nuisance parameters	conventional χ^2 (data – theory) + absolute uncertainties
uncertainty estimation	linear error propagation	nuisance parameters	<ul style="list-style-type: none">• “$\Delta\chi^2 = +1$”• subtraction in quadrature• “offset” method

Significant differences!

- ◆ neglected in naïve combination of results
- ◆ develop unified fit procedure

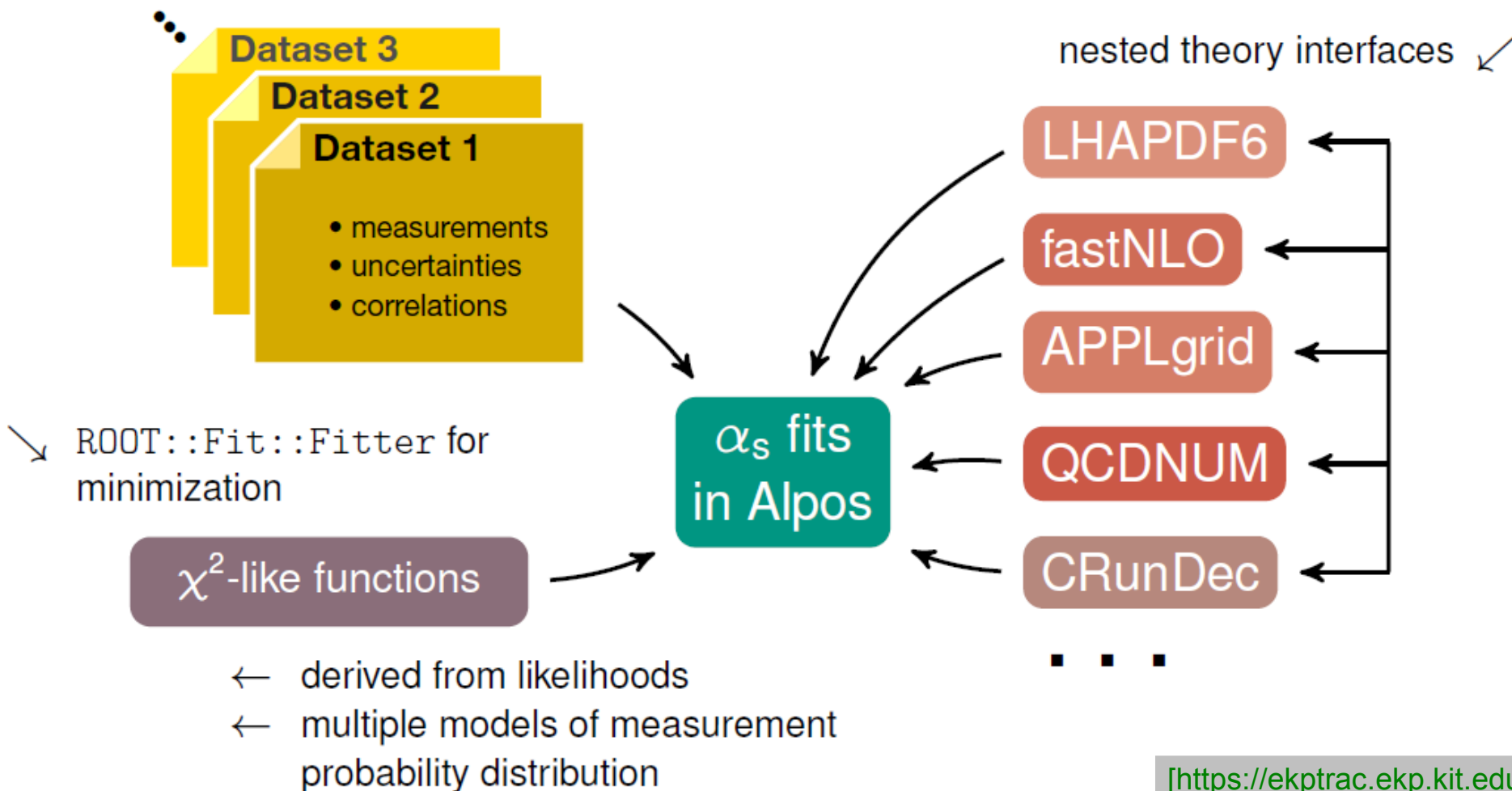


Fitting framework: Alpos

New modular C++ based fitting framework

➔ used for $\alpha_s(M_Z)$, PDF, and electroweak fits within H1 and CMS

↘ input format: experience with xFitter/HERAFitter



↘ ROOT::Fit::Fitter for minimization

nested theory interfaces ✓

- ← derived from likelihoods
- ← multiple models of measurement probability distribution



Fitting framework: Alpos

New modular C++ based fitting framework

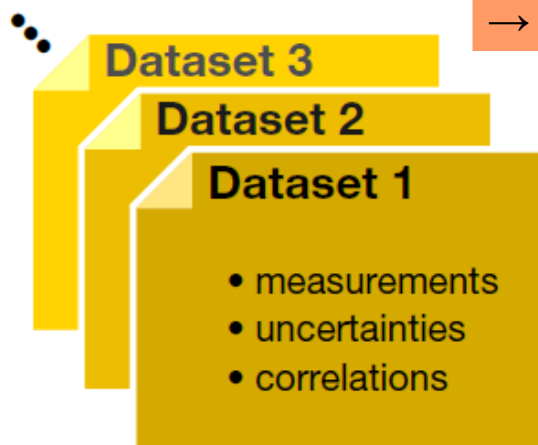
➤ used for $\alpha_s(M_Z)$, PDF, and electroweak fits within H1 and CMS

↘ input format: experience with xFitter/HERAFitter

→ E. Eren: CMS jet results, next talk

→ D. Britzger: DIS jet fits @ NNLO, yesterday

→ F. Olness: xFitter, tomorrow



nested theory interfaces ✓

↘ ROOT::Fit::Fitter for minimization

χ^2 -like functions

α_s fits
in Alpos

LHAPDF6

fastNLO

APPLgrid

QCDNUM

CRunDec

• • •

→ C. Gwenlan: Usage @ NNLO, yesterday

- ← derived from likelihoods
- ← multiple models of measurement probability distribution

[<https://ekptrac.ekp.kit.edu/svn/Alpos>]



Unified fit method

theory predictions

consistent (N)NLO

$\alpha_s(M_Z)$ extraction procedure

direct χ^2 minimization

χ^2 definition

conventional χ^2
(**log data** – **log theory**)
+ relative uncertainties

PDF and non-perturbative uncertainties

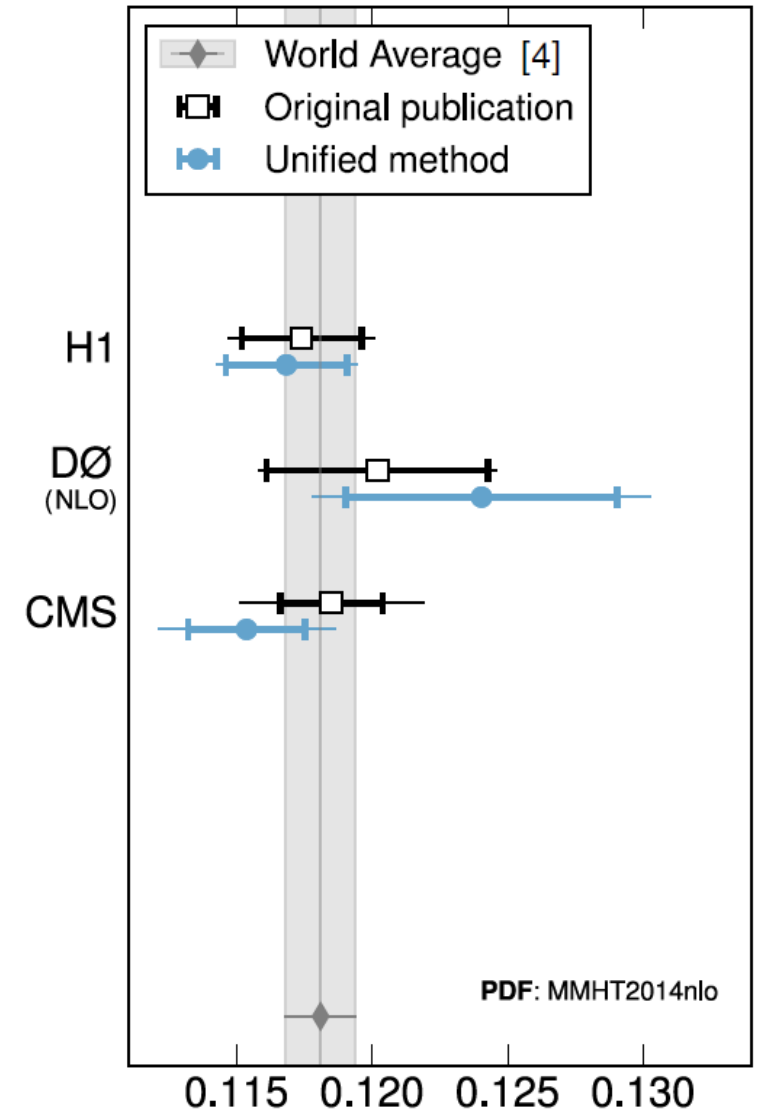
included in χ^2 definition

PDF $\alpha_s(M_Z)$ dependence

additional uncertainty
on $\alpha_s(M_Z)$

Unified approach:

- slight differences wrt. original
- compatible within uncertainties
- more consistent comparison
- ➔ **simultaneous fit**



experimental uncertainty $\alpha_s(M_Z)$
 total uncertainty (except scale)



Unified fit result

theory predictions

consistent (N)NLO

$\alpha_s(M_Z)$ extraction procedure

direct χ^2 minimization

χ^2 definition

conventional χ^2
(**log data** – **log theory**)
+ relative uncertainties

PDF and non-perturbative uncertainties

included in χ^2 definition

PDF $\alpha_s(M_Z)$ dependence

additional uncertainty
on $\alpha_s(M_Z)$

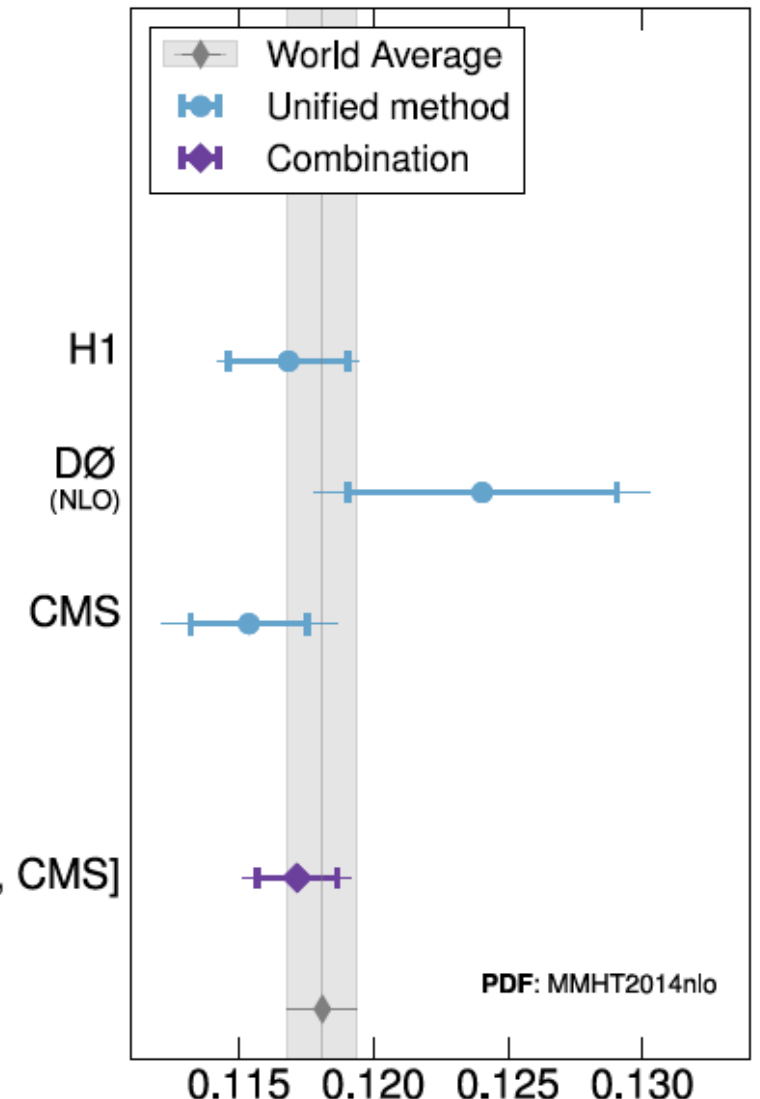
Result of simultaneous fit:

$$\alpha_s(M_Z) = 0.1172(15)_{\text{exp}} (14)_{\text{theo w/o scale}} (50)_{\text{scale}}$$

$$[\chi^2_{\text{min}}/\text{ndf} = 152/178 = 0.86]$$

D. Savoiu, Master's thesis, IEKP-KA/2016-25, KIT

[H1, DØ, CMS]



experimental uncertainty
 total uncertainty (except scale)
 $\alpha_s(M_Z)$



More datasets



Objective

- **Develop a robust procedure to determine $\alpha_s(M_Z)$**
 - **Include more than one dataset**
 - **Consistent treatment of theory**
 - **Extensible to additional observables**
 - **Unique**
 - **Flexibility**
- **How?**
 - **Start with inclusive jet data**
 - **Wide kinematic range through abundant production of jets**
 - **Measured in many experiments**
 - **Well defined in fiducial volume of detectors**
 - **Compare to theoretical prediction**
 - **Directly sensitive to $\alpha_s(M_Z)$**
 - **Available at NLO in QCD+EW**
 - **QCD @ NNLO just around the corner**
 - **Less ambiguous with respect to scale choice**



Outlook

- NNLOJET provides NNLO in common interface for:
 - ➔ Z incl., Z+jet, W incl., pp jet+dijets, H incl., H+jet, DIS jet+dijets, e+e- 3jets
 - ➔ W+jet almost ready; more to come
- APPLgrid+fastNLO interface (NNLO-Bridge) is working
- Numerous adaptations implemented by all sides
- Large-scale productions tested for Z+jet and DIS jet
- **Work in progress: Implementation of final combination procedure for interpolation grids**
- **Looking forward to many new NNLO interpolation grids in 2017**

We acknowledge support from an IPPP Associateship and Baden-Württemberg HPC support through BwUniCluster and BwForCluster.



Backup

α_s

Method comparison

H1 fit methodology

$$\chi_{\text{H1}}^2 \rightarrow \sum_{ij} (\ln m_i - \ln t_j) [\mathbf{V}_{(\text{rel})}^{-1}]_{ij} (\ln m_j - \ln t_j)$$

- iterative χ^2 minimization (*MINUIT*)
 - determine central value with experimental uncertainties only
 - assume PDF without $\alpha_s(M_Z)$ dependence; use MSTW2008nlo with $\alpha_s(M_Z) = 0.118$
- additional theory uncertainties: NP corr., PDF, PDF $\alpha_s(M_Z)$, PDF set, μ_r , μ_f
 - obtained through additional fits / linear error propagation

DØ fit methodology

$$\chi_{\text{DØ}}^2 \rightarrow \sum_i \frac{\left[m_i - t_i \frac{1 + \sum_k \delta_{ik}^{(\text{NP})} (\alpha_k^{(\text{NP})}) + \sum_l \delta_{il}^{(\text{PDF})} (\alpha_l^{(\text{PDF})})}{1 + \sum_j \delta_{ij}(\epsilon_j)} \right]^2}{\sigma_{i,\text{stat}}^2 + \sigma_{i,\text{uncorr}}^2}$$

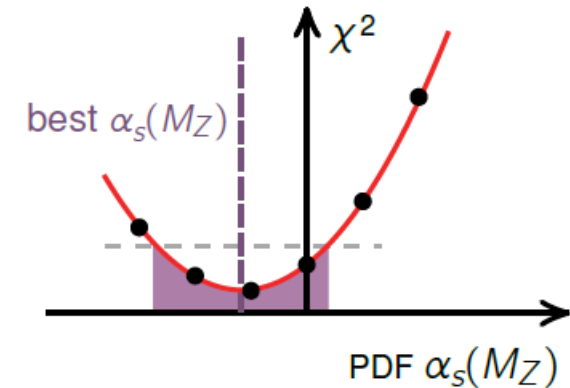
- iterative χ^2 minimization (*MINUIT*)
 - one nuisance parameter for each PDF eigenvector and each NP correction factor
 - interpolate cross section predictions obtained for PDFs assuming different values of $\alpha_s(M_Z)$
- aNNLO (NLO predictions with threshold corrections + NNLO PDFs)
- 88 out of 110 data points excluded ← correlations with MSTW2008 PDFs

Method comparison

CMS fit methodology

$$\chi_{\text{CMS}}^2 \rightarrow \sum_{ij} (m_i - t_j) [(\mathbf{V}_{\text{exp}} + \mathbf{V}_{\text{PDF}})^{-1}]_{ij} (m_j - t_j)$$

- χ^2 is evaluated for each PDF in an $\alpha_s(M_Z)$ series
 - resulting $(\chi^2, \alpha_s(M_Z))$ points are assumed to lie on a parabola
 - fit of second-degree polynomial function \rightarrow central value and uncertainty on $\alpha_s(M_Z)$
- PDF: CT10nlo (results are also provided for MSTW2008 and NNPDF21)
- NP uncertainties obtained by performing additional fits with correlated variation of theory



Fit methods **differ significantly!**

- \rightarrow “naive” combination of results (weighted average) not very conclusive
- \rightarrow need to extract $\alpha_s(M_Z)$ using measurements from all experiments in a **unified** fit procedure



PDF $\alpha_s(M_Z)$ dependence

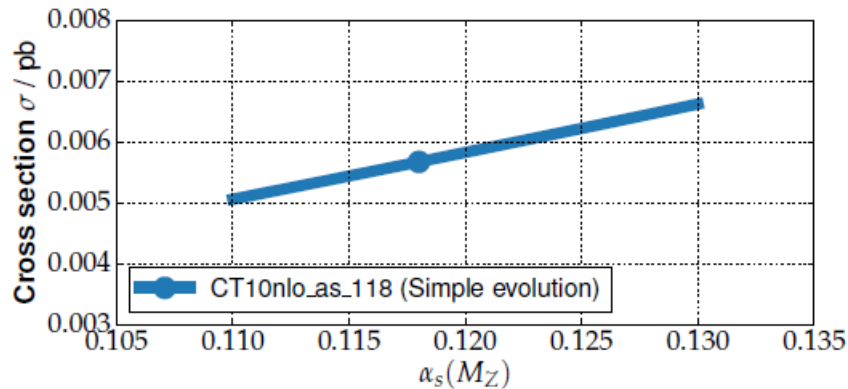
How to express the $\alpha_s(M_Z)$ dependence of the cross section?

❓ how to account for $\alpha_s(M_Z)$ dependence in PDFs?

Two methods are studied:

“Fixed PDF” (○)

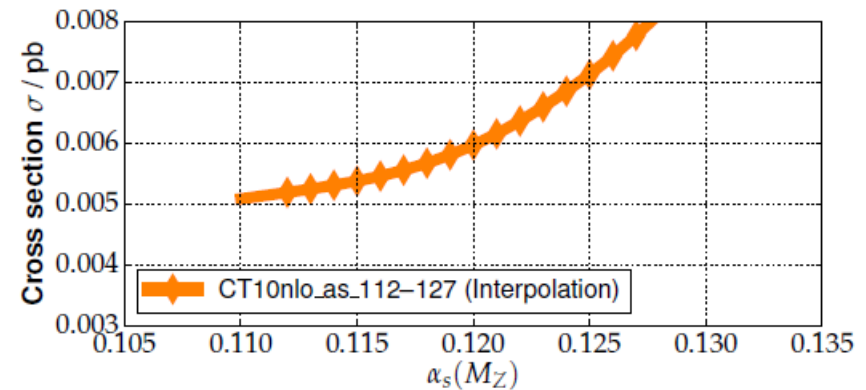
(method used in H1 publication)



- calculate cross section using PDF for **one** chosen $\alpha_s(M_Z)$
- prediction $\sigma(\alpha_s(M_Z))$ directly from fastNLO

“PDF Interpolation” (◇)

(method used in DØ publication)



- calculate cross section using PDF for **each** available $\alpha_s(M_Z)$
- prediction $\sigma(\alpha_s(M_Z))$ from **interpolation** between the points



Method comparison

“Fixed PDF”

- + $\alpha_s(M_Z)$ dependence is **quadratic**, as expected for inclusive jet cross sections
- + well-defined theory
- + clear breakdown of PDF uncertainties
- introduces an additional procedural uncertainty due to $\alpha_s(M_Z)$ used in PDF fit
- possible bias towards assumed PDF $\alpha_s(M_Z)$

choose this as main method

“PDF Interpolation”

- + provides a way to include the uncertainty due to the choice of PDF $\alpha_s(M_Z)$ **in the fit**
- o interpolation method needs to be defined (e.g. fit or splines)
 - ▲ spline interpolation not well suited for some PDFs (e.g. NNPDF)
- spline extrapolation may give unphysical results
- ? does procedure reproduce PDF α_s dependence?

In most cases, both methods yield comparable results



Procedural PDF uncertainties

- additional PDF-related procedural uncertainties arise in addition to “PDF uncertainties” themselves:

- ① choice of PDF set
- ② choice of $\alpha_s(M_Z)$ assumed when fitting PDF

