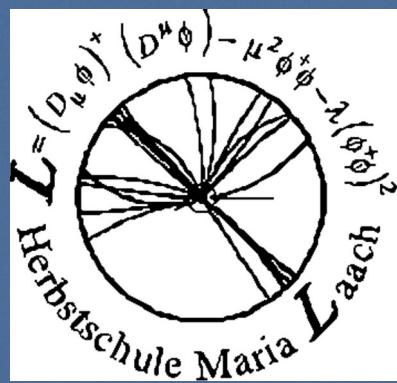


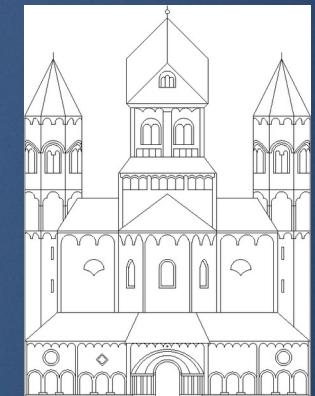


# QCD and Jets at the LHC

V03 – From jet measurements to SM  
parameters (or new physics)



Herbstschule  
Maria Laach



Klaus Rabbertz

# *Outline*



- Inclusive jet measurement in details
- More on jets
  - Dijet cross section
  - Ratios & normalised distributions
- The strong coupling constant

# *Outline*



- Inclusive jet measurement in details
- More on jets
  - Dijet cross section
  - Ratios & normalised distributions
- The strong coupling constant

Hot topics I could not cover:

- Years of substructure analyses for q/g separation or boosted heavy particles
  - Lund jet plane analysis (C/A declustering)
- Flavor jets

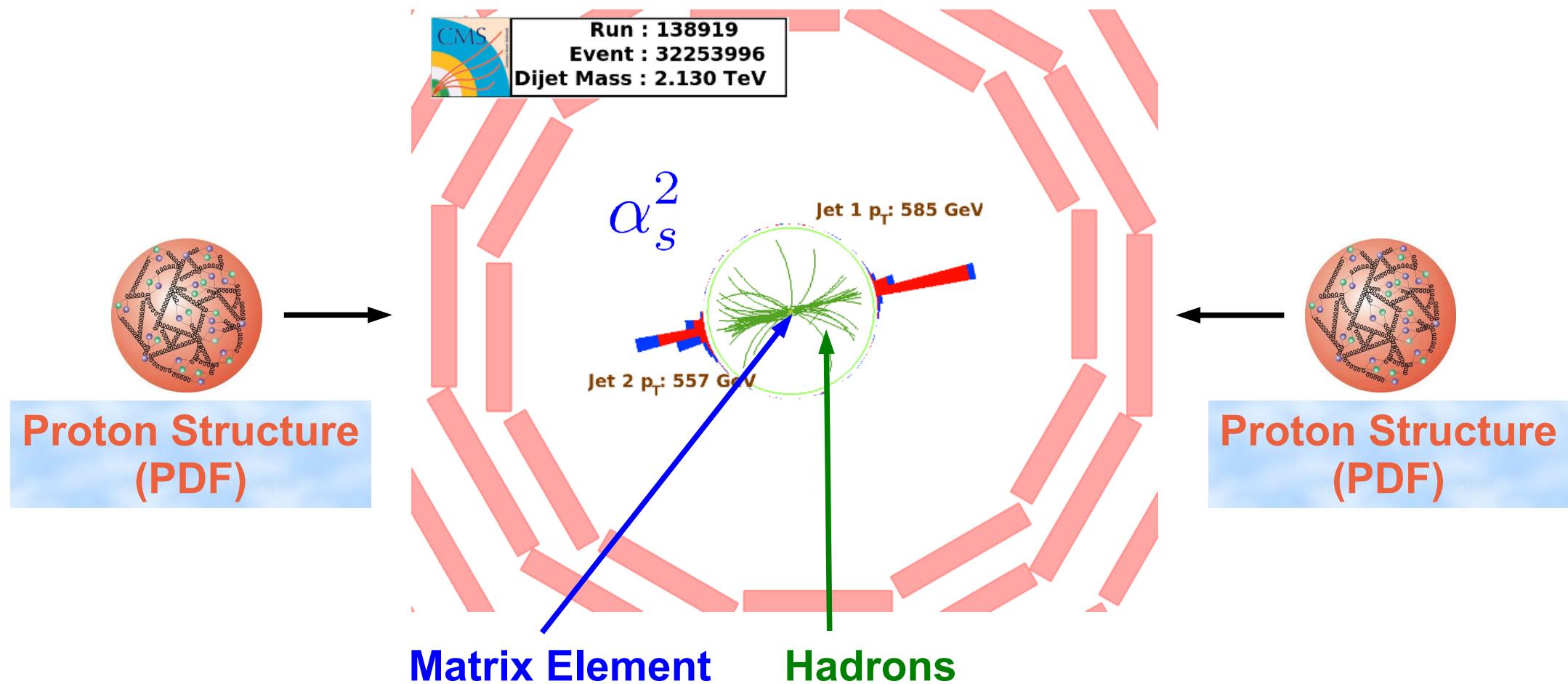


# Jets at the LHC



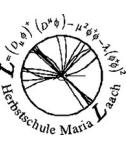
## Abundant production of jets:

- Jets at hadron colliders provide the highest reach ever to determine the strong coupling constant at high scales Q
- Also learn about hard QCD, the proton structure, non-perturbative effects, and electroweak effects at high Q



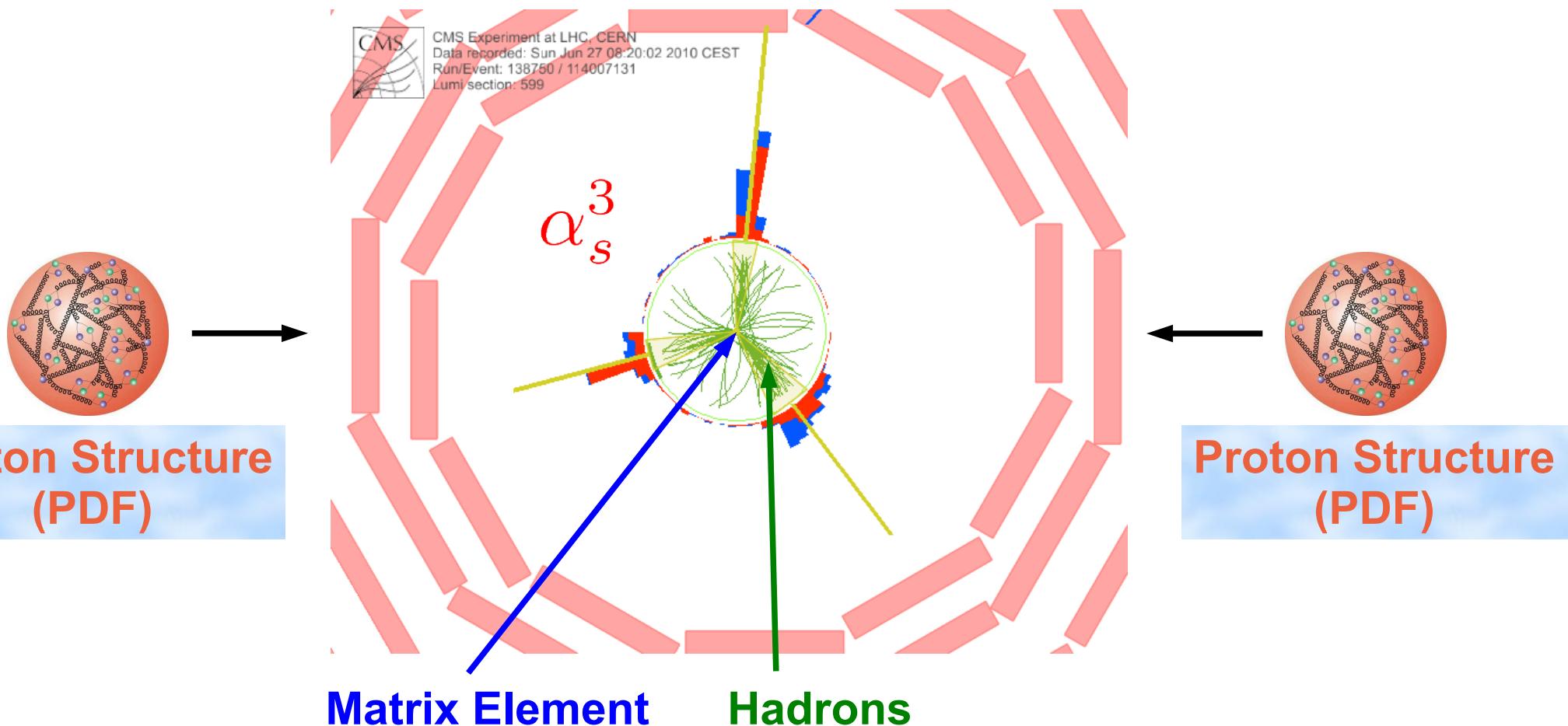


# Jets at the LHC



Abundant production of jets:

→ Extract  $\alpha_s(M_Z)$ , the least precisely known fundamental constant!





# Jet cross sections $\sim \alpha_s^2$

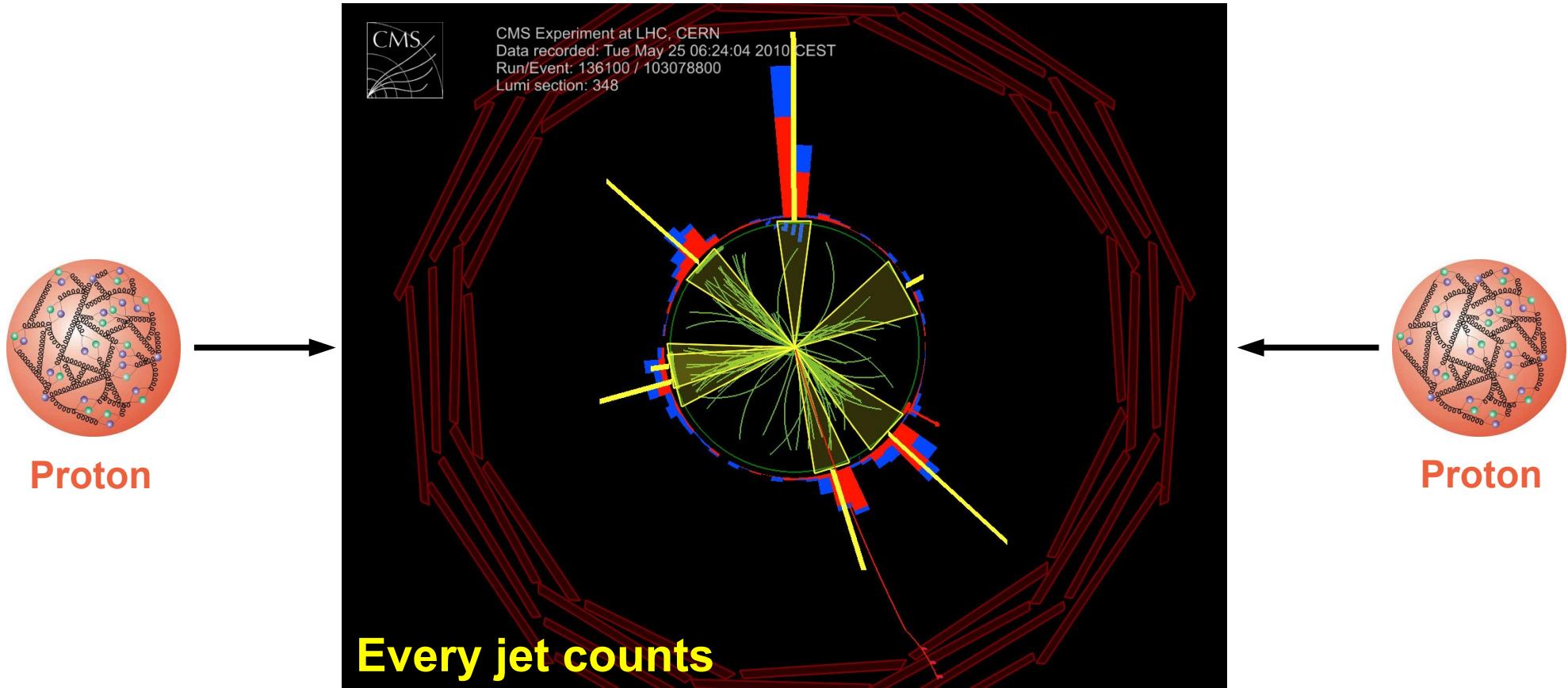


- Useful for i.a.:
  - + Determination of  $\alpha_s(M_Z)$  in single-parameter fit
  - + Test consistency of running of  $\alpha_s(Q)$
  - + Multi-parameter fit of  $\alpha_s(M_Z)$  & PDFs
  - + Multi-parameter fit including EFT parameters
- Subject to all systematic uncertainties: JEC, JER, MHOU, luminosity, ...



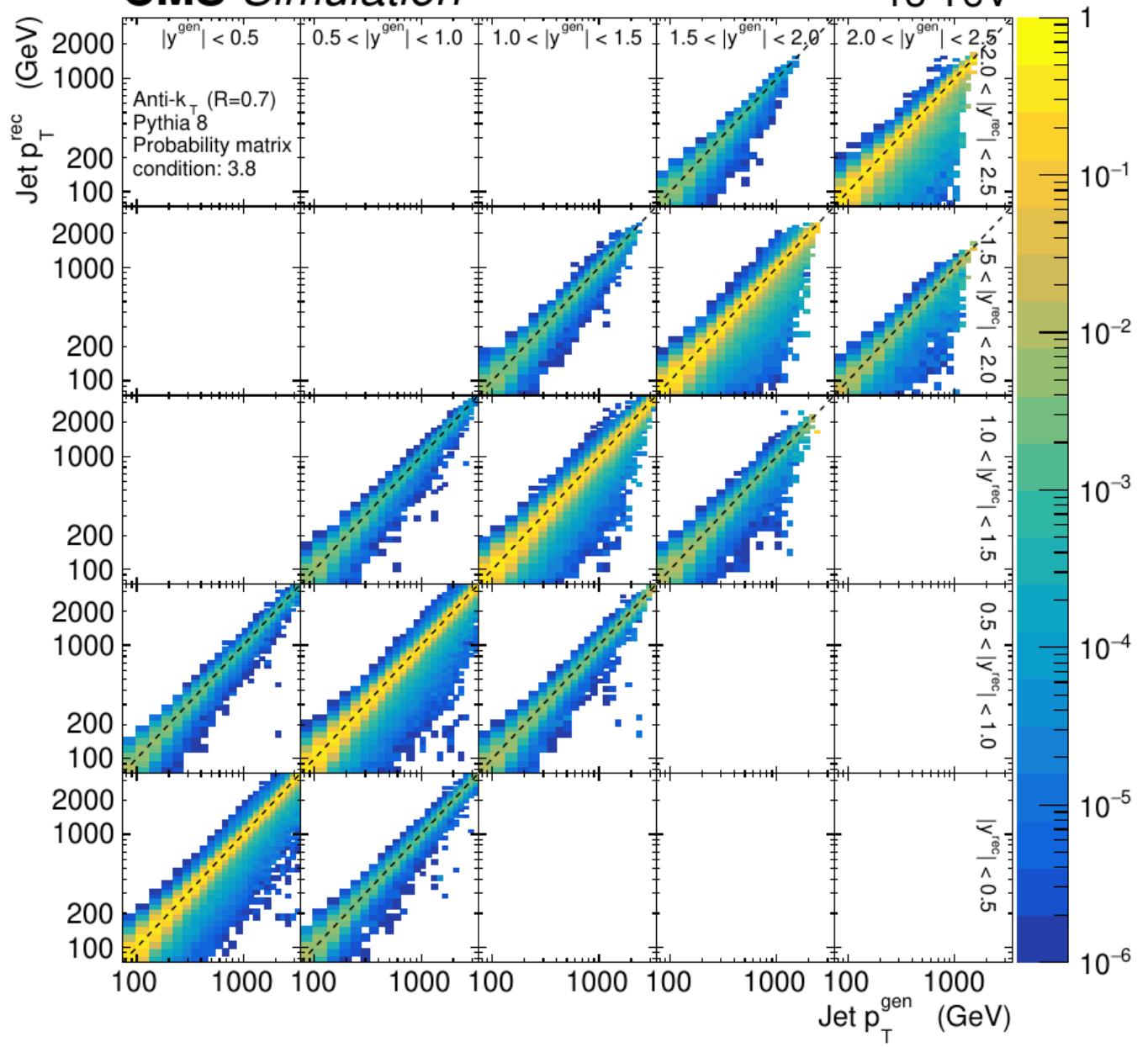
# All inclusive

## Large transverse momenta



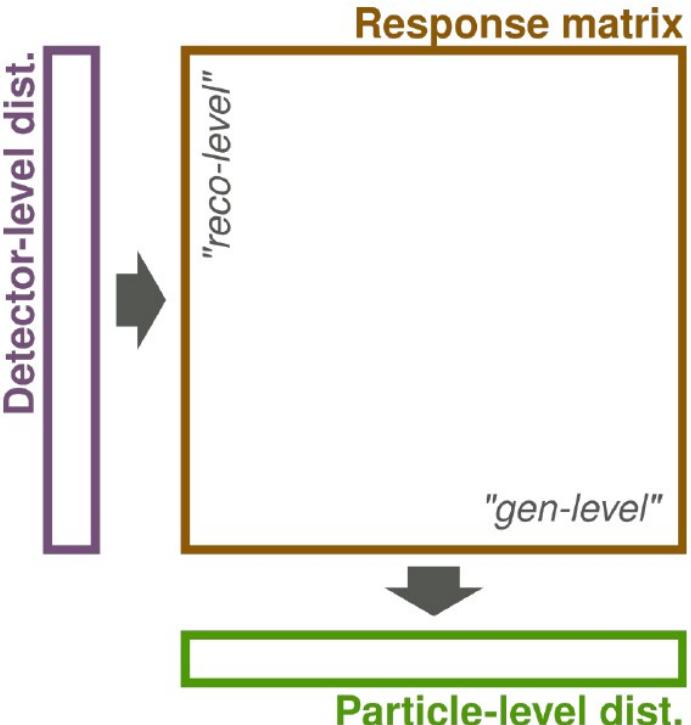
# Response matrix

CMS Simulation



13 TeV

T unfold, S. Schmitt, JINST 7 (2012) T10003.



- Unfold effect of detector smearing
- Needs response from full simulation
- Sufficiently well-conditioned (3.8) / diagonal to allow matrix inversion

CMS JHEP02 (2022) 142, JHEP12 (2022) 035.



# Inclusive jets: cross section



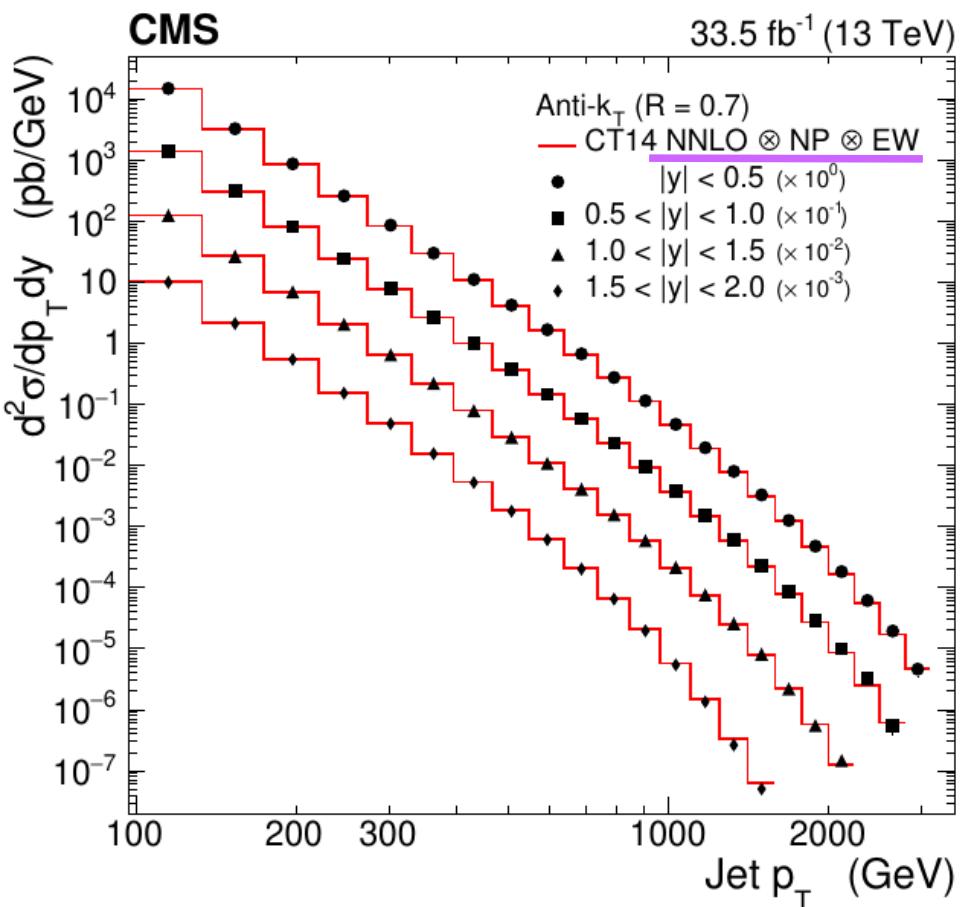
Overall agreement with NNLO x NP x EW

Over many orders of magnitude

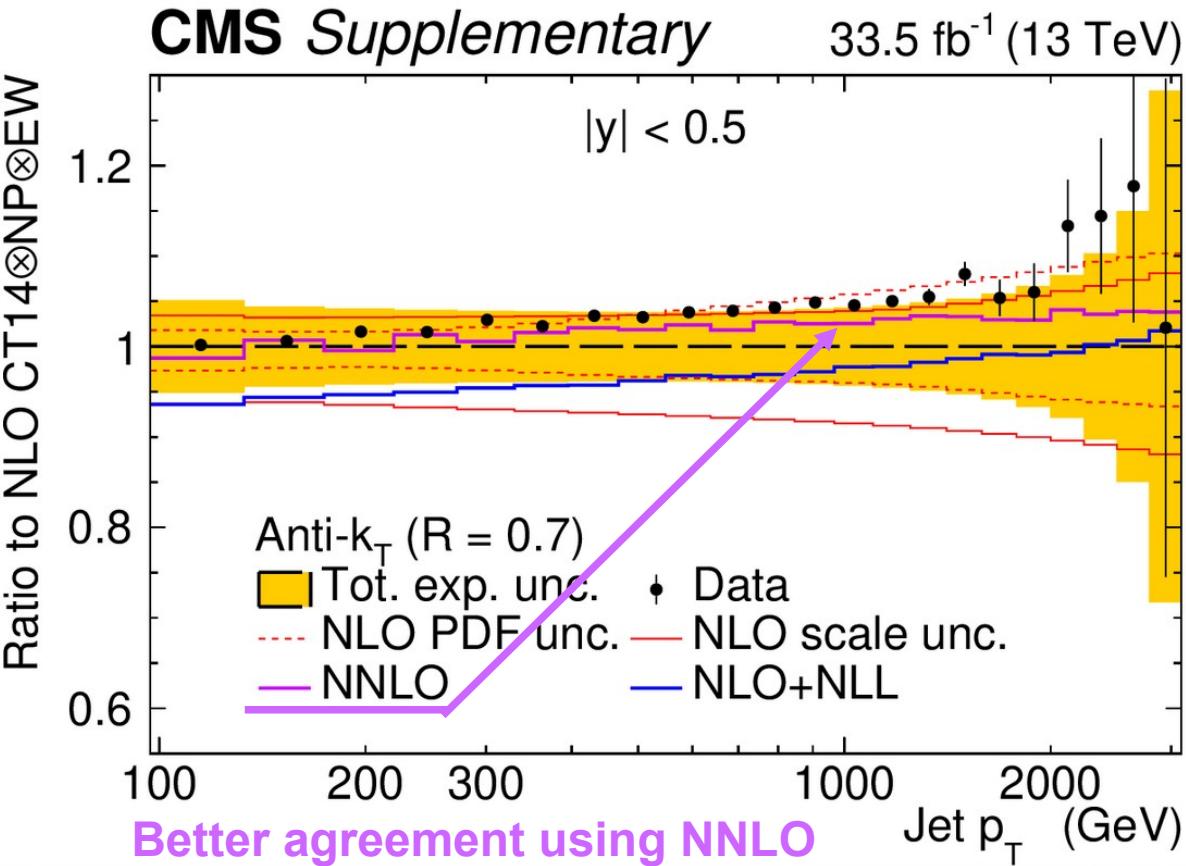
Even beyond 2 TeV in jet  $p_T$  and for rapidities  $|y|$  up to 2

$$\frac{d^2\sigma}{dp_T dy} \propto \alpha_s^2$$

anti- $k_T$ , R=0.7, 13 TeV

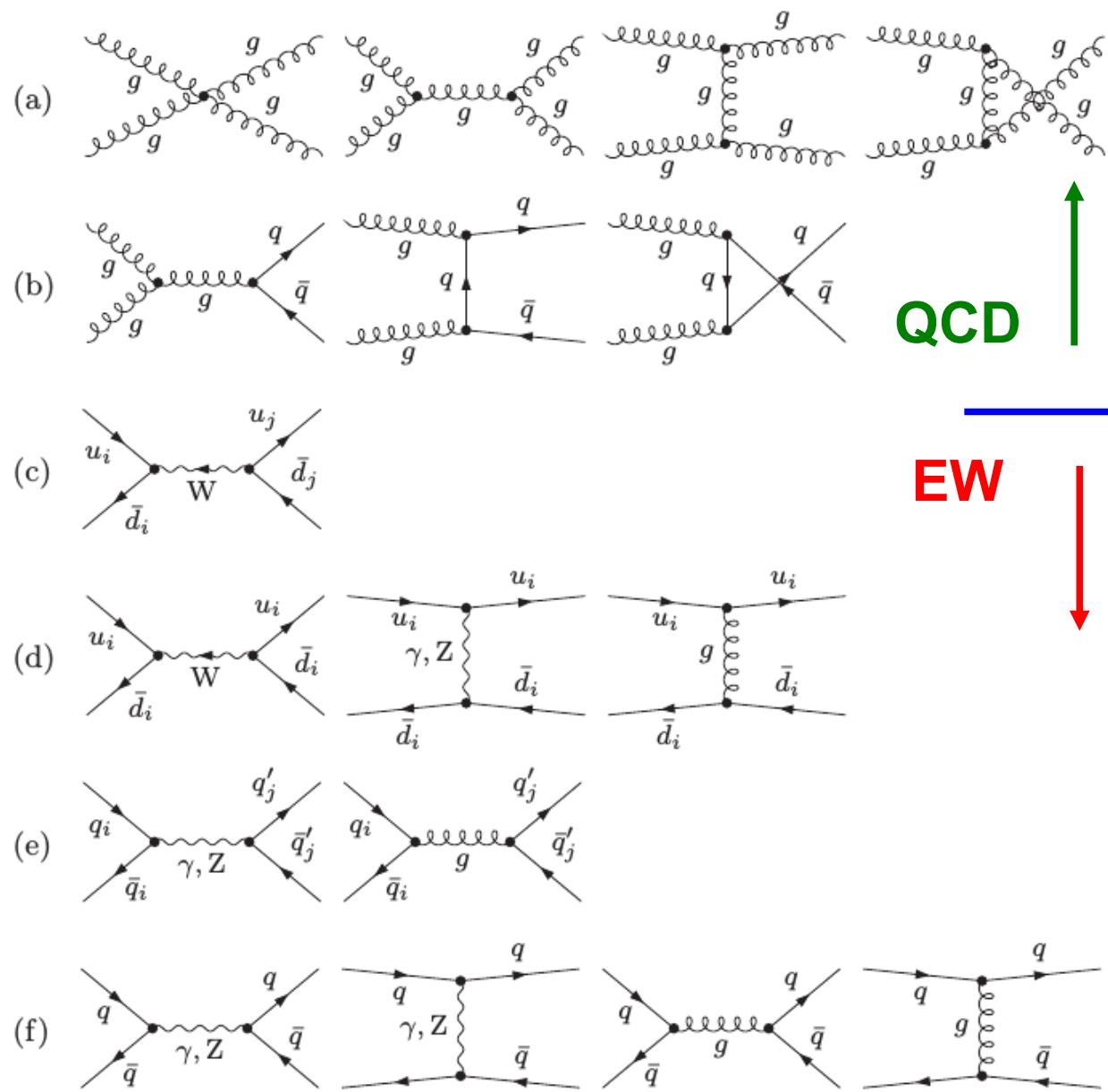


Ratio to NLO x NP x EW for  $|y| < 0.5$

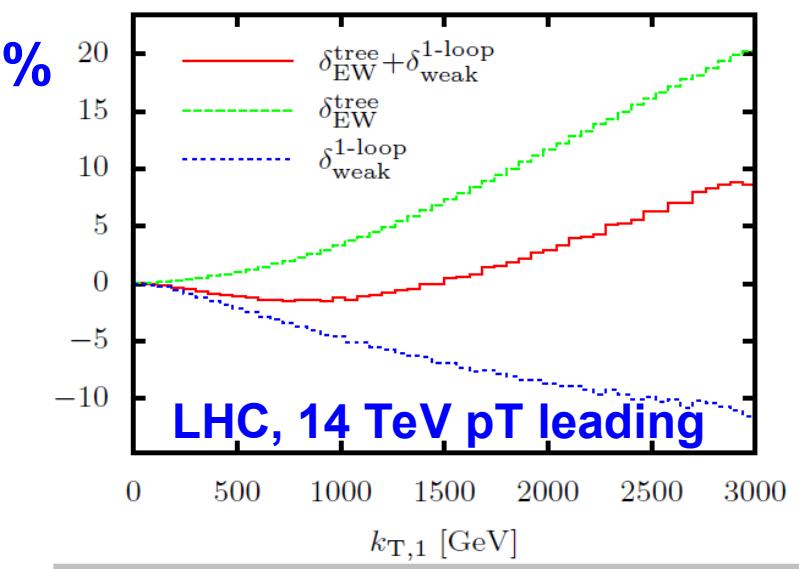
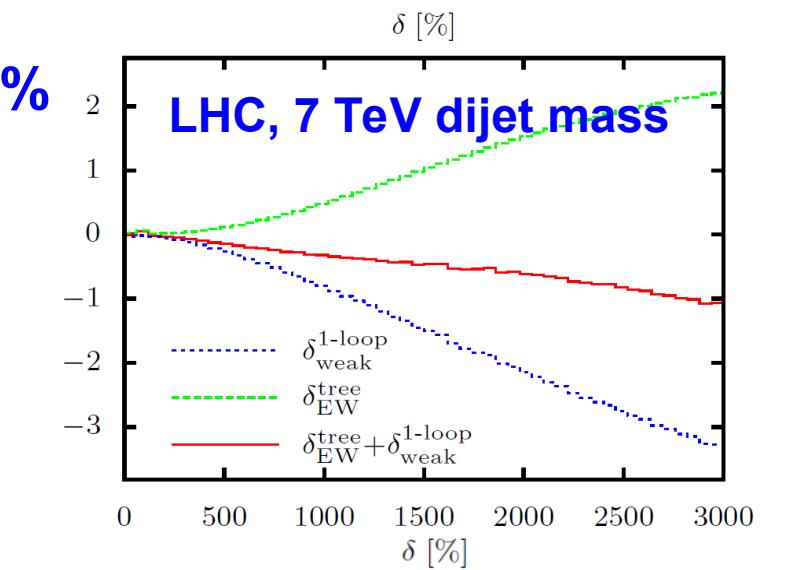




# Progress in theory: NLO EW



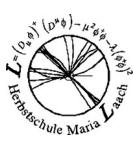
**Elektroweak corrections  $\propto \alpha \alpha_s^2$**



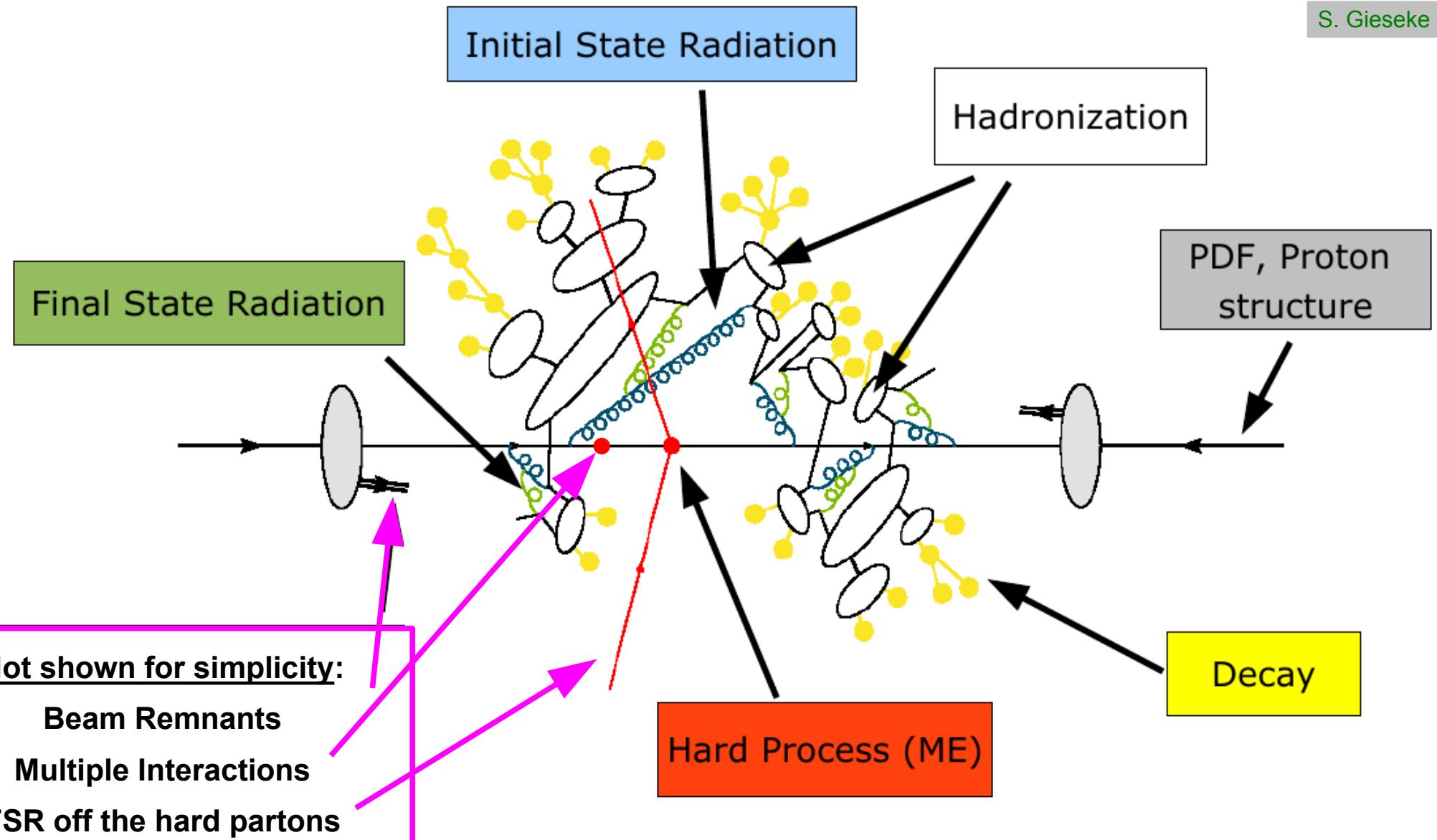
S. Dittmaier, A. Huss, C. Speckner, JHEP11 (2012);  
R. Frederix et al., JHEP 04 (2017) 076.



# Event display from MC generator



S. Gieseke





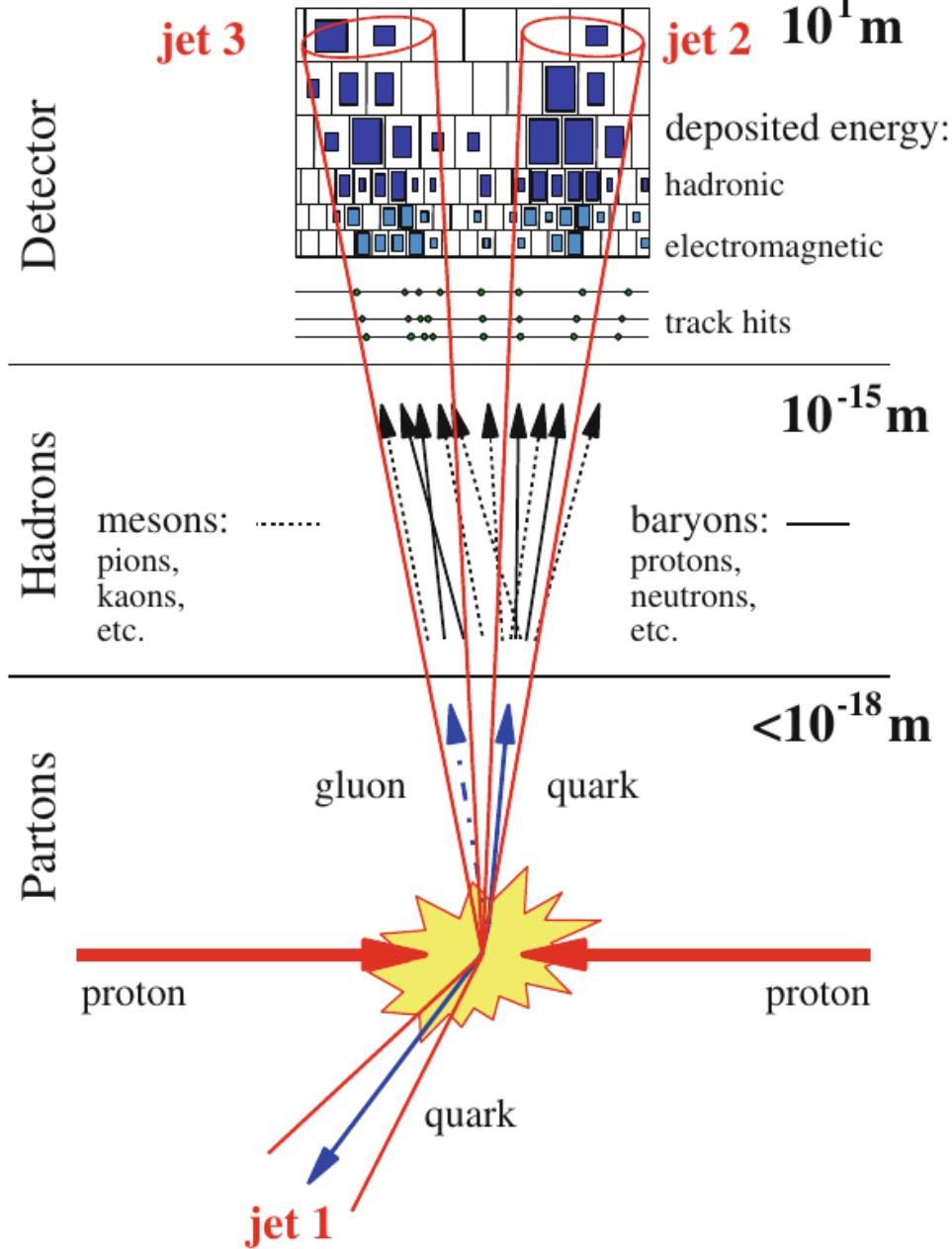
# Comparison data-theory



## Measurements

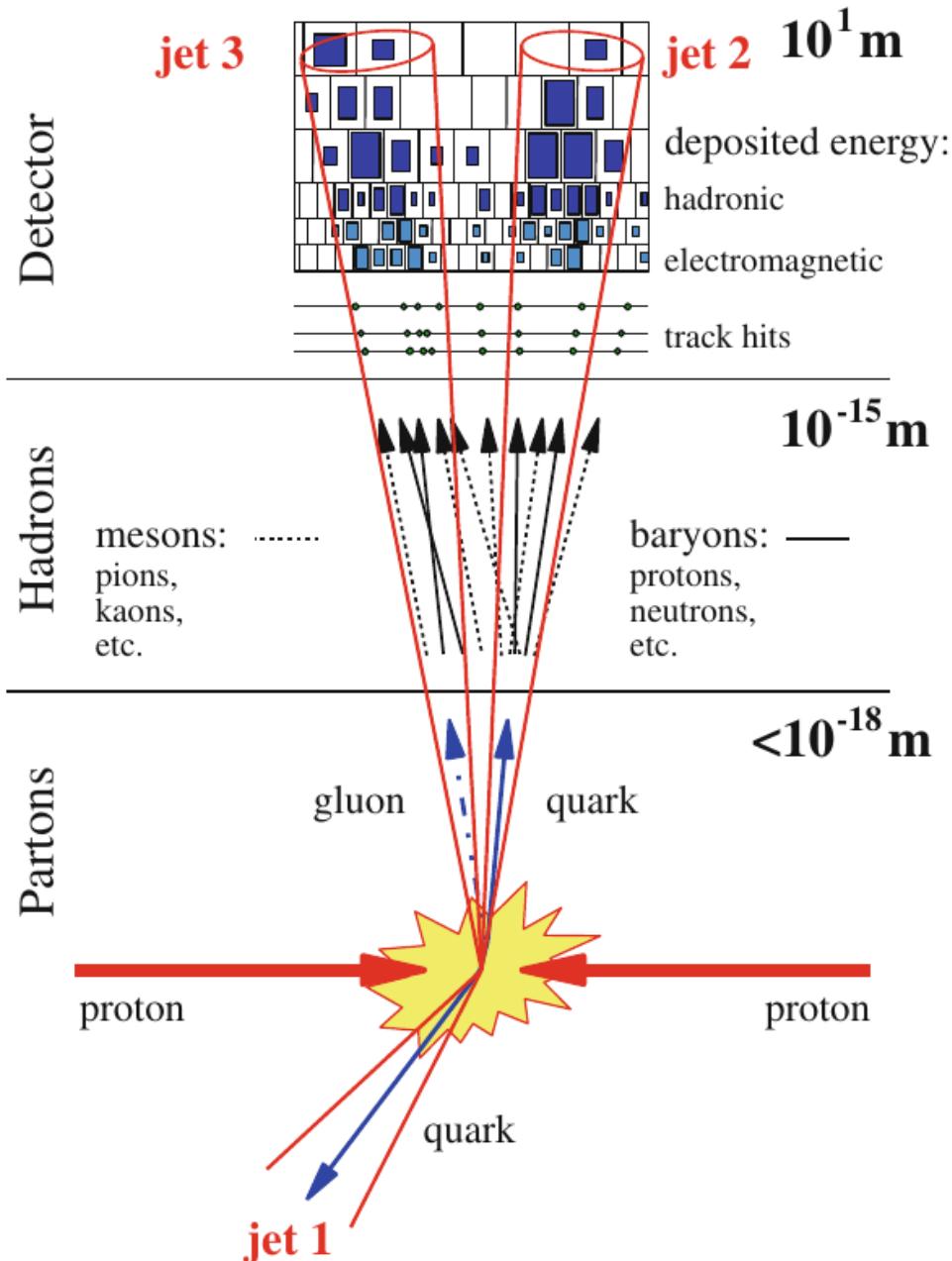
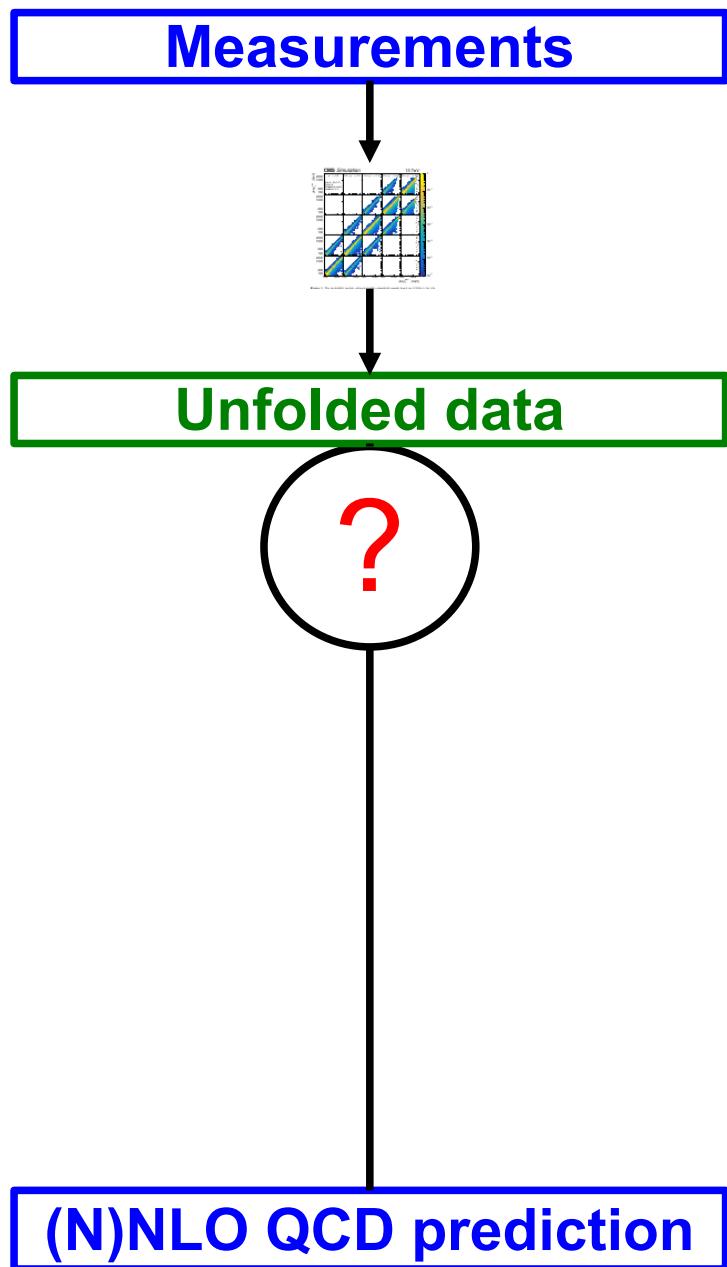
?

(N)NLO QCD prediction



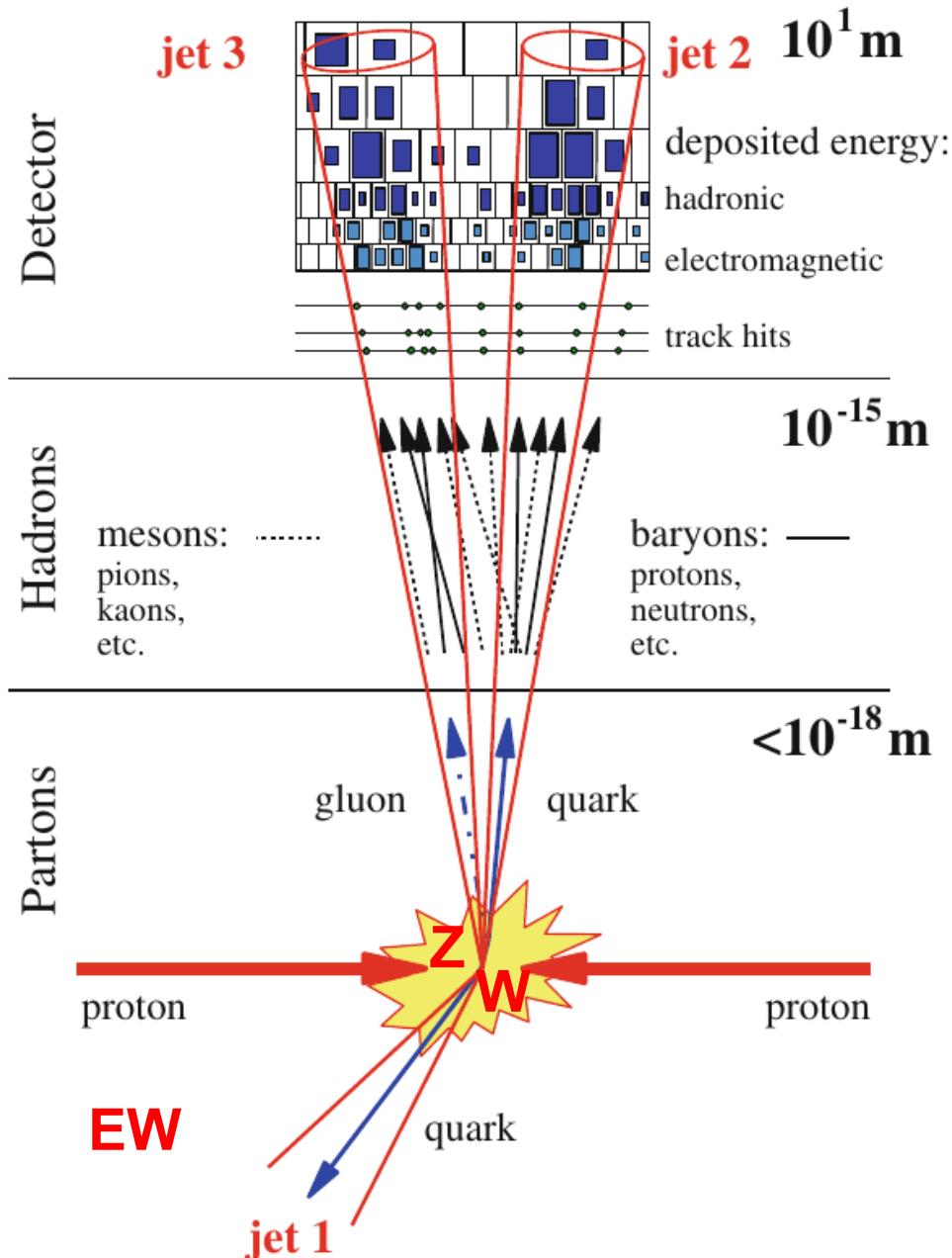
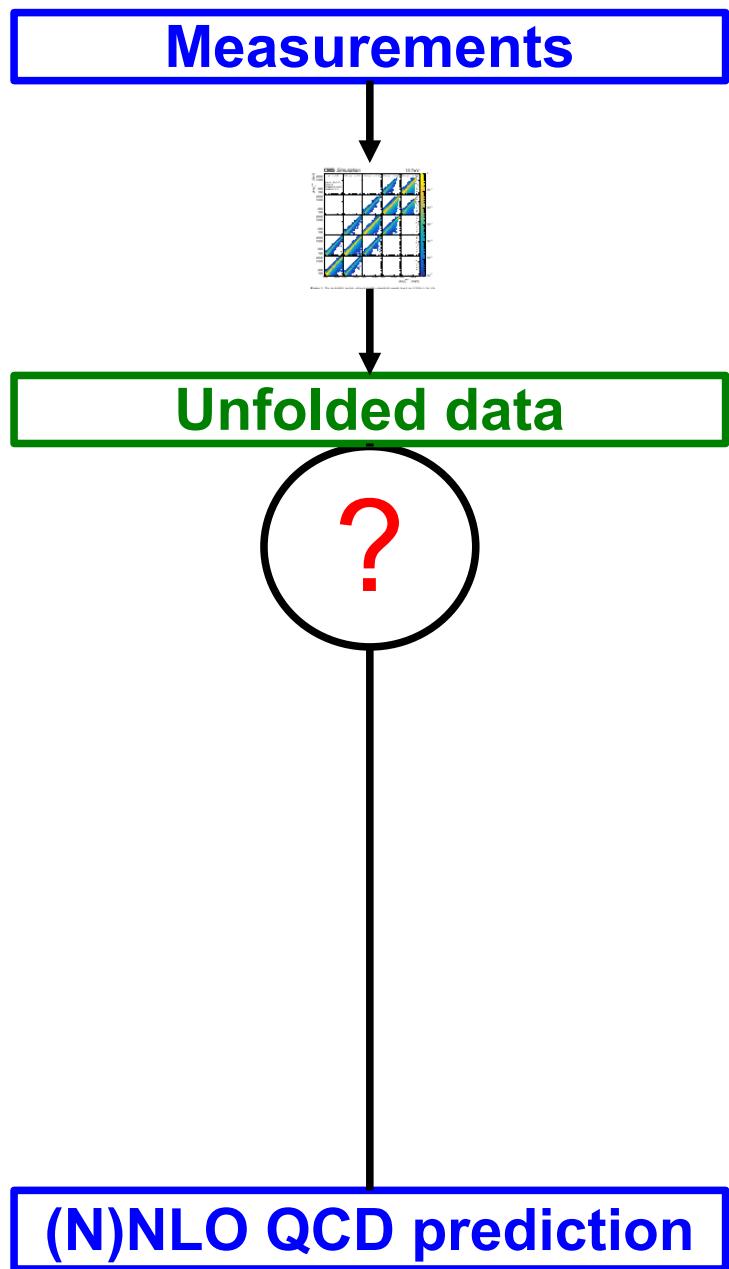


# Comparison data-theory



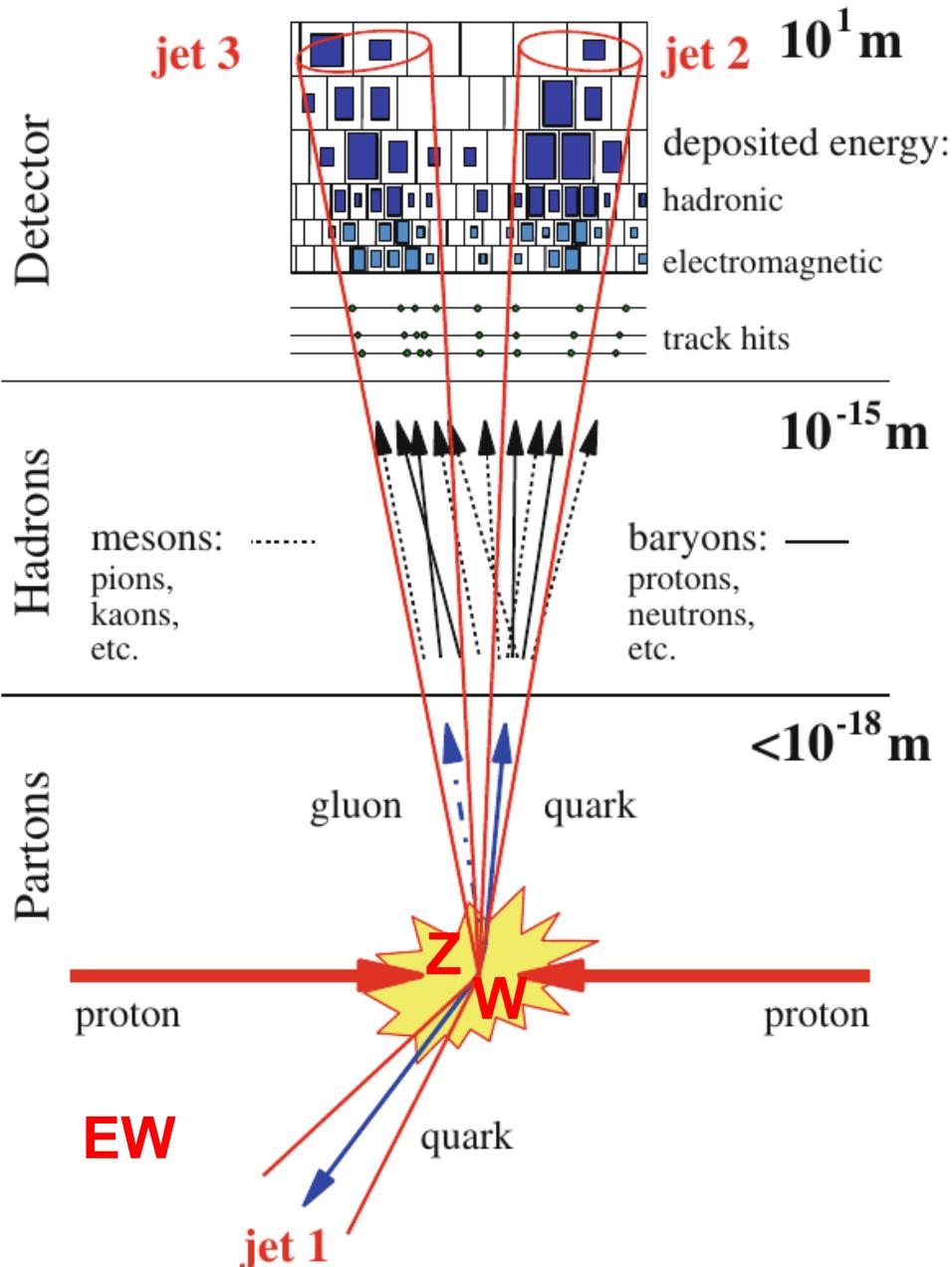
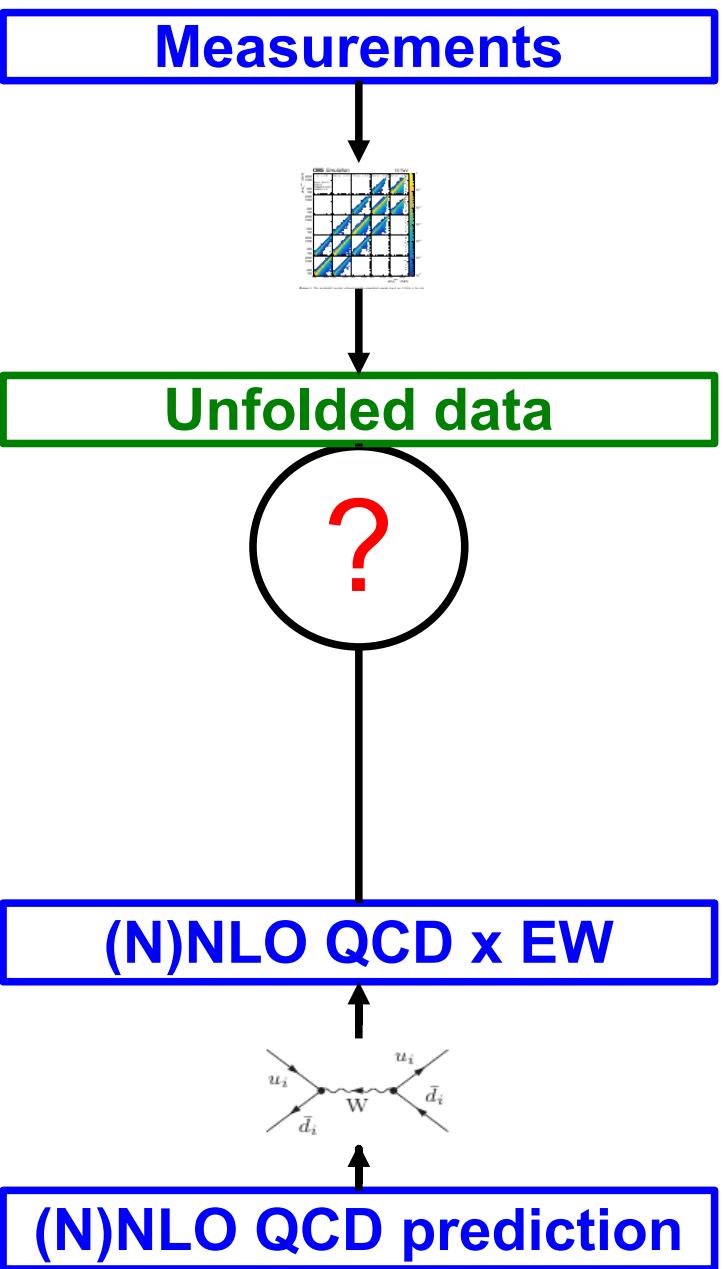


# Comparison data-theory



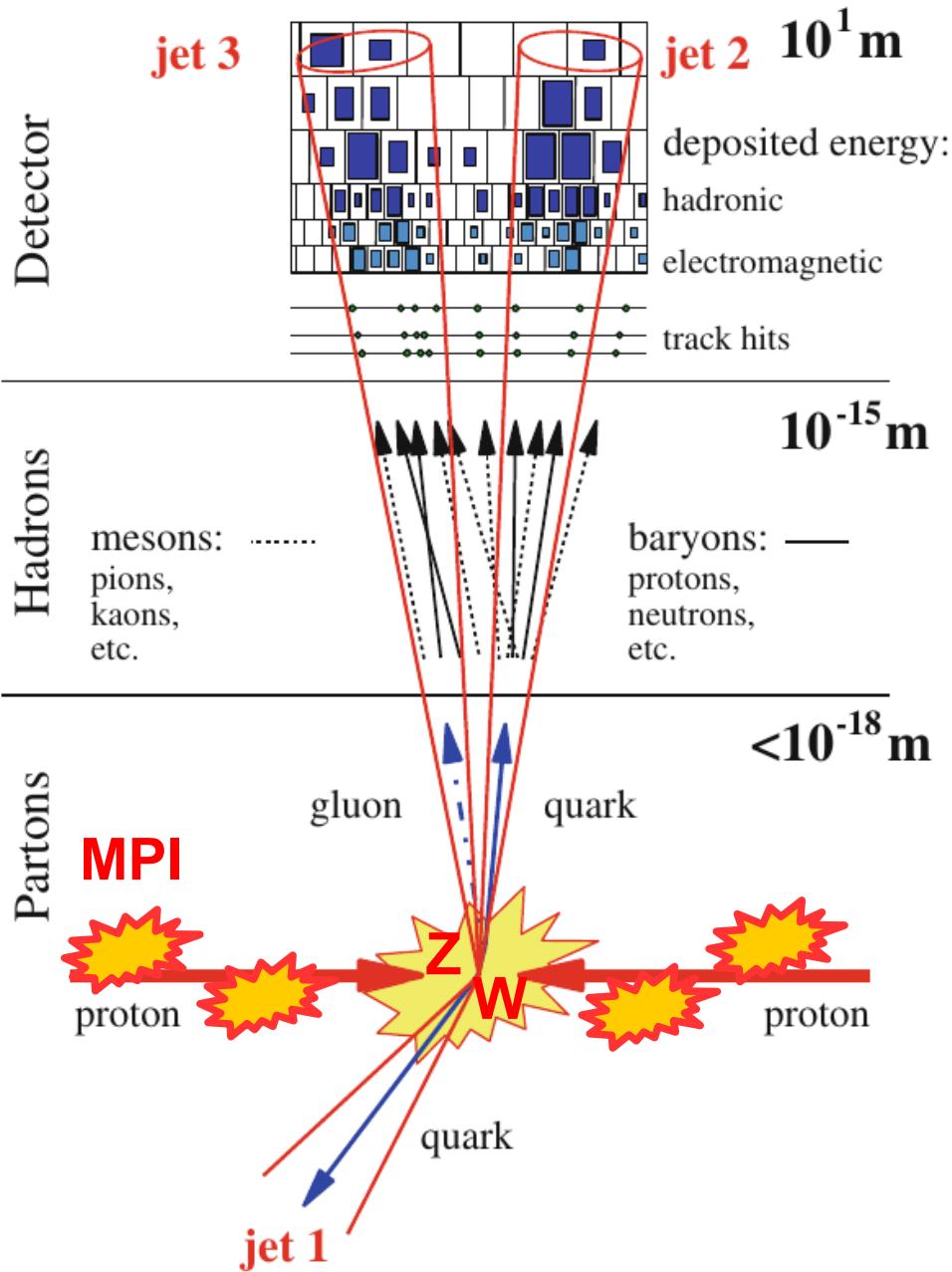
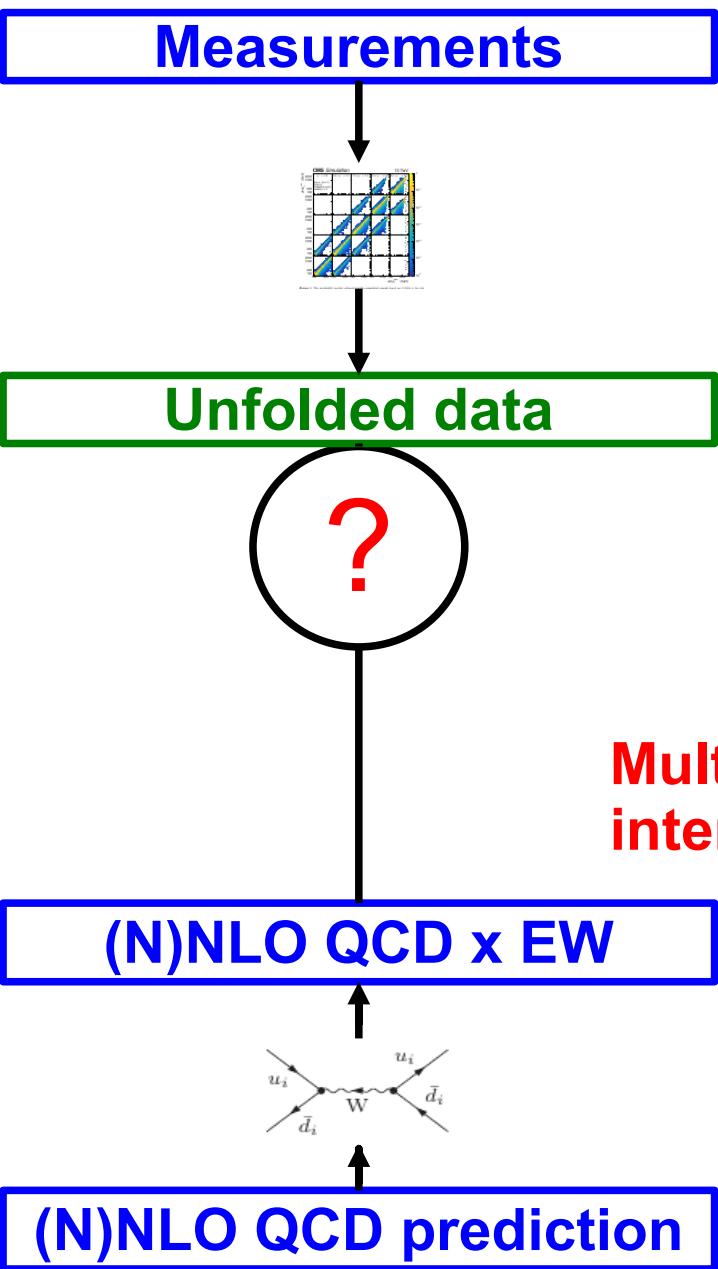


# Comparison data-theory



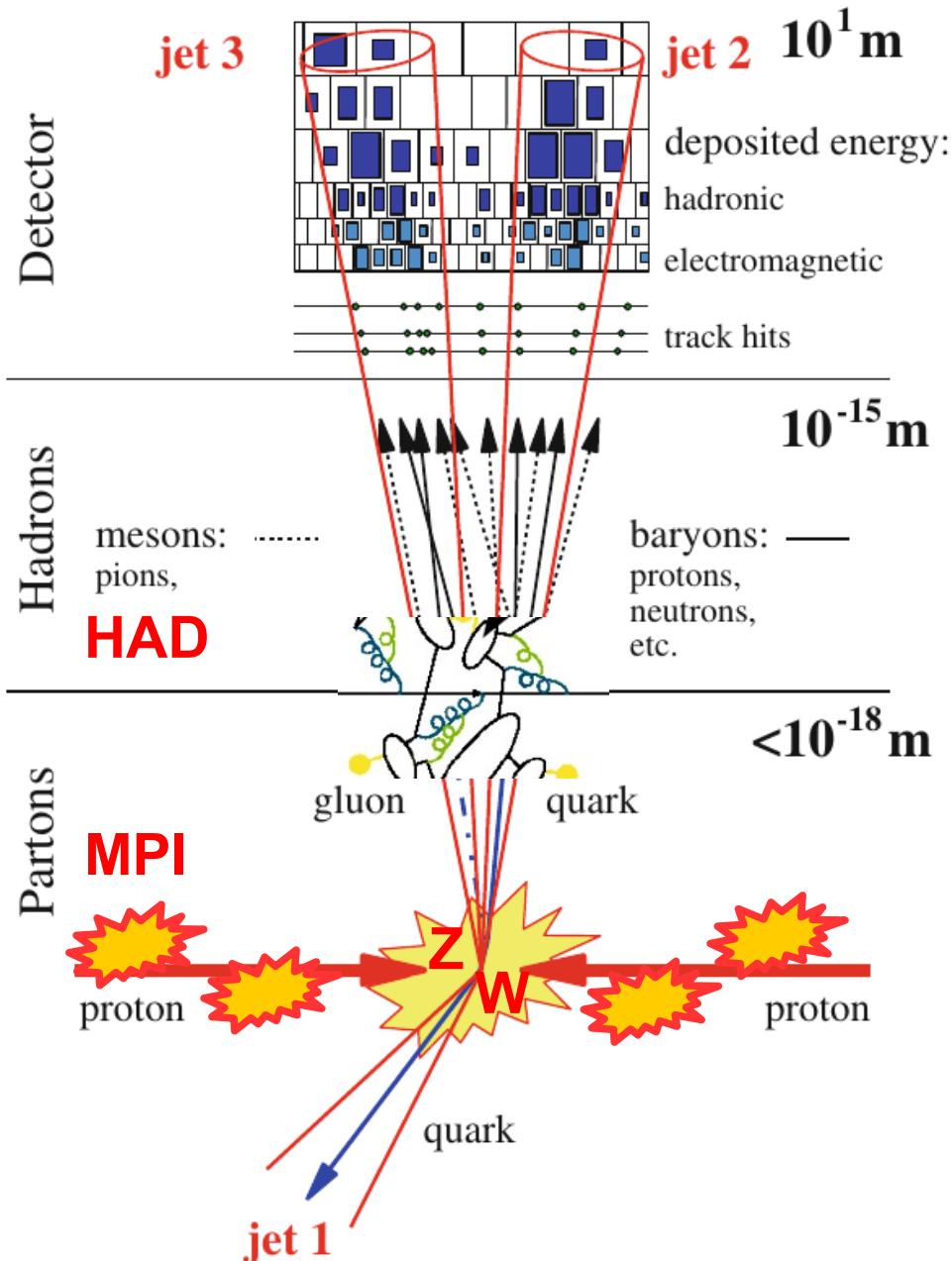
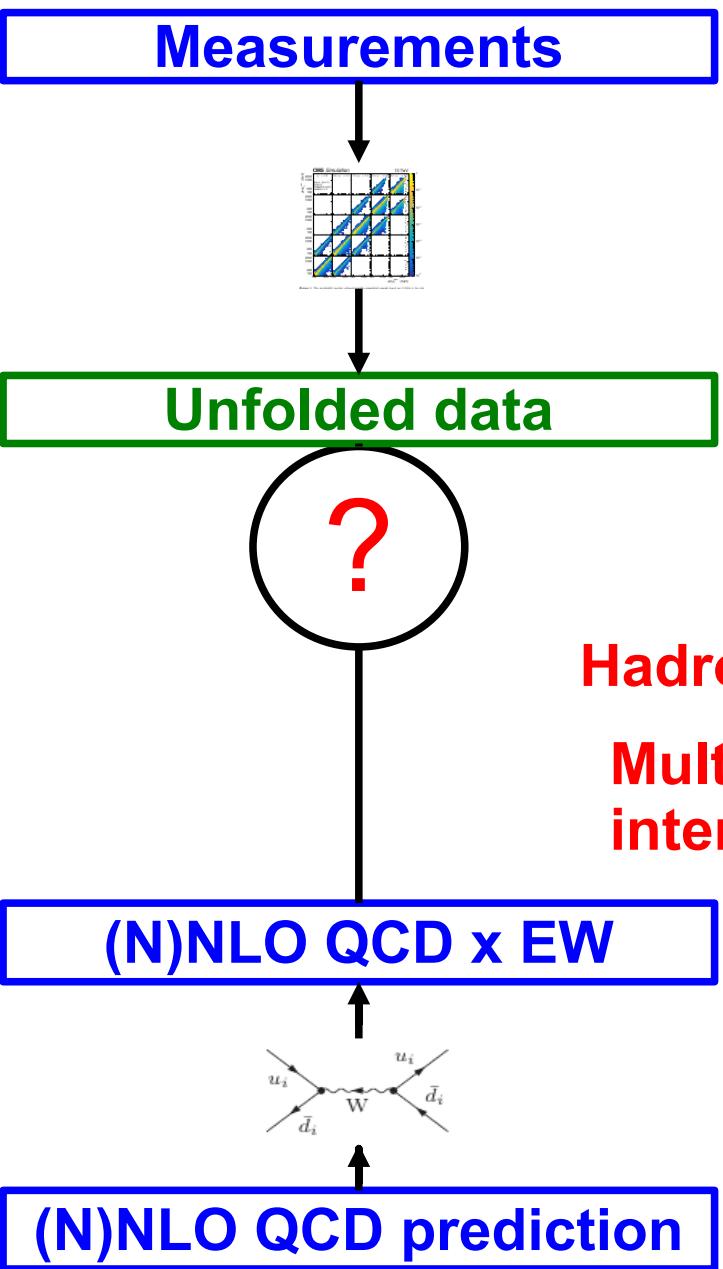
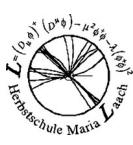


# Comparison data-theory



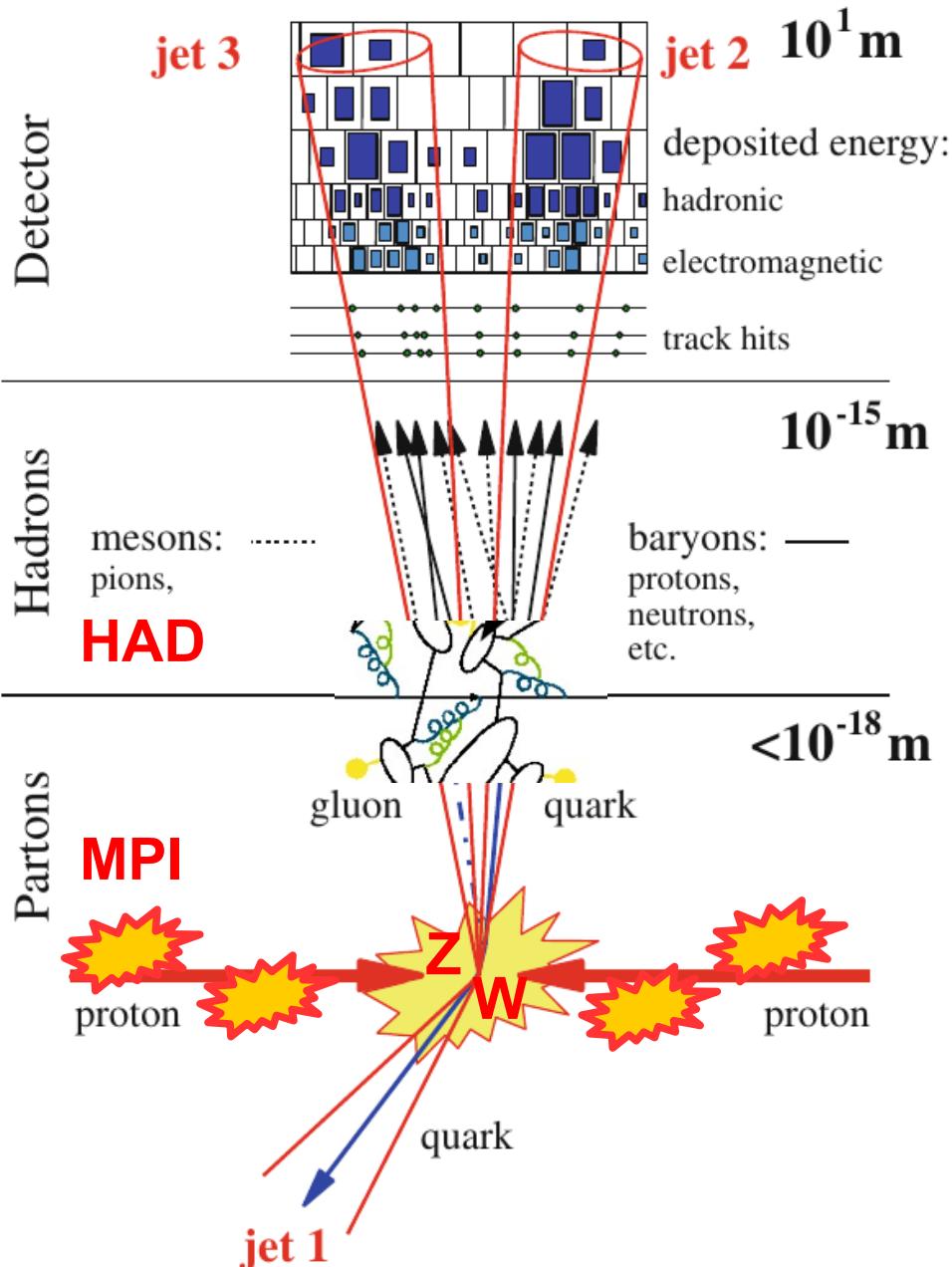
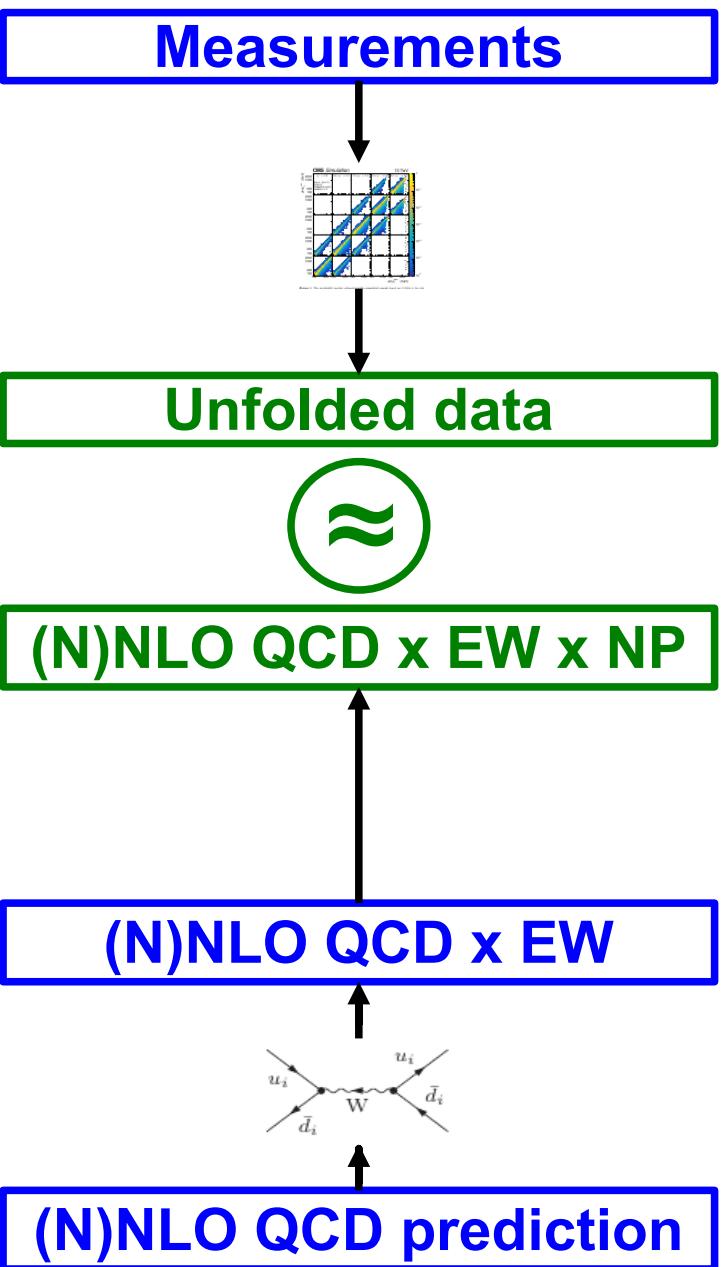


# Comparison data-theory





# Comparison data-theory

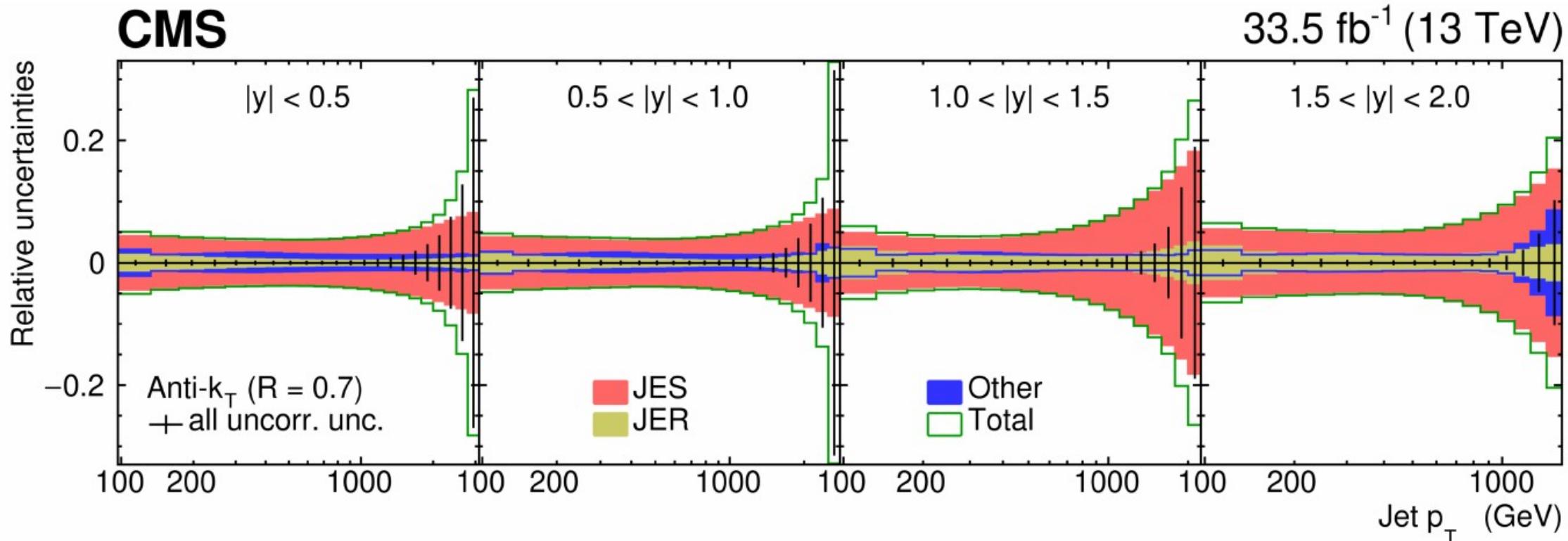




# Inclusive jets: exp. uncertainties

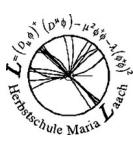


Of the order of 5%, larger at high  $y$  and  $p_T$   
Dominated by JES uncertainty (also JEC)  
Except at highest  $p_T \rightarrow$  statistical uncertainty





# Inclusive jets: theory corrections



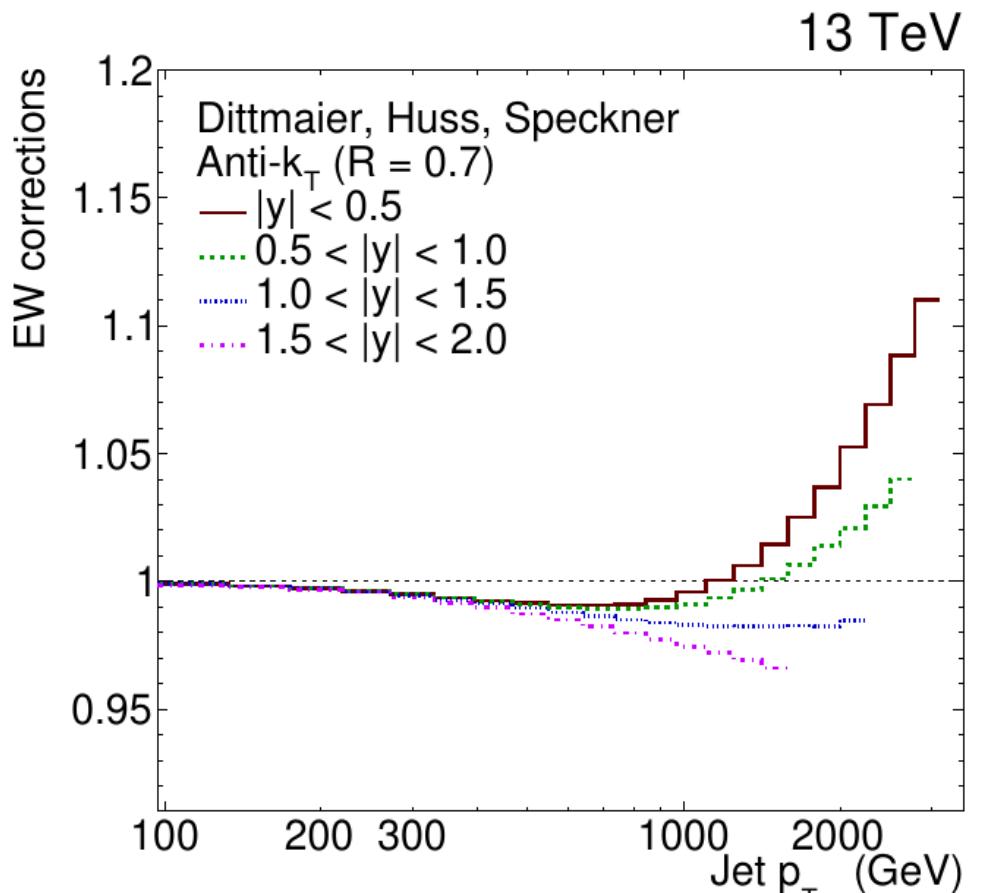
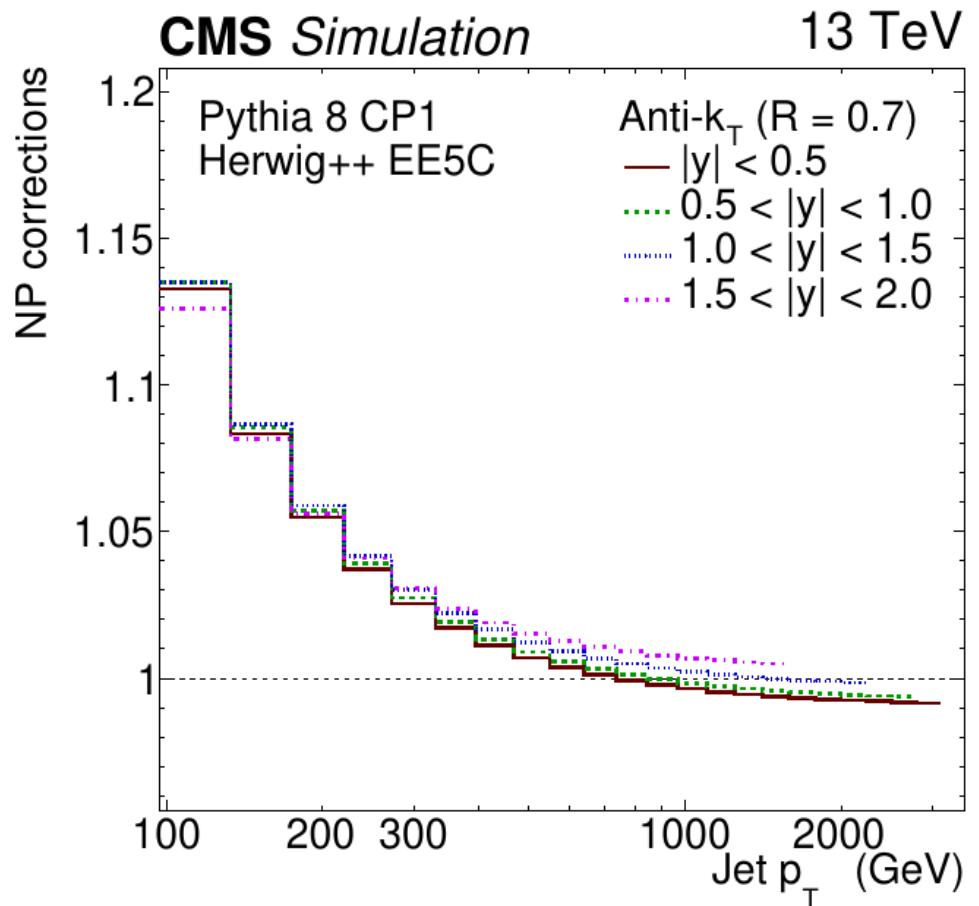
anti-kt, R=0.7, 13 TeV

## Nonperturbative correction factors:

- estimated from tuned MC event generators
- strongly dependent on jet size R
- less important at high  $p_T$

## Electroweak correction factors:

- calculated perturbatively
- strongly dependent on jet rapidity  $y$
- very important at high  $p_T$



Dittmaier, Huss, Speckner, JHEP 11 (2012) 095.



# Inclusive jets: theory corrections



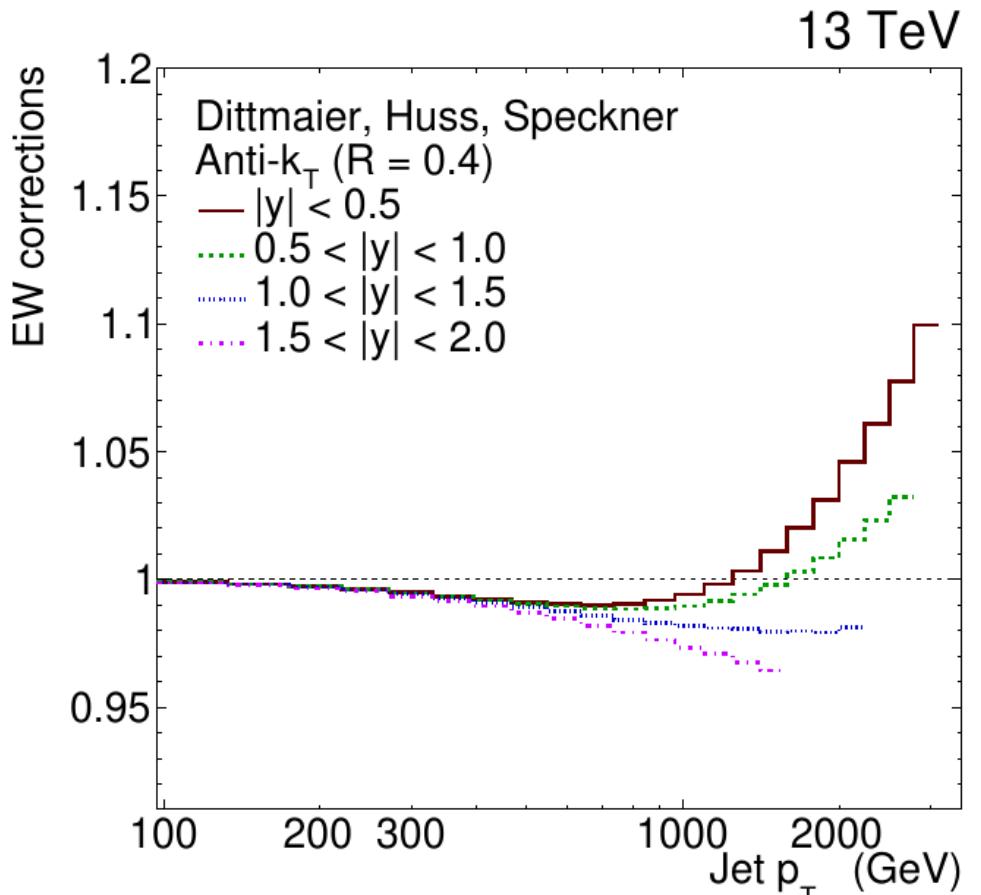
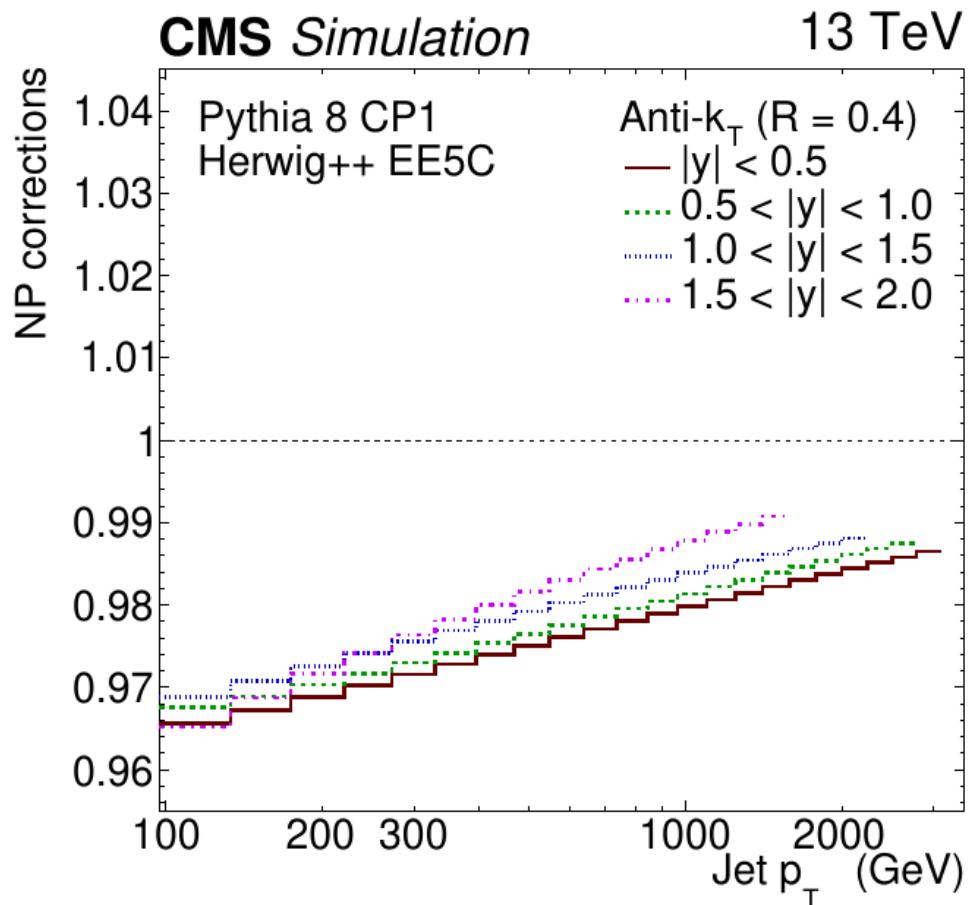
anti-kt, R=0.4, 13 TeV

## Nonperturbative correction factors:

- estimated from tuned MC event generators
- strongly dependent on jet size R
- less important at high  $p_T$

## Electroweak correction factors:

- calculated perturbatively
- strongly dependent on jet rapidity  $y$
- very important at high  $p_T$



Dittmaier, Huss, Speckner, JHEP 11 (2012) 095.



# Jet size dependence



## Jet $p_T$ shift as a function of $R$ for several sources:

• pert (Parton shower)  
scales with

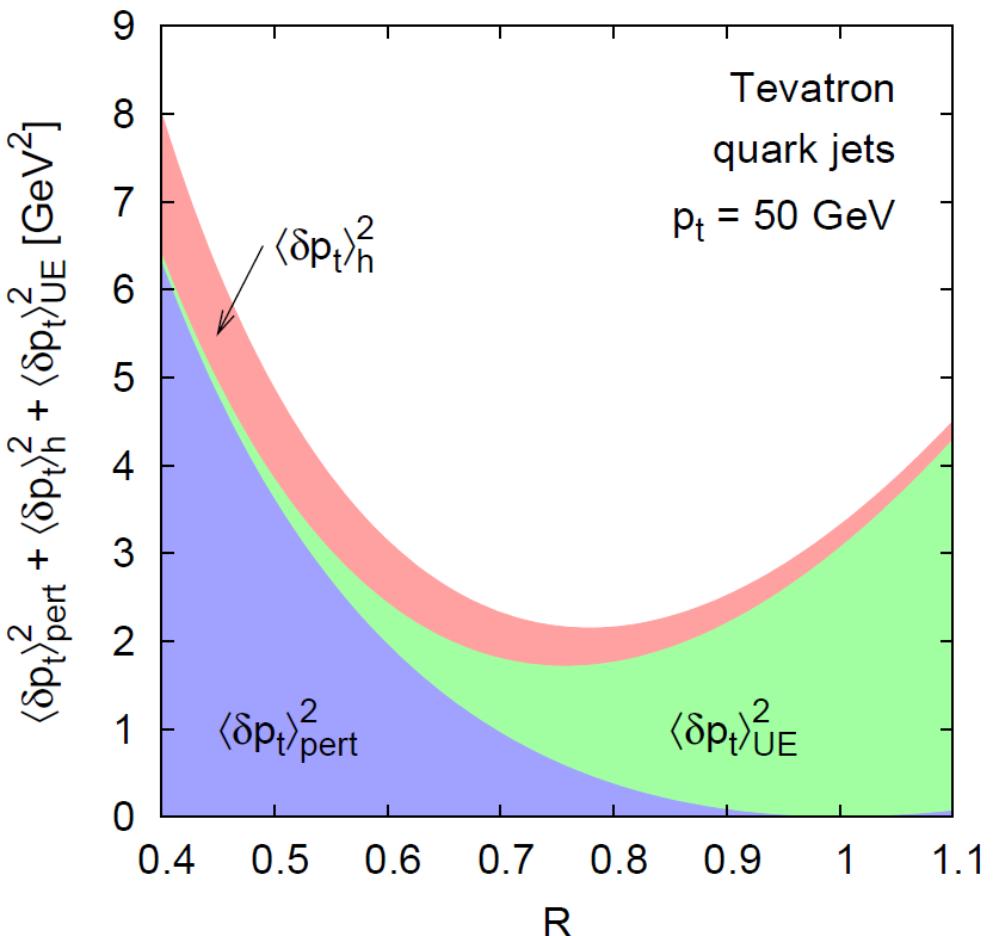
$$\ln(R) + \mathcal{O}(1)$$

• h (Hadronisation)  
scales with

$$-\frac{1}{R} + \mathcal{O}(R)$$

• UE (Multiple Parton Interactions)  
scales with

$$R^2 + \mathcal{O}(R^4)$$



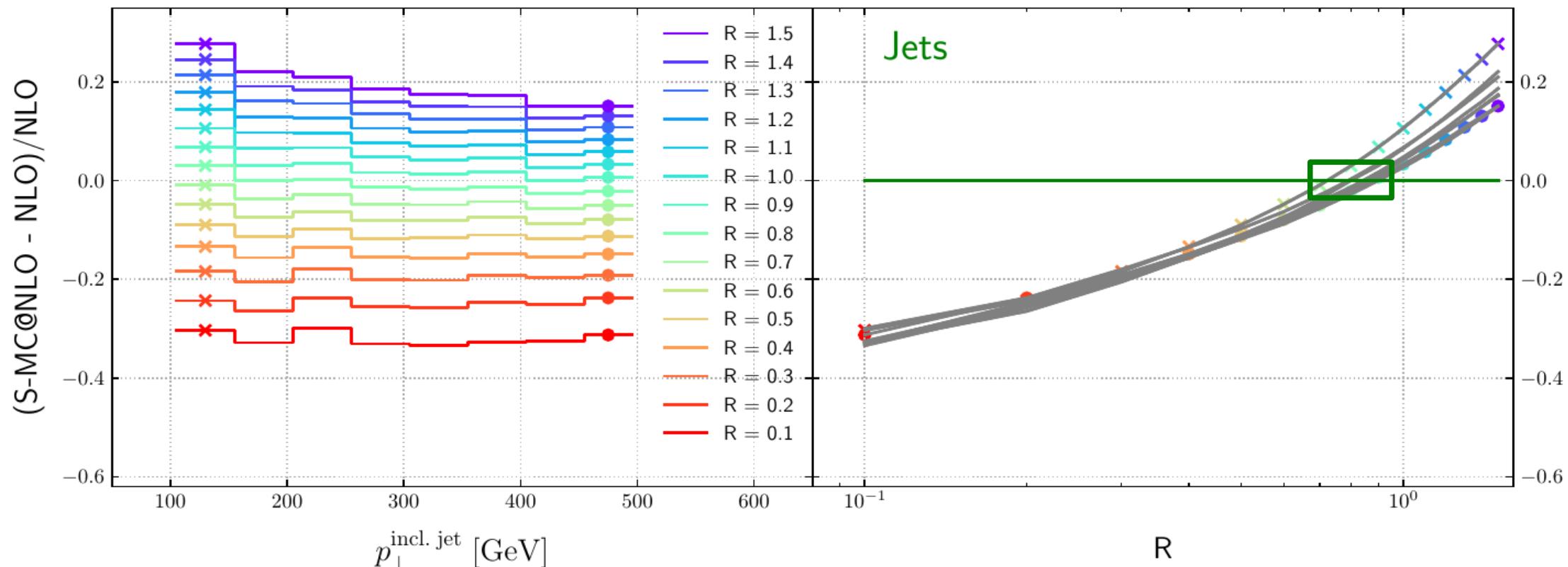
Dasgupta, Magnea, Salam, JHEP02 (2008) 055.



# Recent investigation on $R$ dep.



Relative difference between predictions of  
MC generator NLO+PS+MPI+HAD and NLO



Difference smallest for  $R$  around  $0.7 - 1.0 \rightarrow$  sweet spot!

Bellm et al., EPJC 80 (2020) 93.



# Chi<sup>2</sup> Fit



Data points  $D_i$

Theory prediction  $T_i$

$$\chi^2 = \sum_{ij}^N (D_i - T_i) C_{ij}^{-1} (D_j - T_j)$$



inverted  
covariance matrix  $C_{ij}$

$$C = \text{cov}_{\text{unf+stat}} + \text{cov}_{\text{uncor}} + \left( \sum_{\text{sources}} \text{cov}_{\text{JES}} \right) + \text{cov}_{\text{lumi}} + \text{cov}_{\text{PDF}}$$

All uncertainty components in fit incl. correlations!

Scale and NP uncertainty via extra fits → offset method

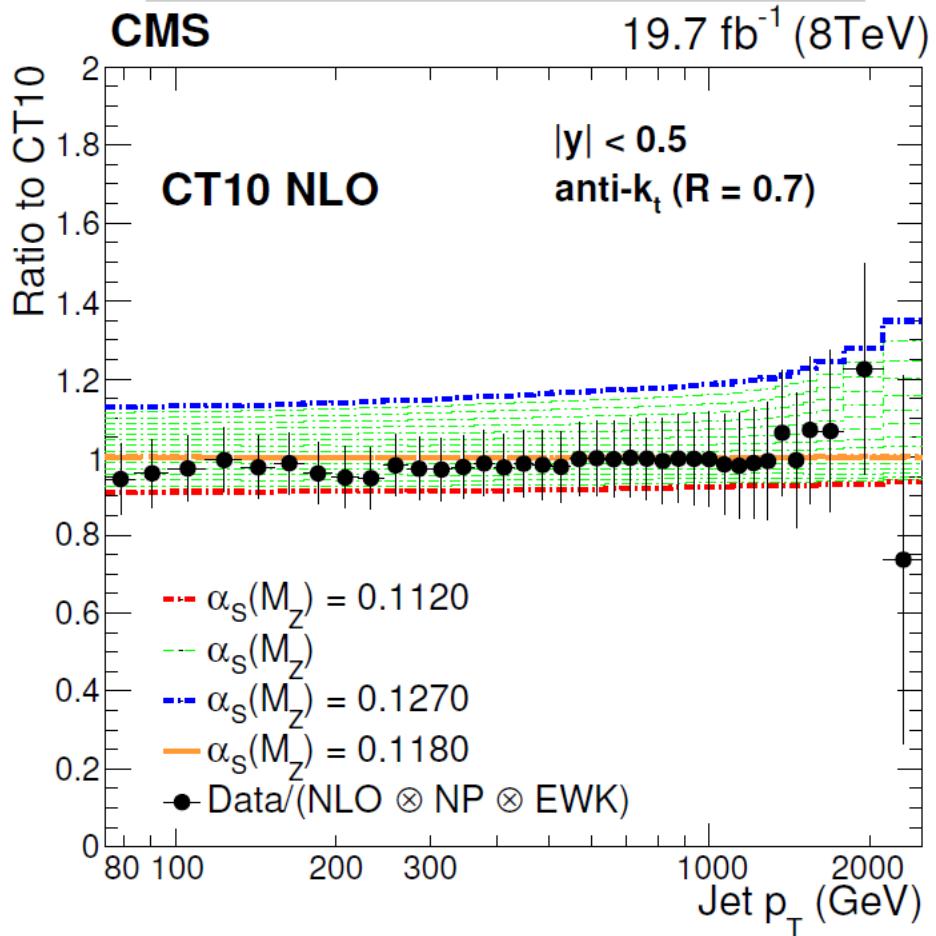


# Inclusive jets: $\alpha_s$



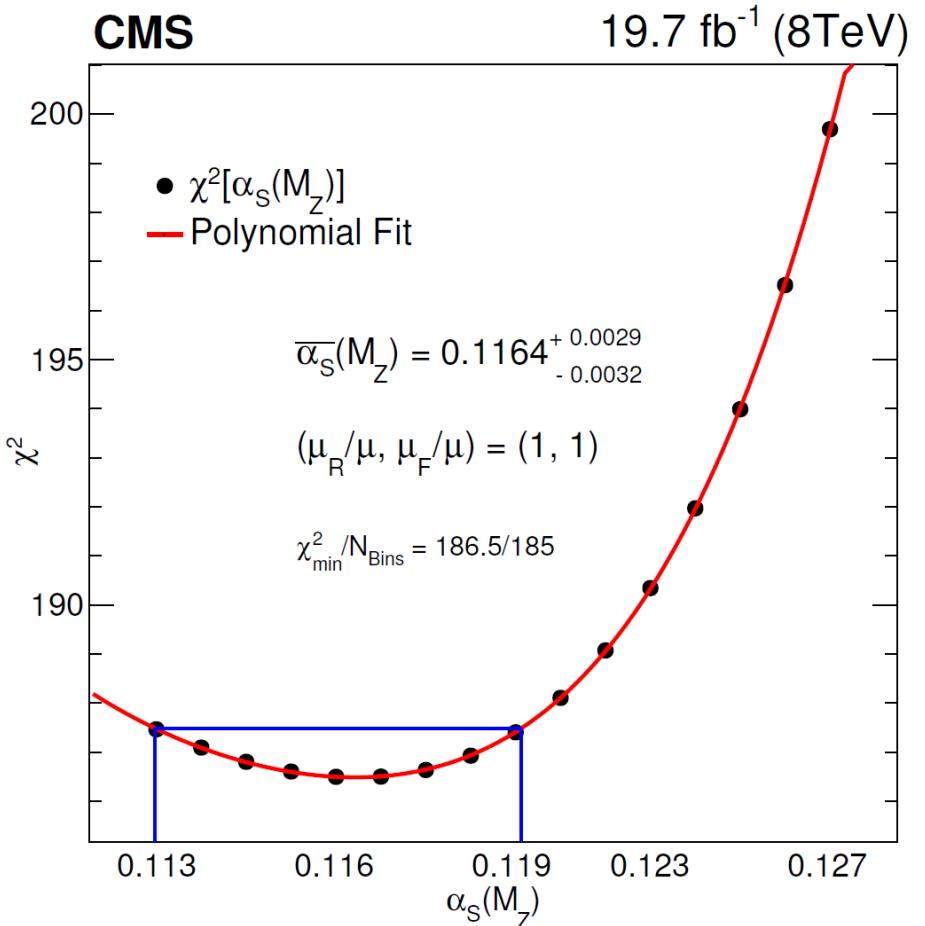
## Sensitivity to $\alpha_s(M_Z)$ at NLO

- CMS: anti- $k_t$   $R = 0.7$  at  $\sqrt{s} = 8$  TeV
- QCD scale choice:  $\mu_R = \mu_F = p_{T,jet}$



## $\chi^2$ fit of $\alpha_s(M_Z)$ for all jet $p_T$ and $|y|$ bins

- In fit: all exp. + PDF + NP uncertainties
- PDFs: CT10 NLO PDF sets for various  $\alpha_s(M_Z)$



Example from older analysis at 8 TeV!



# Scale dependence



Jet cross section to all orders in perturbative QCD:

$$\sigma(pp \rightarrow jj + X) \propto \sum_{n=2}^{\infty} c_n(\mu_r) \alpha_s^n(\mu_r)$$

**LO Coefficient, here  $c_2$  independent of scale  $\mu_r$ :**  $c_2(\mu_r) \equiv c_2$

**Coefficients of higher orders depend on  $\mu_r$  and renorm.- scheme, e.g.:**

**Infinite series independent of  $\mu_r$ :**  $\overline{\text{MS}}$   $\mu_r^2 \frac{d}{d\mu_r^2} \sum_{n=2}^{\infty} c_n(\mu_r) \alpha_s^n(\mu_r) = 0$

**Not so the truncated one!**

$$\mu_r^2 \frac{d}{d\mu_r^2} \sum_{n=2}^N c_n(\mu_r) \alpha_s^n(\mu_r) \propto \mathcal{O}(\alpha_s^{N+1}(\mu_r))$$

**So for example:**

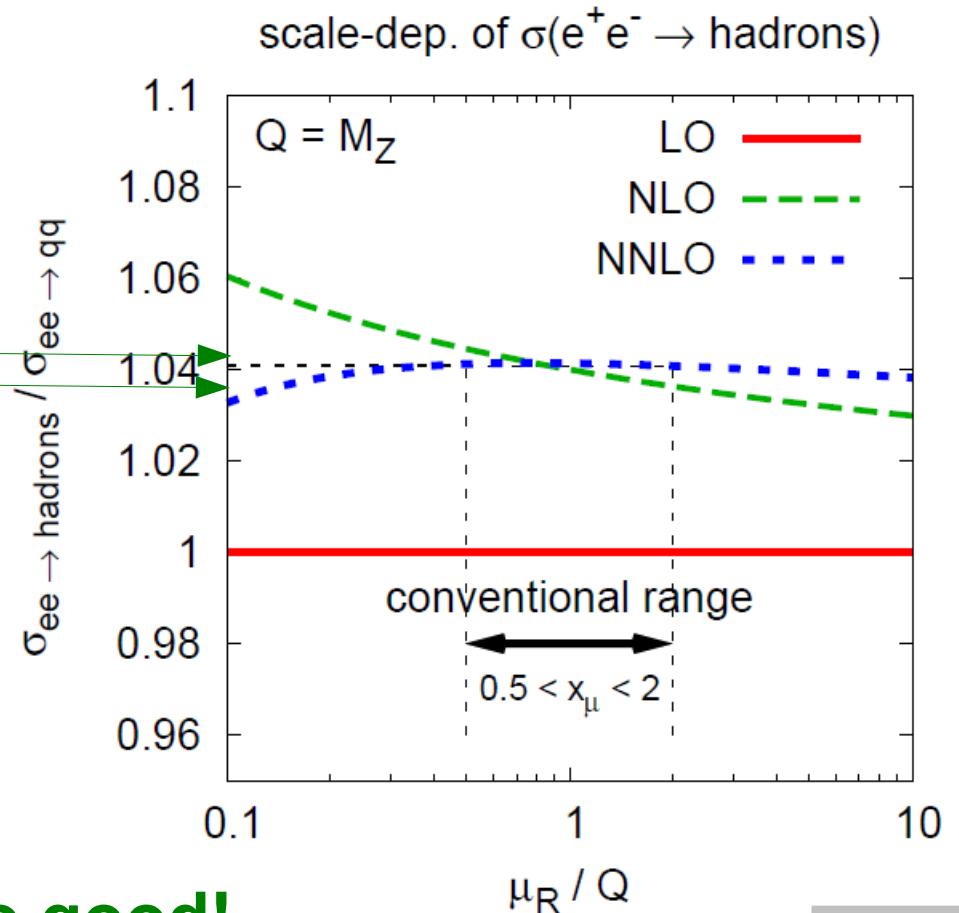
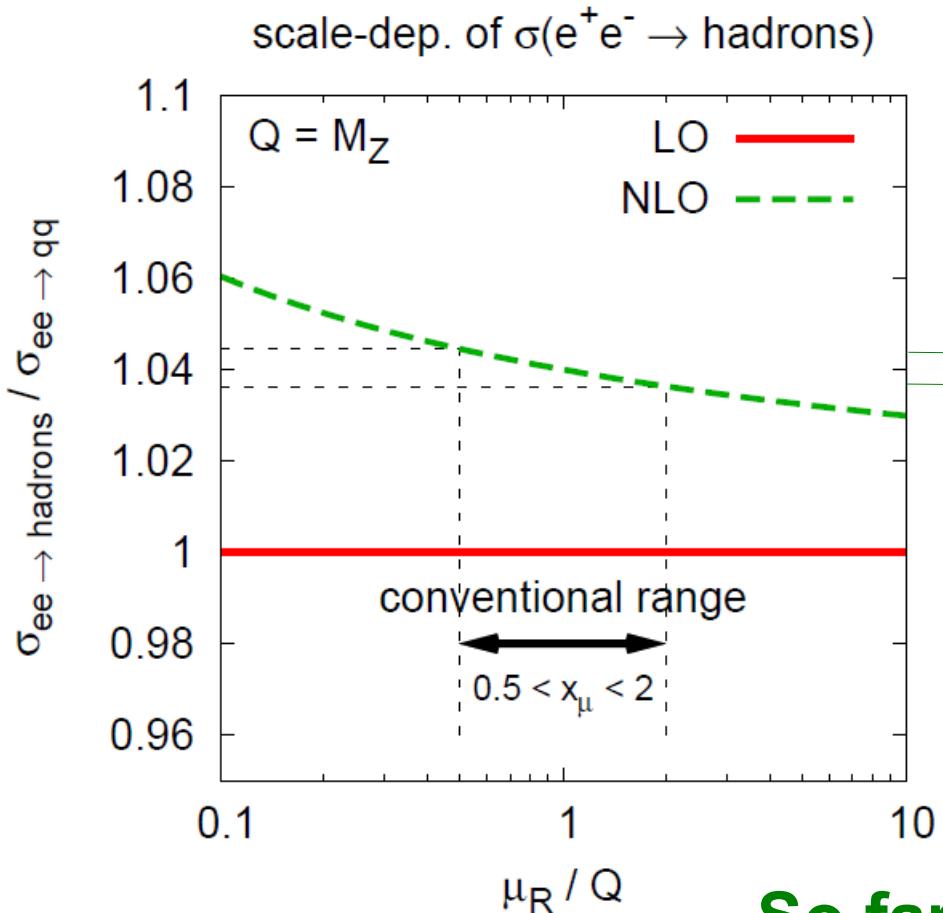
$$c_3(Q) = c_3(1) + \frac{\beta_0}{2\pi} \ln\left(\frac{\mu_r}{Q}\right) c_2$$



# Conventional recipe



- Large LO scale dependence  $\sim \alpha_s(\mu_r)$
- Increasingly compensated by further terms
- Recipe(!): Estimate impact of higher orders by  $\mu_r$  variation



So far so good!

G. Salam,  
arxiv:1011.5131

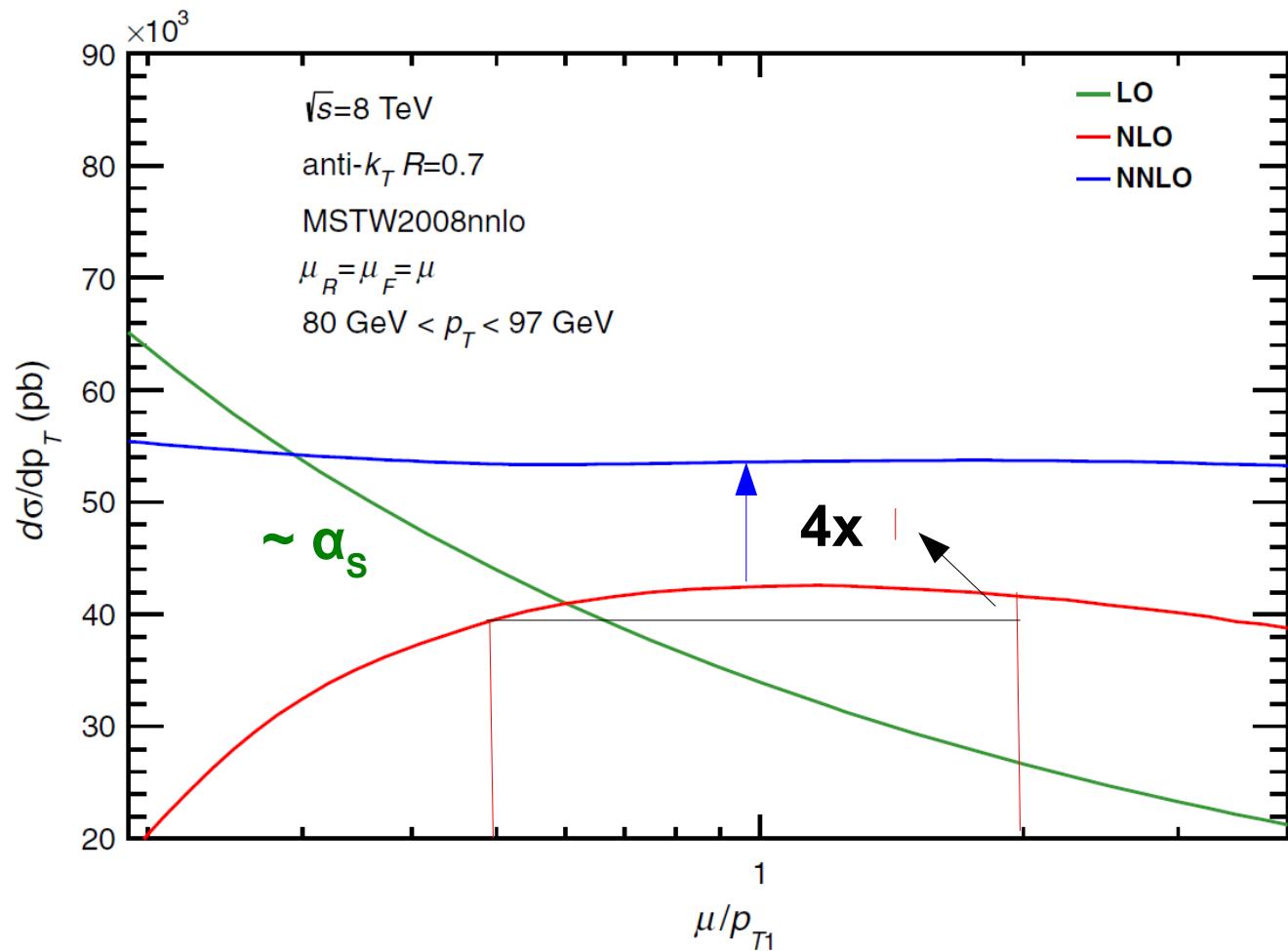


# Problems 1



Can go wrong, if e.g.:

## 1) Base scale badly chosen



Scale is:

$p_T$  leading jet:  $p_{T1}$

Looks much better, if  
respective jet  $pT$  is  
used!

Example plot of dep.:  
inklusive Jets,  $gg \rightarrow \text{jets}$

Gehrmann-De Ridder, Gehrmann, Glover, Pires,  
Phys. Rev. Lett., 2013, 110, 162003

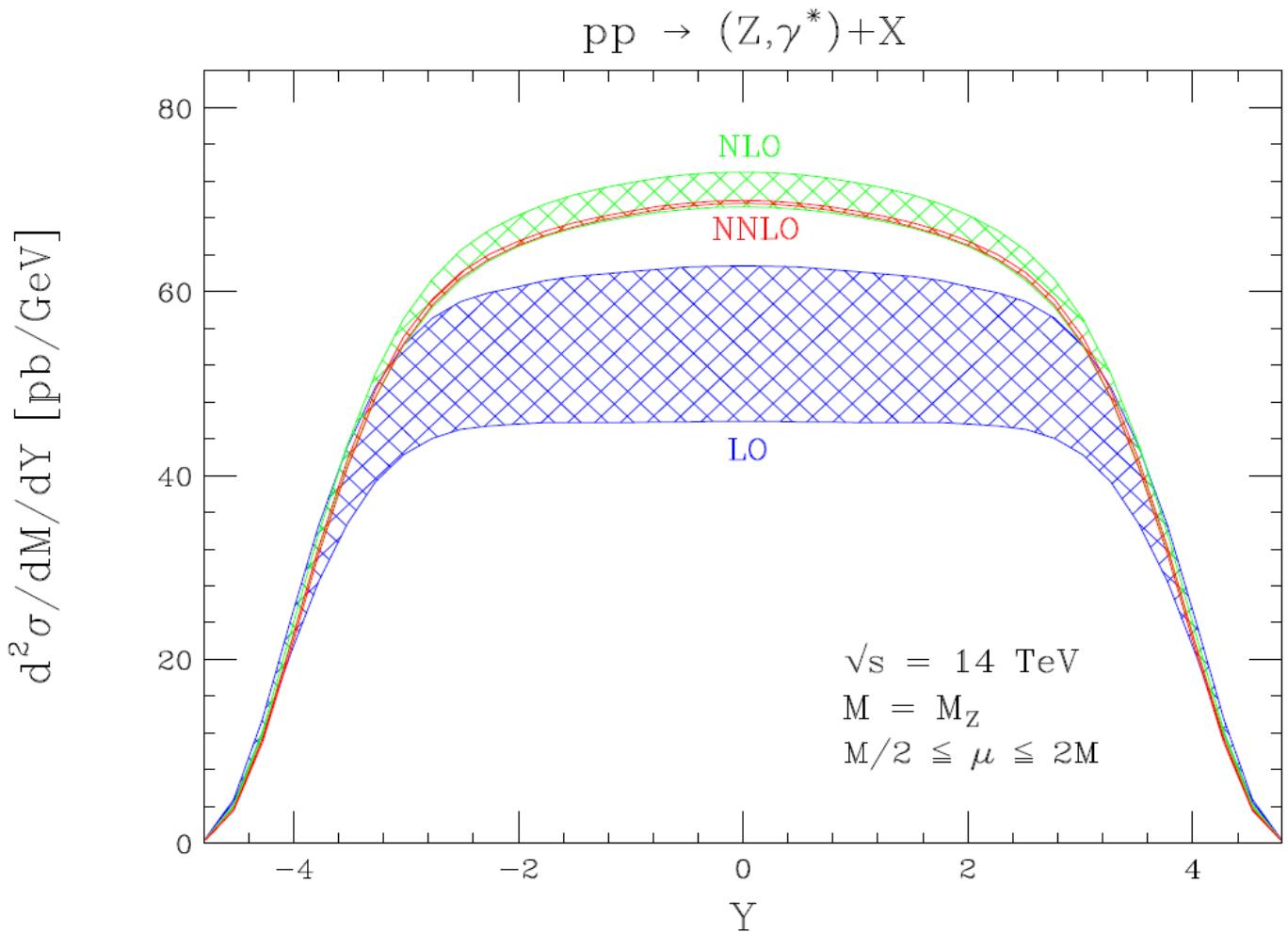


# Problems 2



Can go wrong, if e.g.:

- 1) Base scale badly chosen
- 2) In multi scale problems, e.g. Z+jet production



$M_Z$  or  $p_{T,\text{jet}}$  as scale?  
Both can be sensible,  
depends on phase  
space.

Anastasiou, Dixon, Melnikov, Petriello,  
Phys. Rev. D, 2004, 69, 094008



# Problems 3



Can go wrong, if e.g.:

- 1) Base scale badly chosen
- 2) In multi scale problems, e.g. Z+jet production
- 3) New production channels or graph types appear

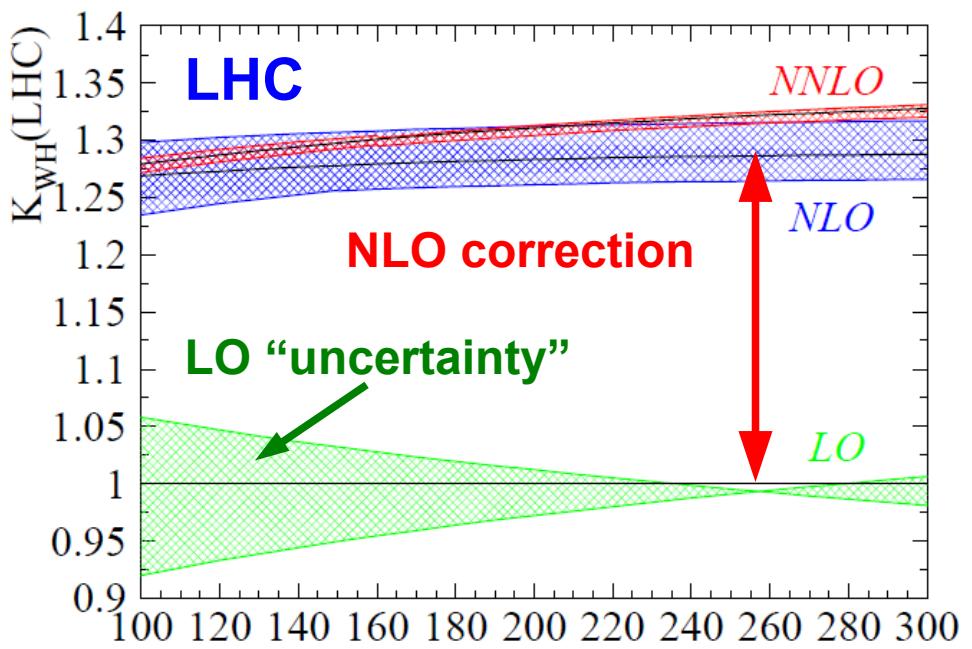
Process: Higgs radiation:  $\text{pp} \rightarrow \text{HV} + \text{X}$

Scale choice:

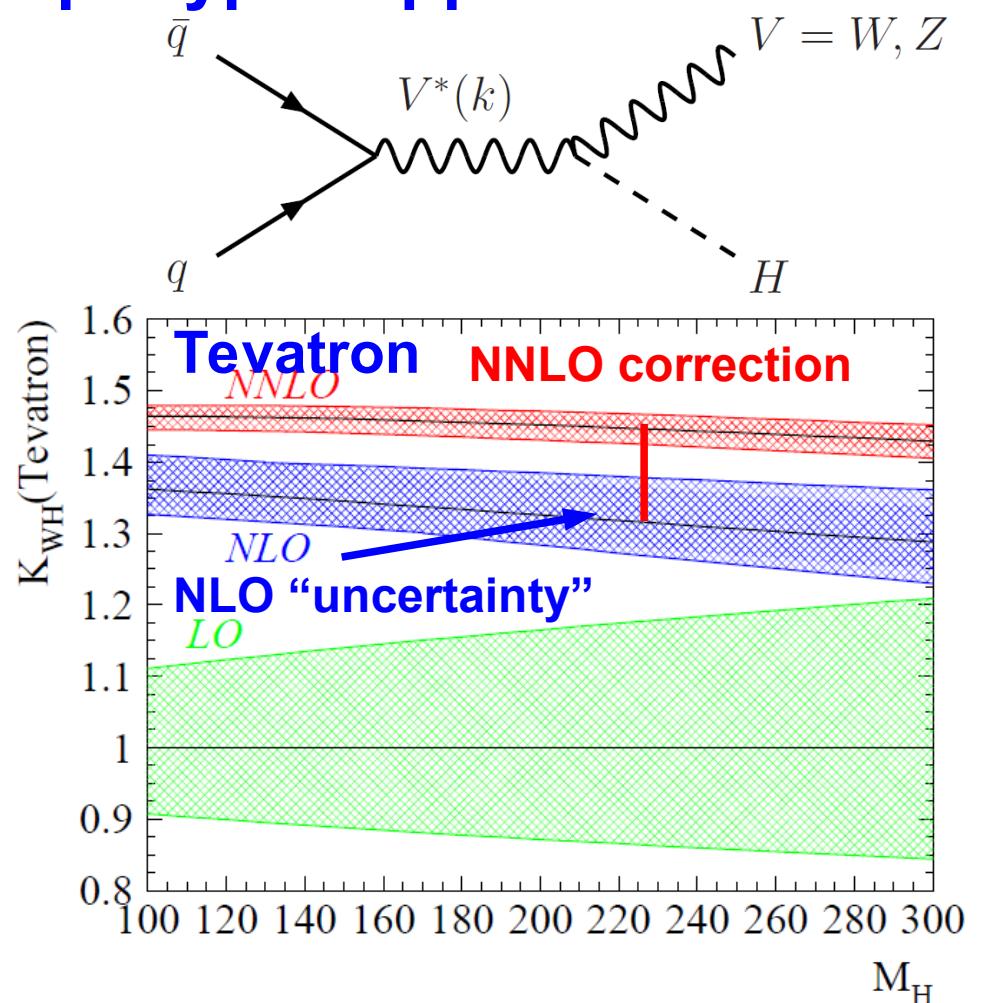
$$M_{\text{HV}}$$

Scale variation  $\mu_{r,f}/M_{\text{HV}}$ :

$$1/3 \dots 3$$

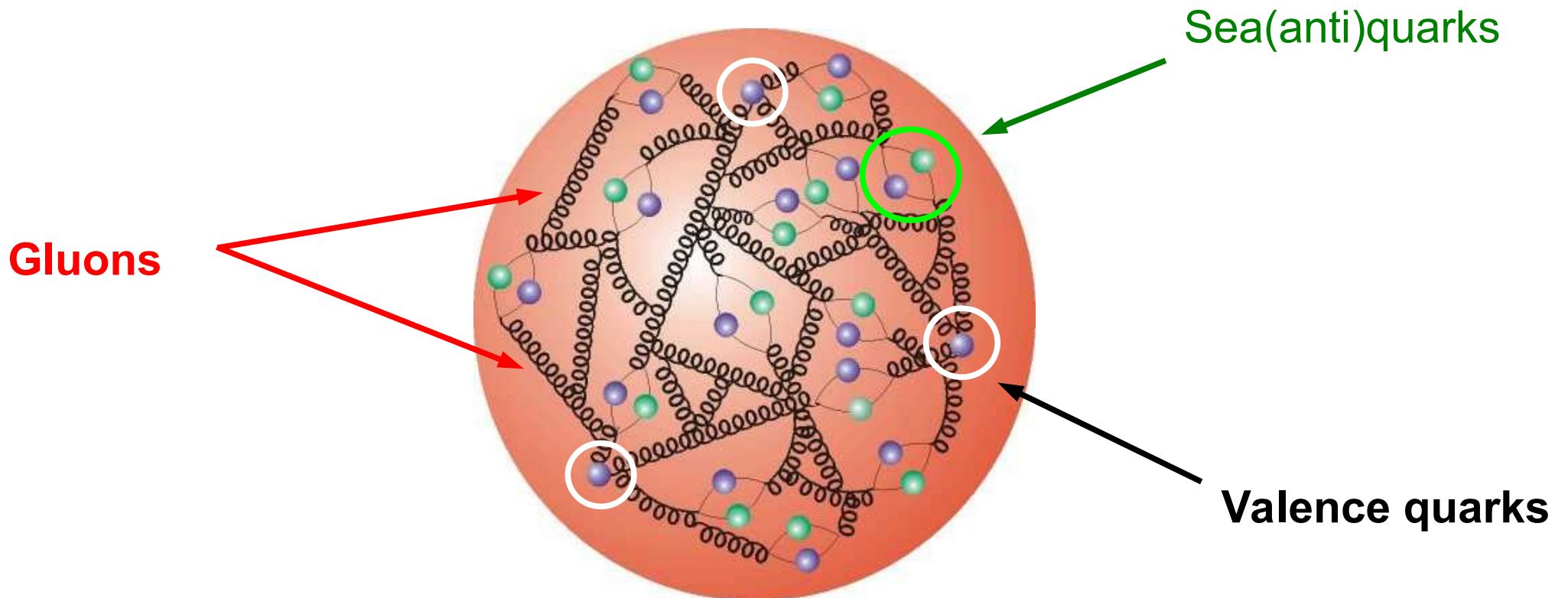
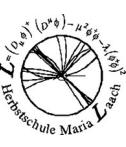


Brein, Djouadi, Harlander,  
Phys.Lett. B579 (2004) 149.



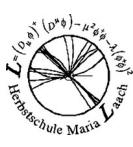


# Constraining PDFs





# Correlation $\sigma$ - PDF

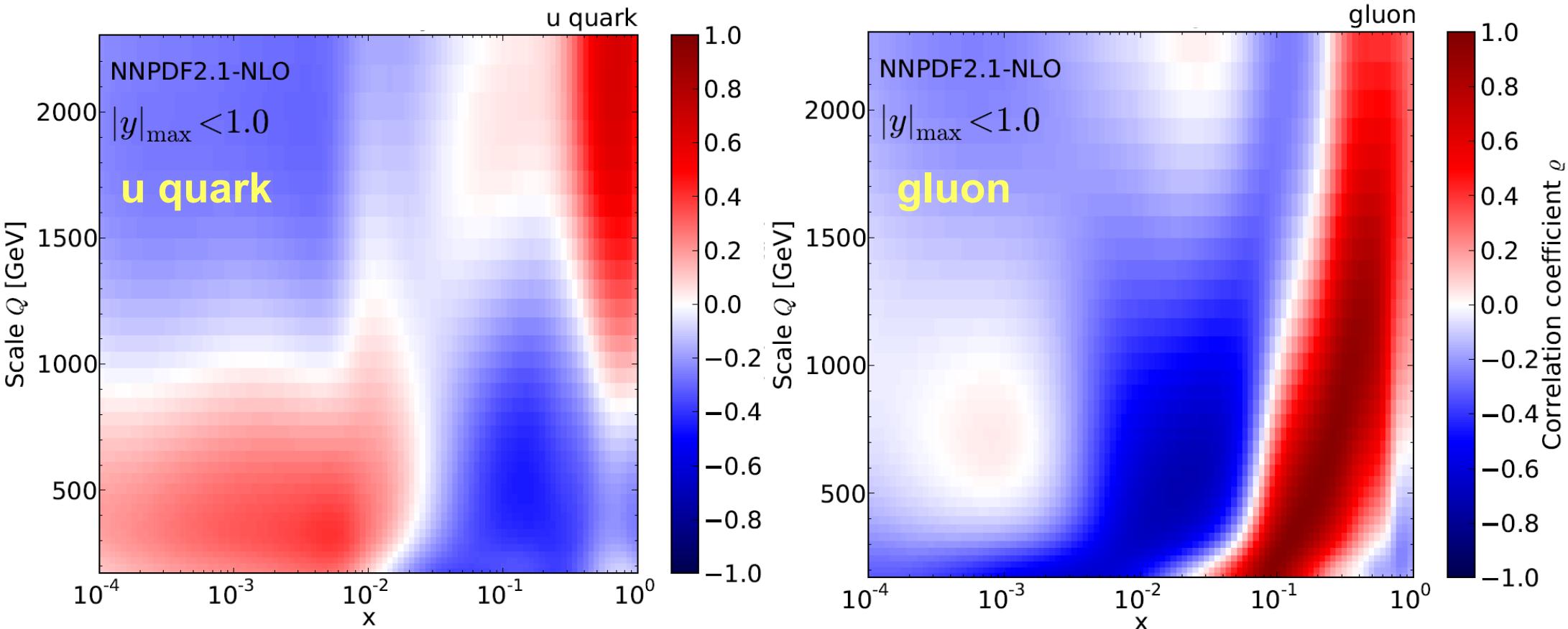


## Measurement of inclusive jets at large pT impacts:

- Gluon density at large  $x$  ( $> 0.1$ )
- Quark density at large  $x$  ( $> 0.3$ )

Works nicely with statistical ensemble uncertainties of NNPDF!

$$\rho_f(x, Q) = \frac{N}{(N-1)} \frac{\langle \sigma_{\text{jet}}(Q)_i \cdot xf(x, Q^2)_i \rangle - \langle \sigma_{\text{jet}}(Q)_i \rangle \cdot \langle xf(x, Q^2)_i \rangle}{\Delta_{\sigma_{\text{jet}}(Q)} \Delta_{xf(x, Q^2)}}.$$





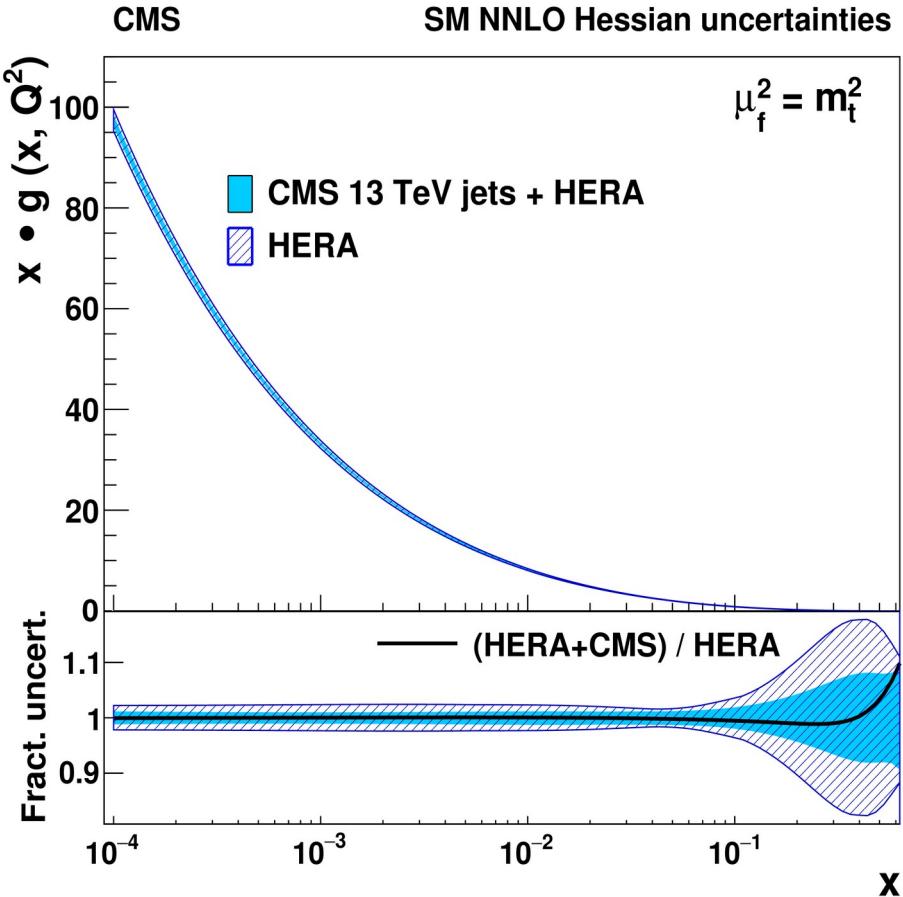
# Inclusive jets: $\alpha_s$ & PDFs



Simultaneous fit of  $\alpha_s$  & PDFs possible combining HERA DIS & CMS jet data using xFitter Tool

CMS result for  $\alpha_s(M_Z)$  at NNLO:  $\alpha_s(m_Z^2) = 0.1166 \pm 0.0016(\text{fitall}) \pm 0.0004(\text{scl})$

Reduced uncertainties of gluon PDF



xFitter (HERAFitter): Alekhin et al., EPJC 75 (2015) 304.



# Inclusive jets: $\alpha_s$ & PDFs

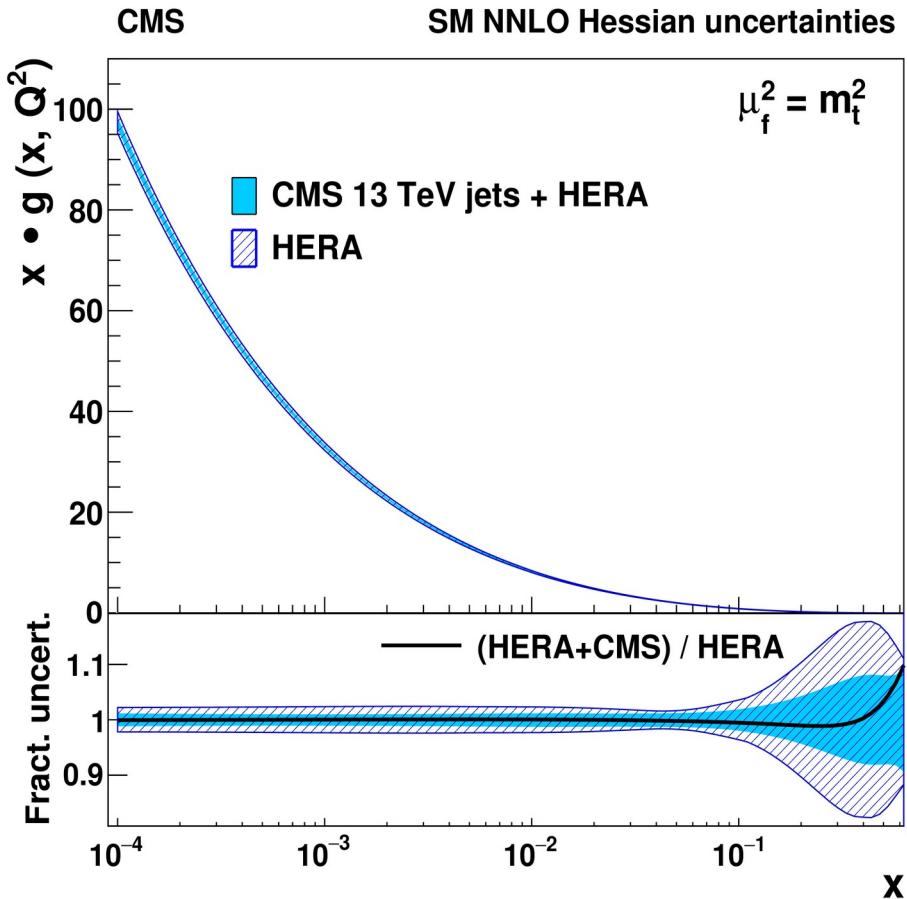


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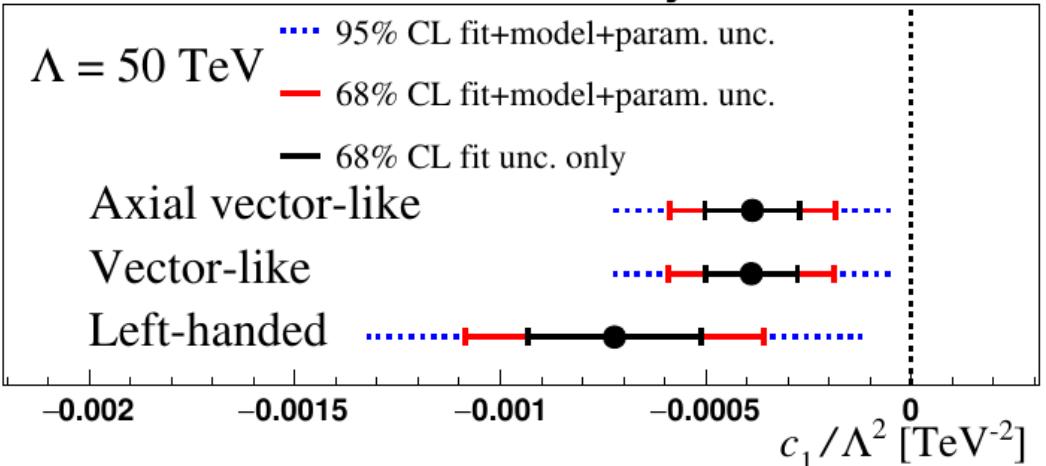


xFitter (HERAFitter): Alekhin et al., EPJC 75 (2015) 304.

Also NLO fit of  $\alpha_s$  & PDFs & CI  
Data compatible with SM  $\rightarrow$  exclusion limits

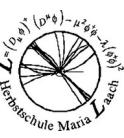
$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{2\pi}{\Lambda^2} \sum_{n \in \{1,3,5\}} c_n O_n. \quad \text{EFT}$$

CMS SMEFT NLO 13 TeV jets &  $t\bar{t}$  + HERA

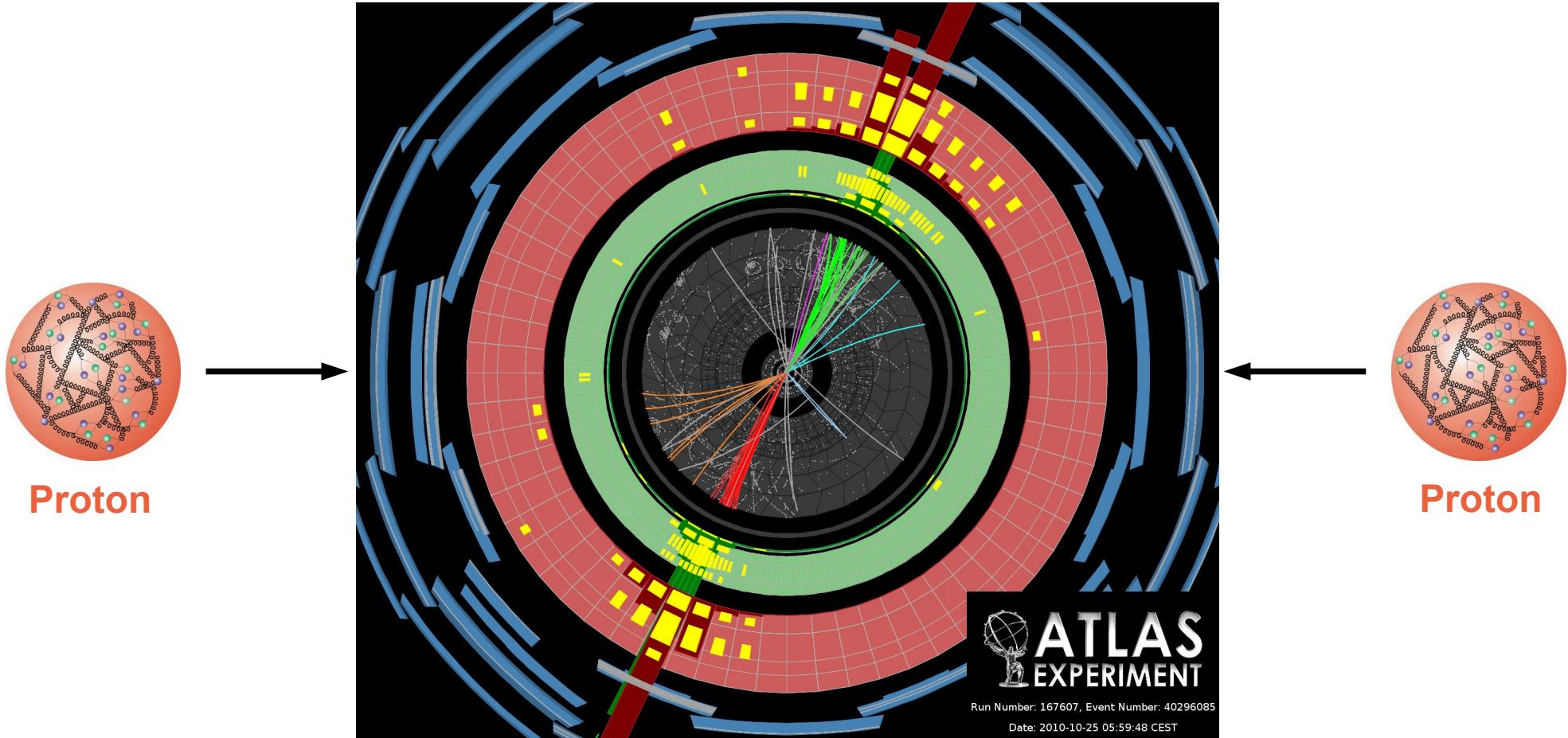




# Dijets

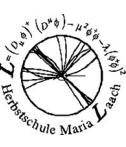


## Large masses





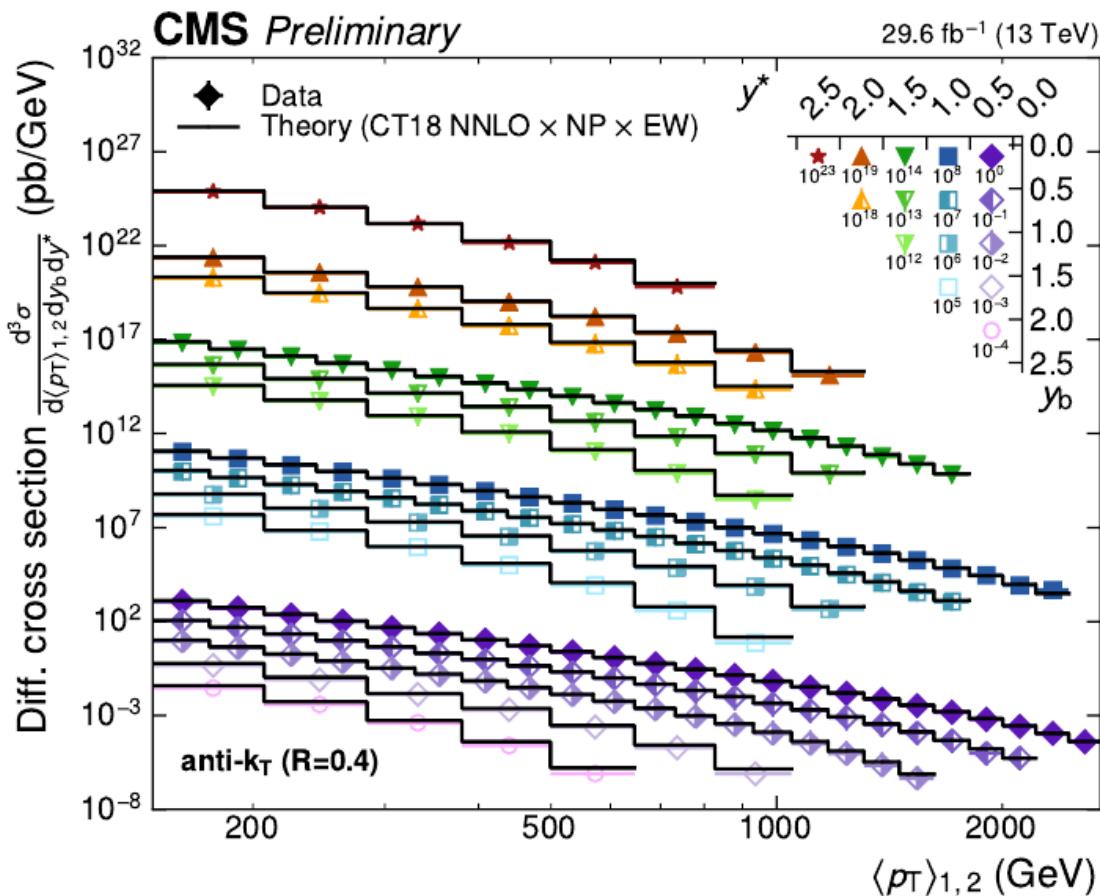
# Double/triple-differential dijets



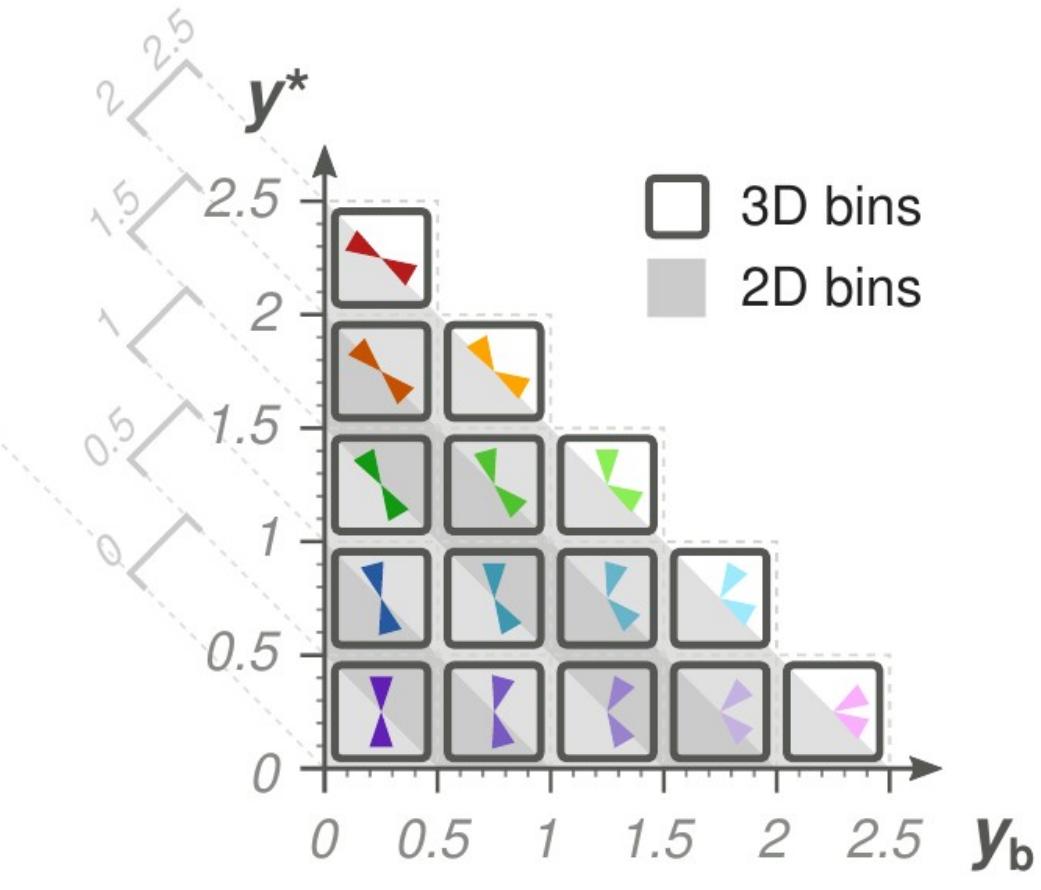
$$\frac{d^2\sigma}{dy_{\max} dm_{1,2}} = \frac{1}{\varepsilon \mathcal{L}_{\text{int}}} \frac{N}{(2 \Delta |y|_{\max}) \Delta m_{1,2}}.$$

$$\frac{d^3\sigma}{dy^* dy_b dx} = \frac{1}{\varepsilon \mathcal{L}_{\text{int}}} \frac{N}{\Delta y^* \Delta y_b \Delta x}.$$

## Comparison to NNLO



## Illustration of dijet event topologies



CMS, PAS-SMP-21-008 (2022).



# Double/Triple-differential dijets

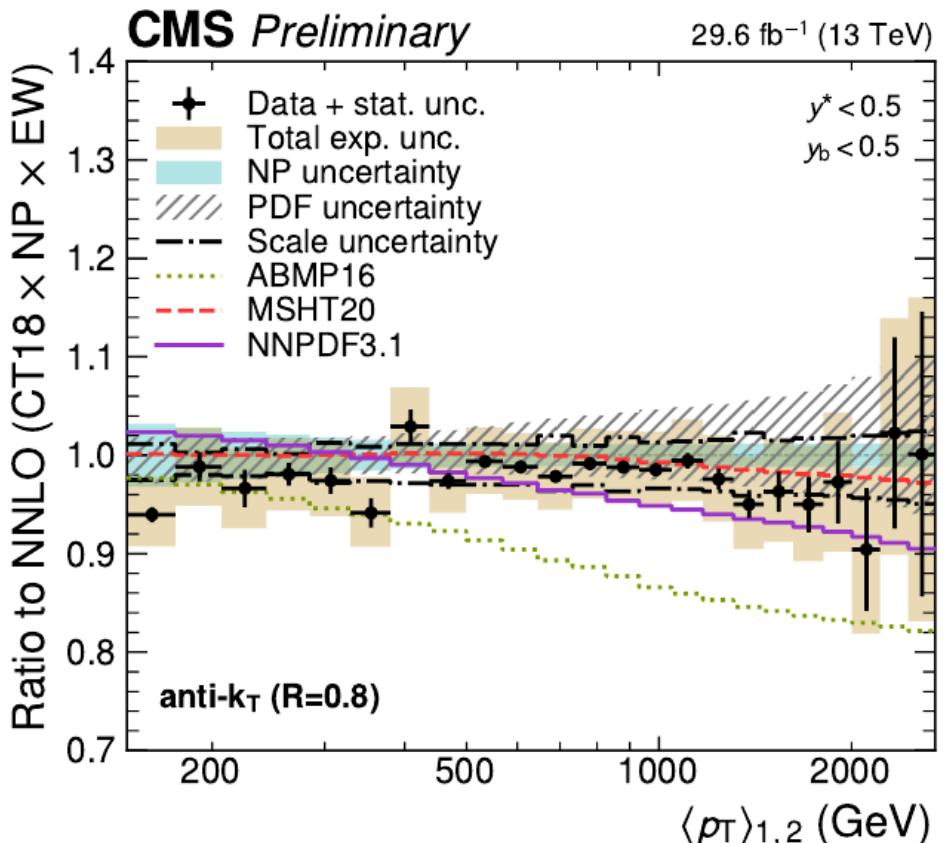
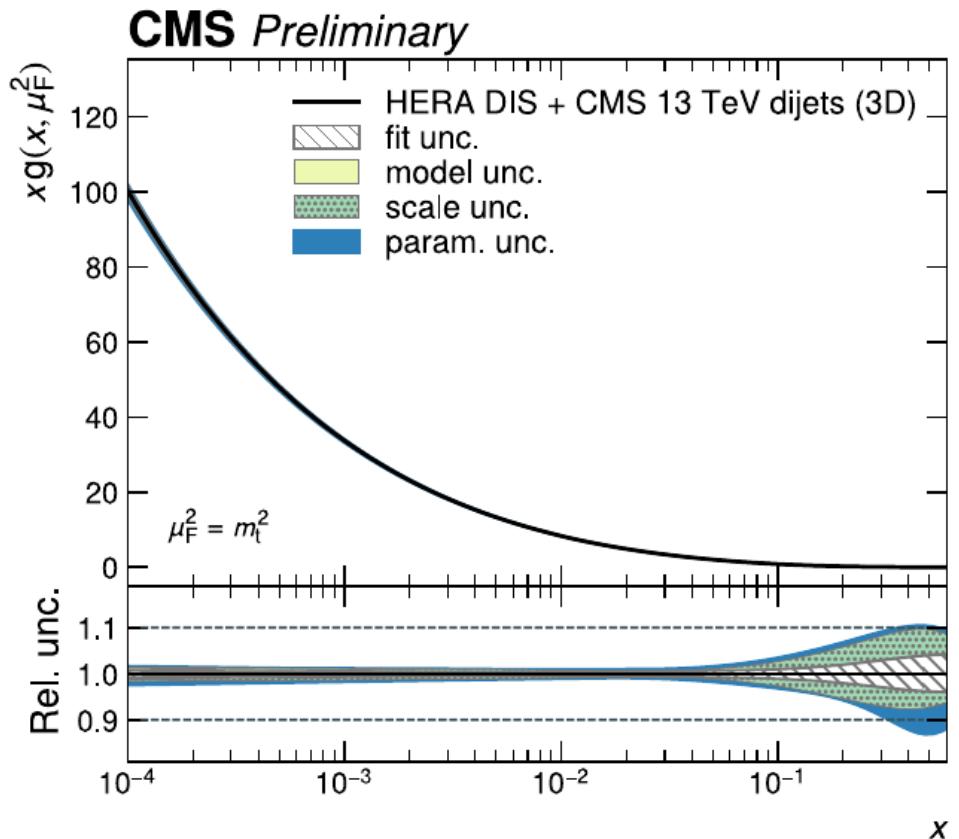


Simultaneous fit of  $\alpha_s$  & PDFs combining  
HERA DIS & CMS djet data using xFitter Tool

Data over NNLO pQCD x NP x EW corrections



Determine gluon PDF



Determine strong coupling

2D

$$\alpha_s(m_Z) = 0.1201 (12)_{\text{fit}} (8)_{\text{scale}} (8)_{\text{model}} (5)_{\text{param}}$$

3D

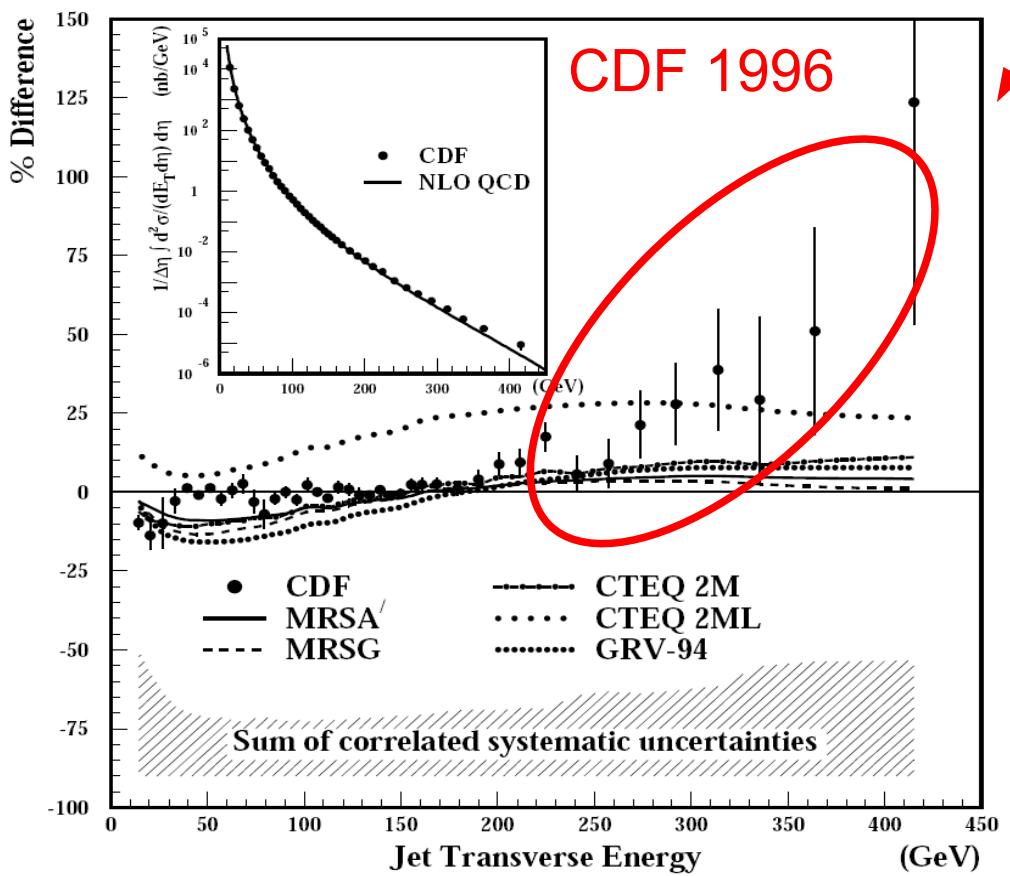
$$\alpha_s(m_Z) = 0.1201 (10)_{\text{fit}} (5)_{\text{scale}} (8)_{\text{model}} (6)_{\text{param}}$$

# New physics ?

"The data are compared with QCD predictions for various sets of parton distribution functions.

The cross section for jets with  $E_T > 200$  GeV is significantly higher than current predictions based on  $O(\alpha_s^3)$  perturbative QCD calculations. ..."

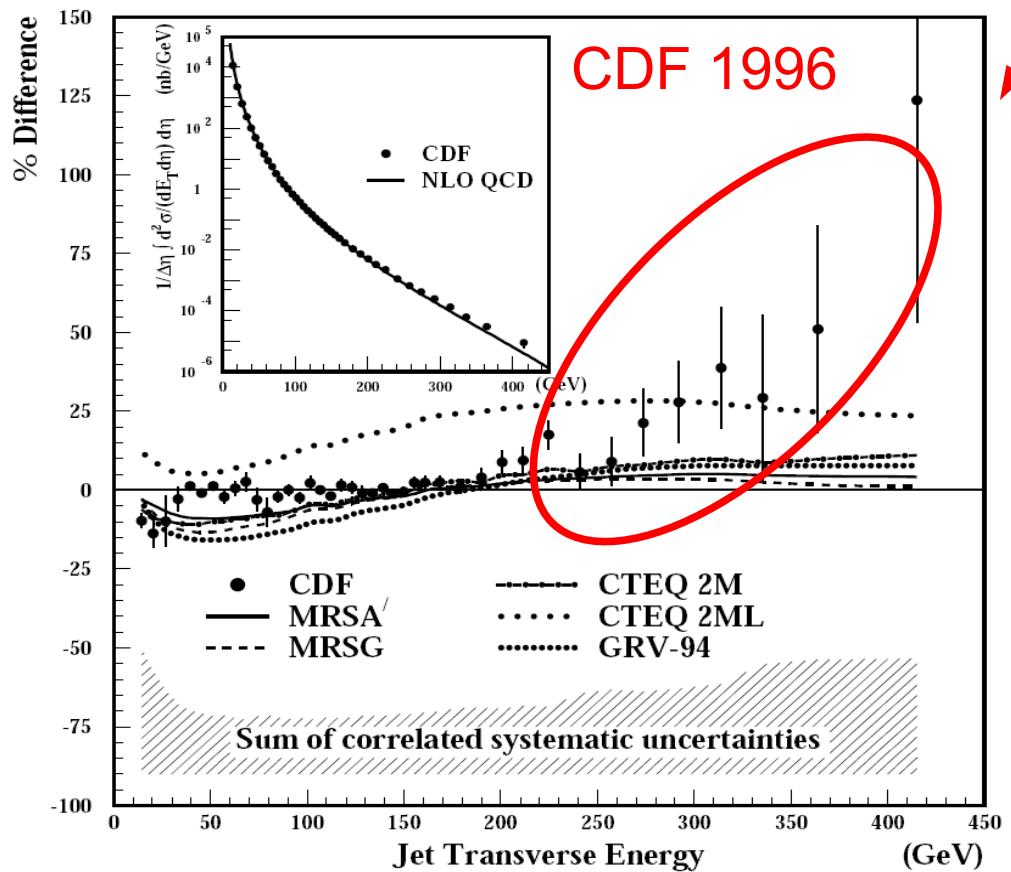
Explained by better adaptation of gluon density in proton!  $\rightarrow g(x, Q^2)$



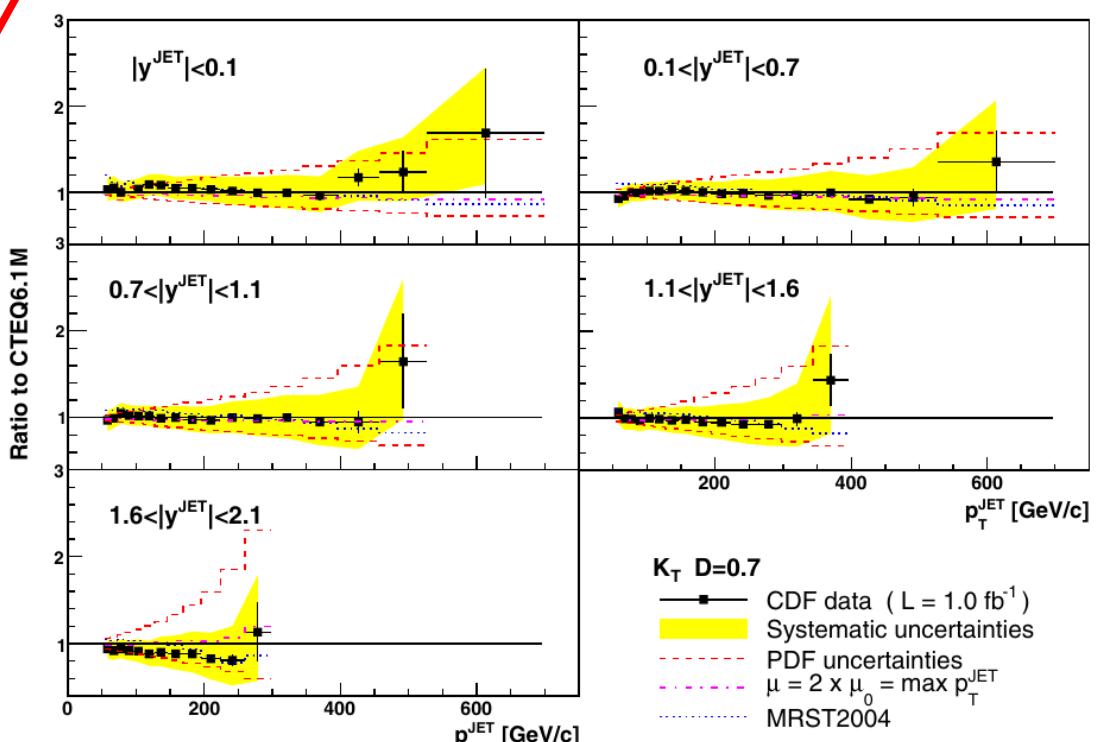
CDF Run 1: Phys.Rev.Lett. 77 (1996)

# New physics ? Not yet.

"The data are compared with QCD predictions for various sets of parton distribution functions. The cross section for jets with  $E_T > 200$  GeV is significantly higher than current predictions based on  $O(\alpha_s^3)$  perturbative QCD calculations. ..."

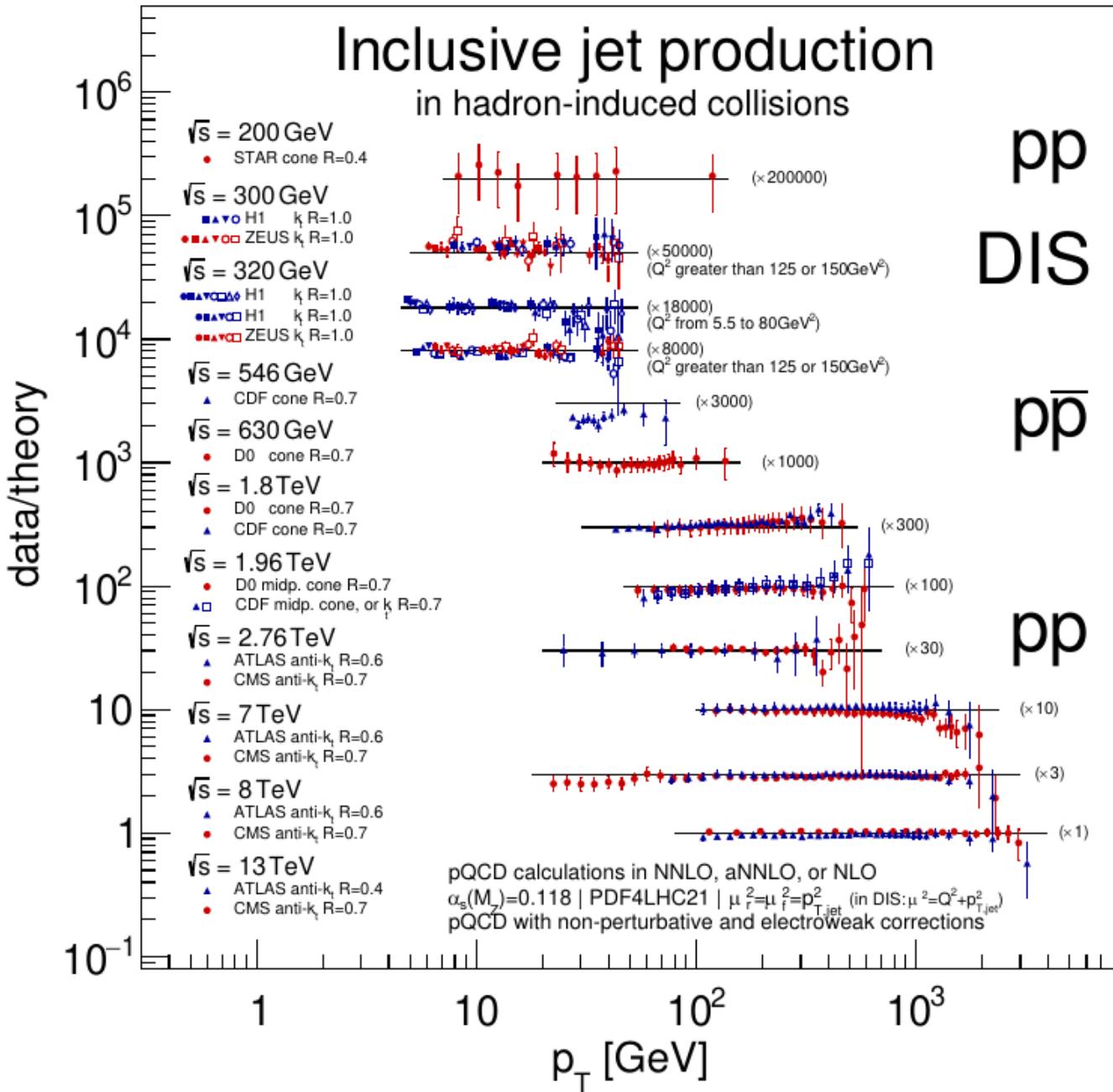


**Explained by better adaptation of gluon density in proton!  $\rightarrow g(x, Q^2)$**   
**Today:**  
**Significantly improved determination of uncertainties**





# No sign of new physics so far



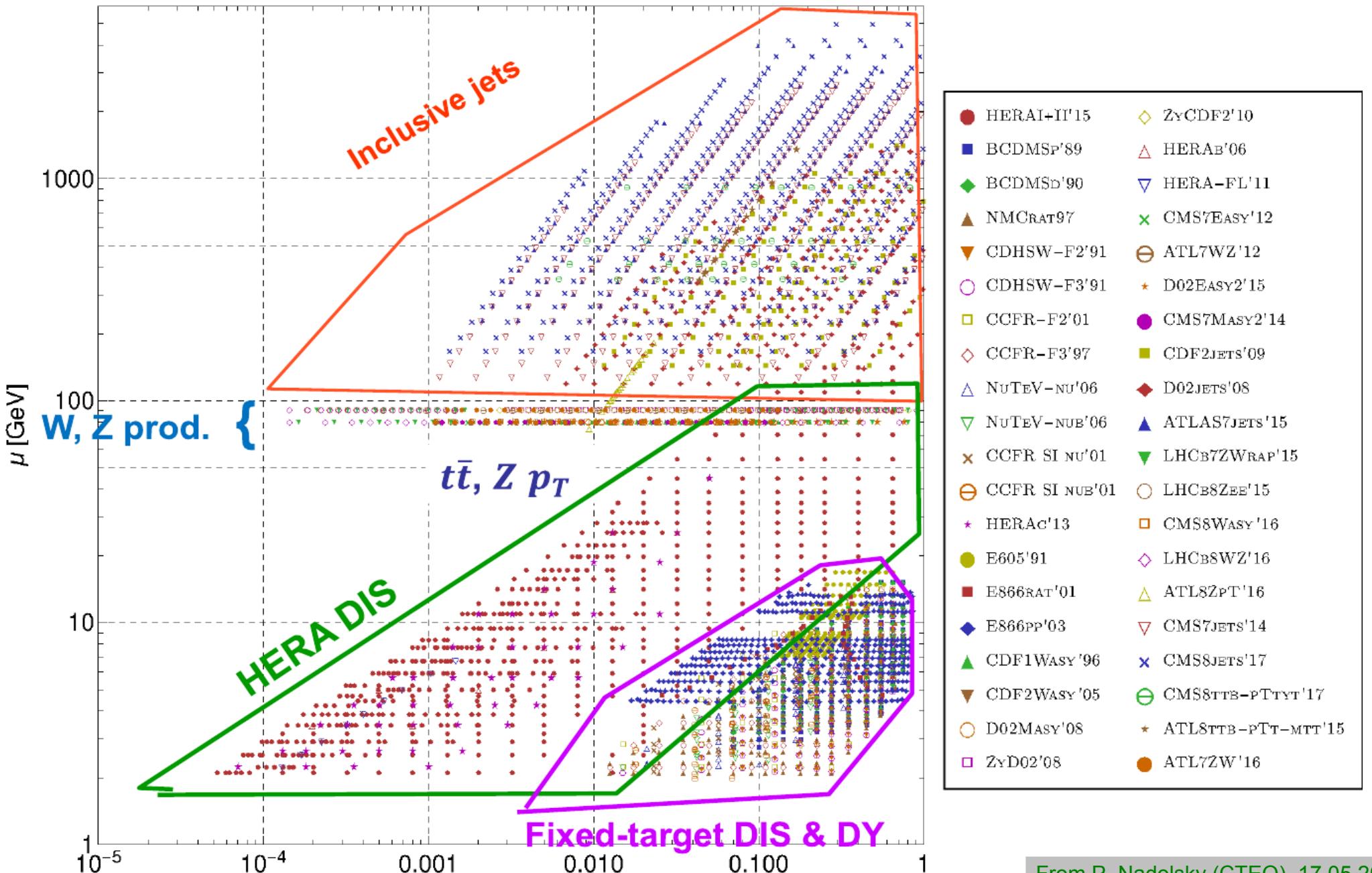
Ratio of data over theory  
for a large number of  
inclusive jet datasets

pp  
DIS  
pp  
pp

50 years of QCD, arXiv:2212.11107.



# Experimental data in CT18 PDFs

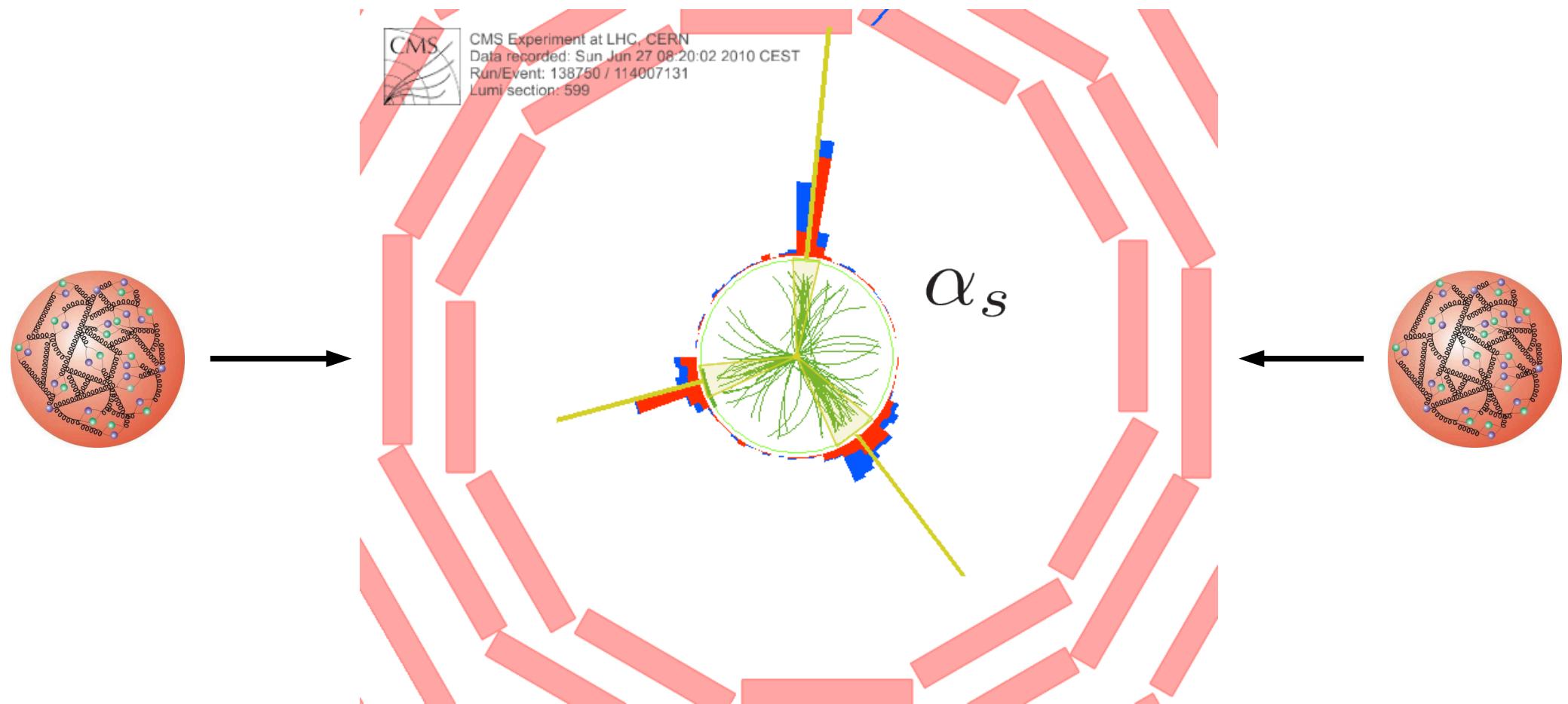


From P. Nadolsky (CTEQ), 17.05.2020.



# Multi-jets

## Higher multiplicity





# Jet cross section ratios



- Determination of  $\alpha_s(M_Z)$  in single-parameter fit
- Test running of  $\alpha_s(Q)$  (reduced PDF dependence)
- Some reduction in sensitivity
- But cancellation of many systematic effects
- More scale choices



# Jet-radius ratios



- Examine radius dependence of jet cross section:
  - ✚ “LO” – two partons in opposite directions
  - ✚ → Always two jets, independently of algorithm → ratio trivially unity
  - ✚ First non-trivial order needs THREE partons
  - ✚ → 3-jet observable, LO corresponds to NLO dijet production → NLOJet++
- Definition: 
$$\left( \frac{d\sigma^{\text{alt}}}{dp_T} - \frac{d\sigma^{\text{ref}}}{dp_T} \right) \Big/ \left( \frac{d\sigma^{\text{ref}}}{dp_T} \right) = \mathcal{R}(\text{alt}, \text{ref}) - 1$$

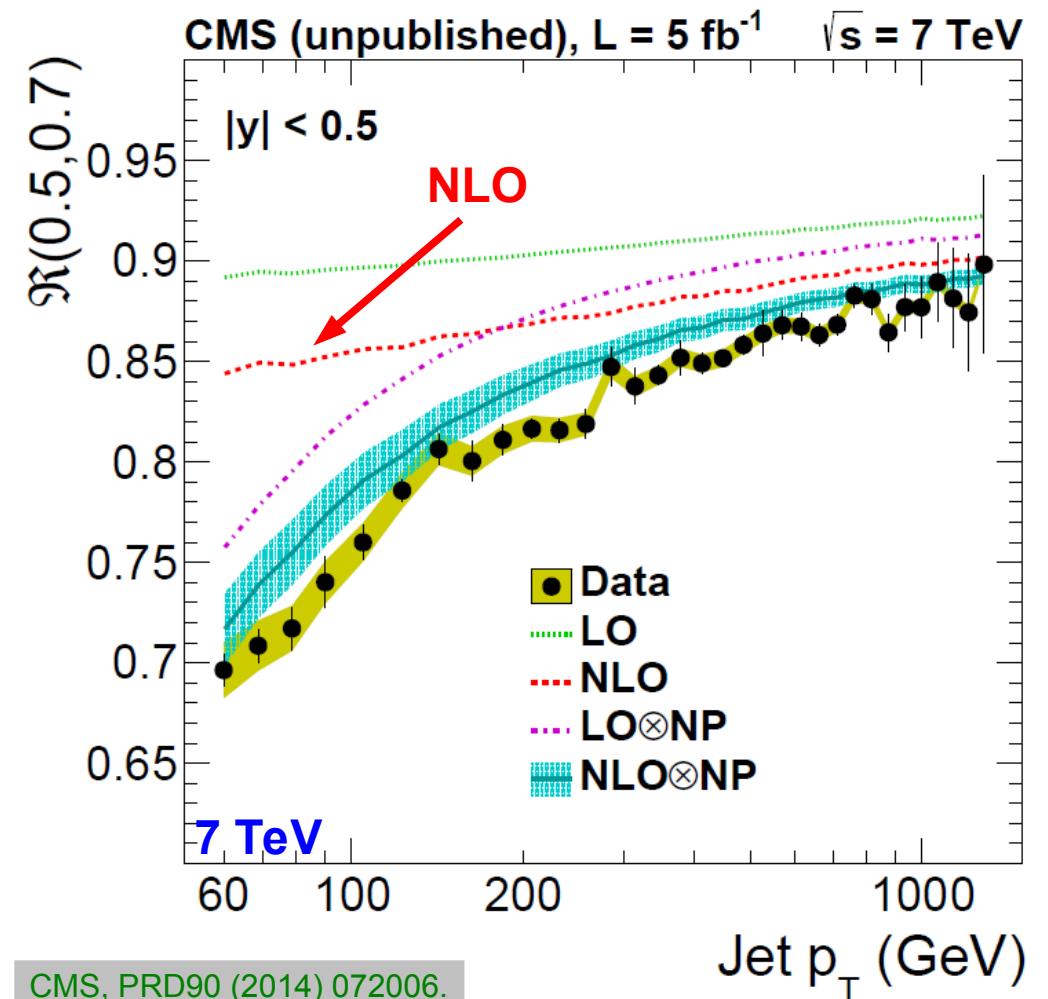
3-Jet NLO	2-Jet NLO
-----------	-----------
- “alt” and “ref” could be two different jet algorithms
  - ✚ ZEUS e.g. investigated kT, anti-kT and SISCone
  - ✚ ALICE + CMS: Two different jet radii for anti-kT

ZEUS, PLB691 (2010) 127.

# Jet radius ratios

Cross-section ratio for  $R = 0.5/0.7$

Emphasizes effect of parton shower  
and hadronisation  
→ NLO 3-jet not sufficient!



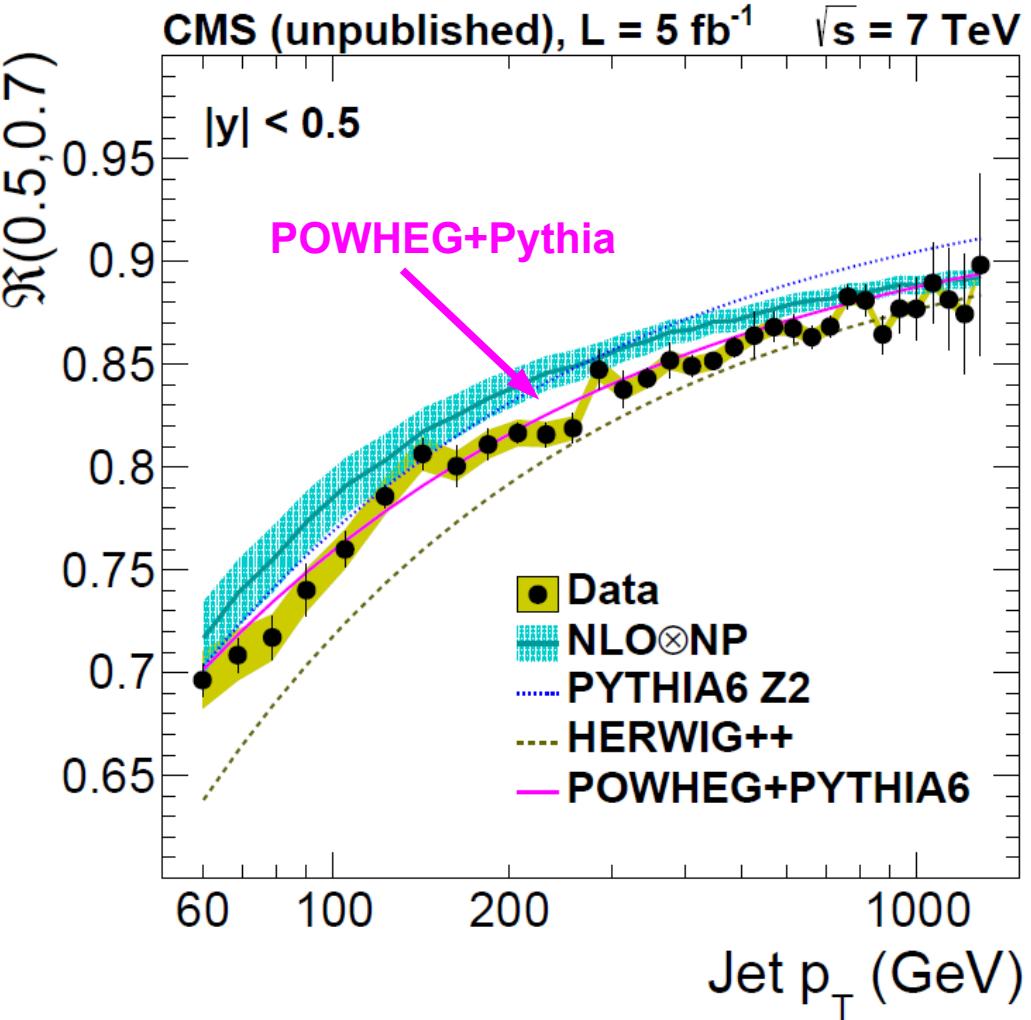
Needs event generators:

LO+PS+HAD → better  
(Pythia6, Herwig++)  
NLO+PS+HAD → best  
(POWHEG+Pythia)

G. Soyez,  
PLB698 (2011).

ALICE study  
 $R=0.2 / R=0.4$

ALICE, PLB722 (2013).





# Dijet azimuthal decorrelation

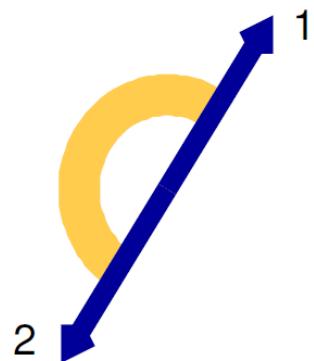


Determine  $\alpha_s(Q)$  from additional parton branchings separated in  $\Phi$  around the two leading jets.  
Binning in sum of scalar transverse momentum  $H_T$  and rapidity separation  $y^*$ .

$$R_{\Delta\phi}(H_T, y^*; \Delta\phi_{\max}) = \frac{\frac{d^2\sigma_{\text{dijet}}(\Delta\phi_{\text{dijet}} < \Delta\phi_{\max})}{dH_T dy^*}}{\frac{d^2\sigma_{\text{dijet}}(\text{inclusive})}{dH_T dy^*}}$$

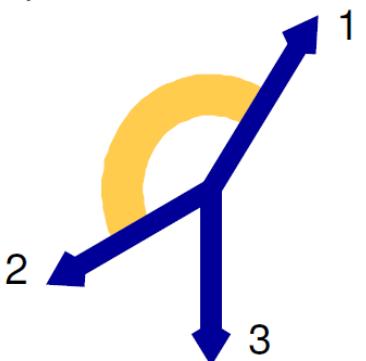
$$R_{\Delta\phi} \propto \alpha_s$$

a)  $2 \rightarrow 2$



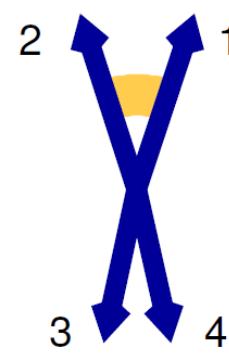
$$\Delta\phi_{\text{dijet}} = \pi$$

b)  $2 \rightarrow 3$



$$2\pi/3 \leq \Delta\phi_{\text{dijet}} \leq \pi$$

c)  $2 \rightarrow 4$

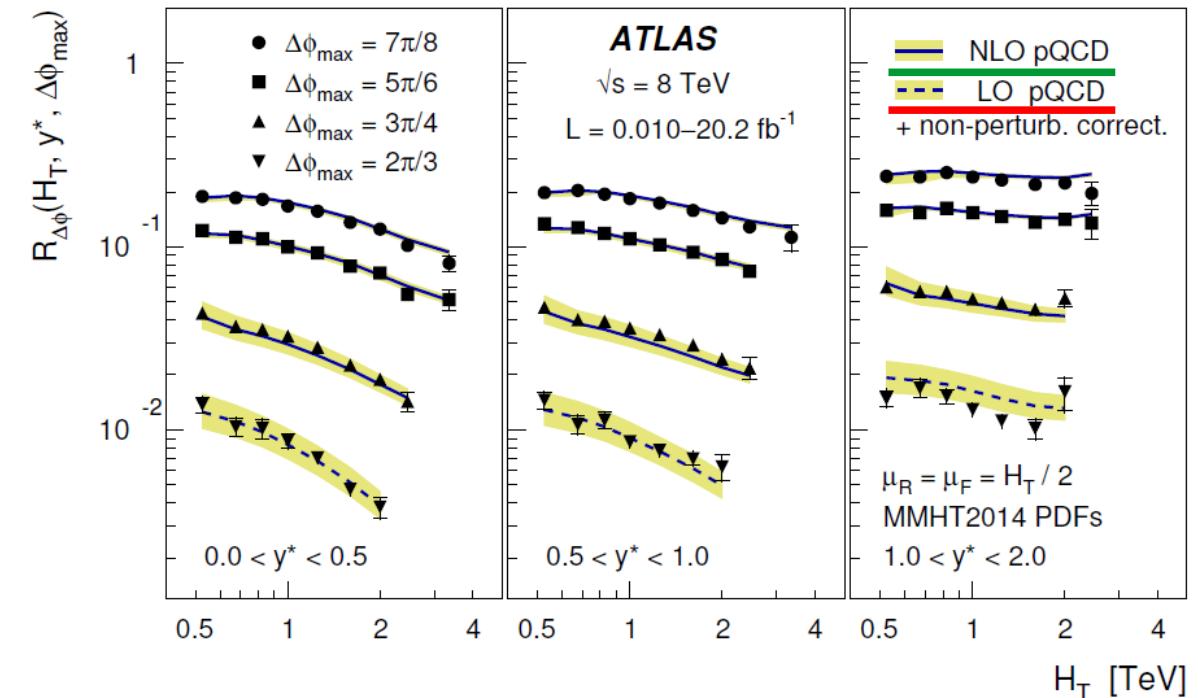


$$0 \leq \Delta\phi_{\text{dijet}} \leq \pi$$

If  $\Delta\phi_{\max}$  in 3-jet region

Wobisch et al., JHEP 01 (2013) 172;  
KR, M. Wobisch, JHEP 12 (2015) 024.

# $R_{\Delta\phi}$ in bins of $Q = H_T/2$

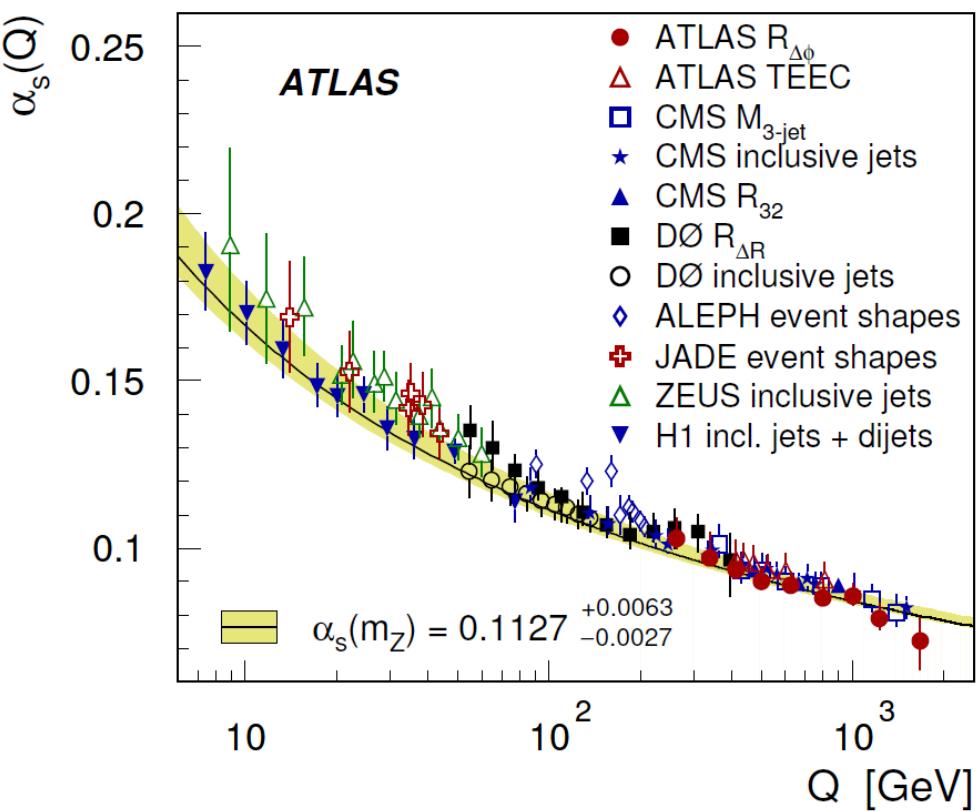


From more precise results with  
 $\Delta\phi_{\max} = 7\pi/8$  in the two  $y^*$  regions below 1.0:

$$\alpha_S(m_Z) = 0.1127^{+0.0063}_{-0.0027}$$

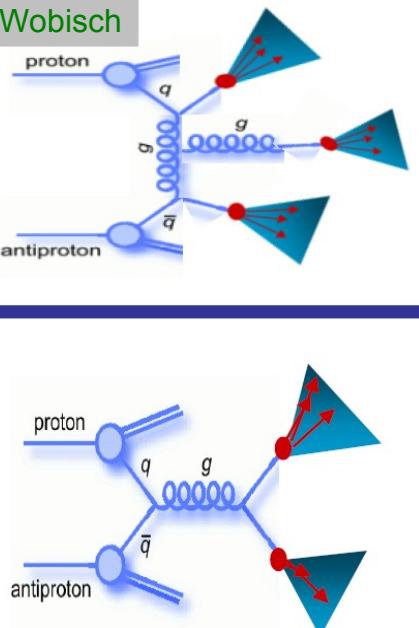
Theory:  
3-jet NLOJet++

Scale choice:  $\mu_R = \mu_F = H_T/2$



# 3- to 2-jet ratios

M. Wobisch



$R_{3/2}$

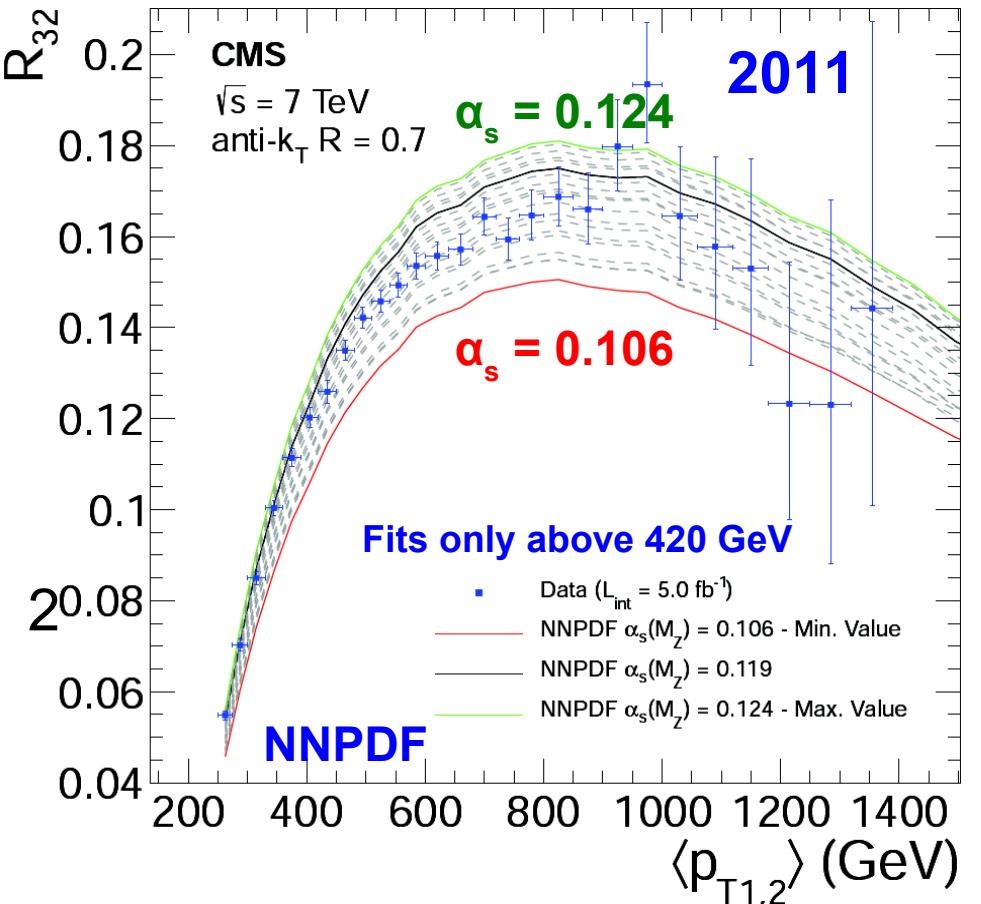
$\alpha_s$

$$\frac{\sigma_{3+\text{jet}}}{\sigma_{2+\text{jet}}} \propto \alpha_s^1$$

$$Q = \langle p_{T1,2} \rangle$$

CMS:  $R_{3/2}$

- Ratio of inclusive 3- to inclusive 2-jet events
- anti- $k_T$  R=0.7
- Min. jet pT: 150 GeV
- Max. rap.:  $|y| < 2.5$
- Data 2011 7 TeV, and 2012 8 TeV prel.



$$\alpha_s(M_Z) = 0.1148 \pm 0.0014 \text{ (exp.)} \pm 0.0018 \text{ (PDF)} \\ \pm 0.0050 \text{ (theory),}$$

**BUT do we gain from taking ratios?**

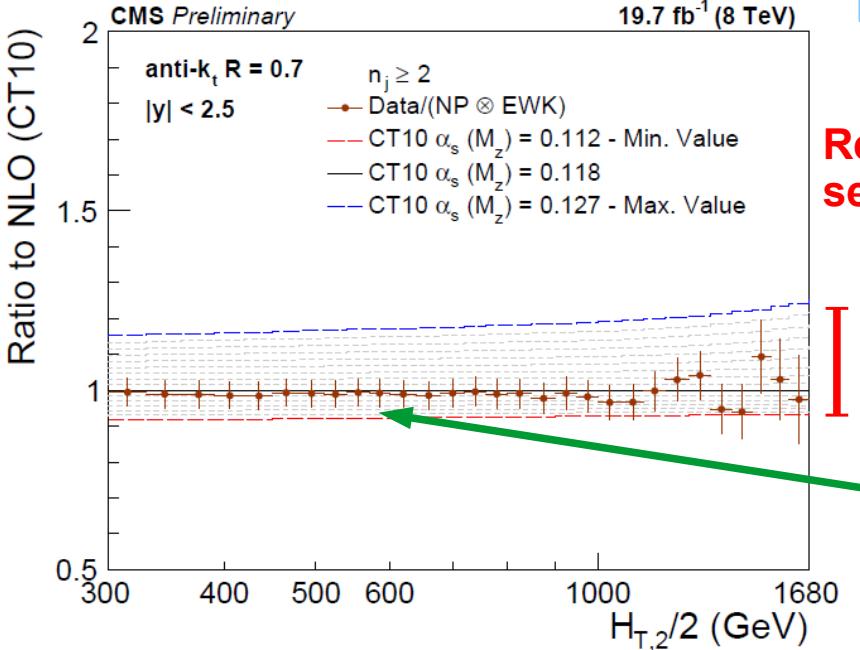
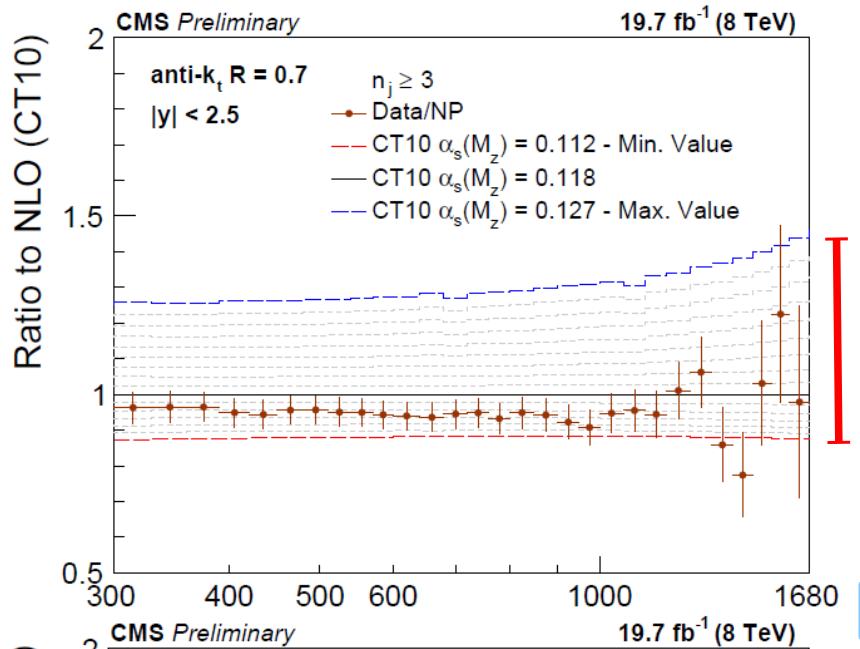


# Sensitivity vs. systematic effects



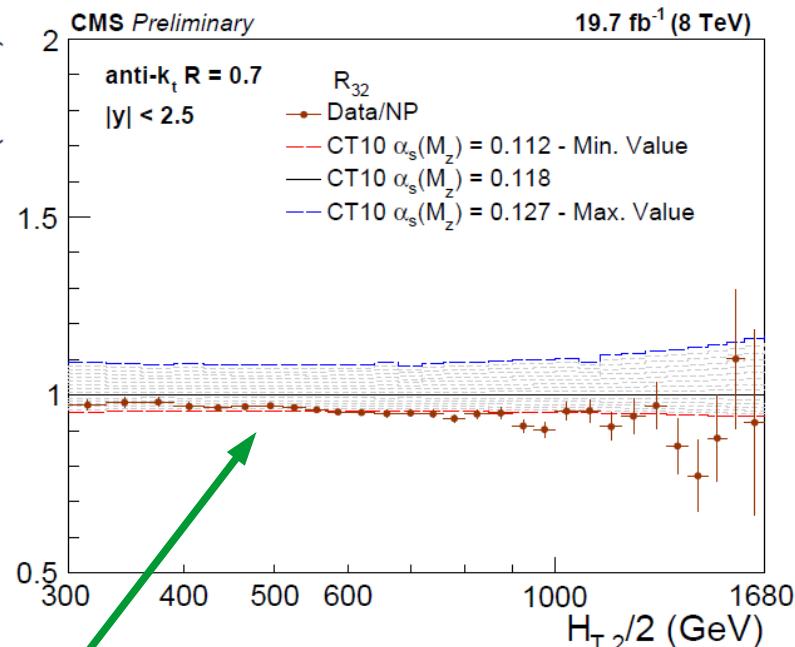
Inclusive 3-jet cross section

$$\sigma_{3j} \propto \alpha_s^3$$



Inclusive 3-jet to inclusive 2-jet cross section ratio

$$R_{3/2} \propto \alpha_s$$



Reduced sensitivity

Much reduced systematic uncertainty

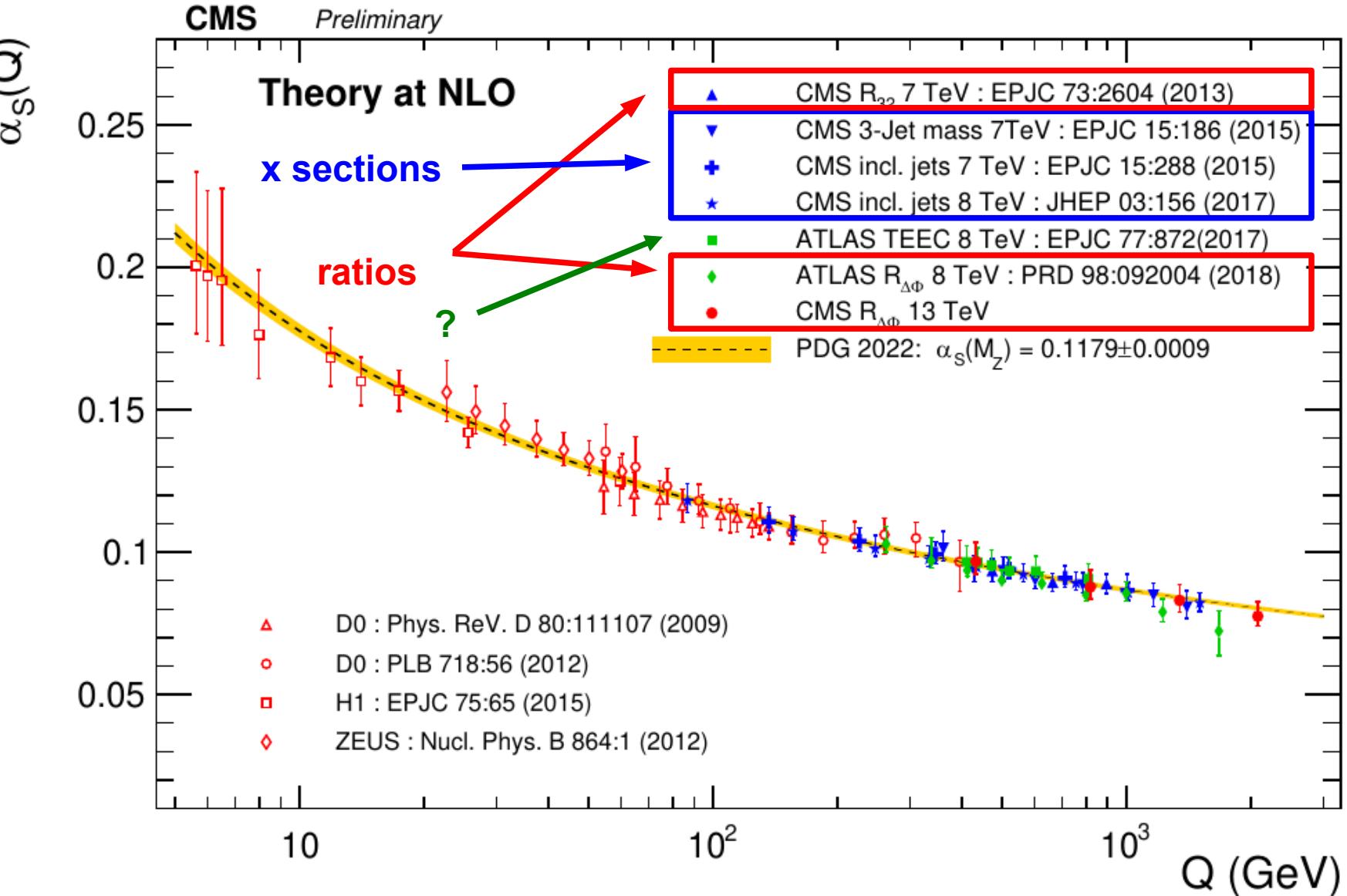


# Running of $\alpha_s(Q)$ (CMS style)



Perform fits in fixed intervals of the chosen scale Q

$\alpha_s(Q)$



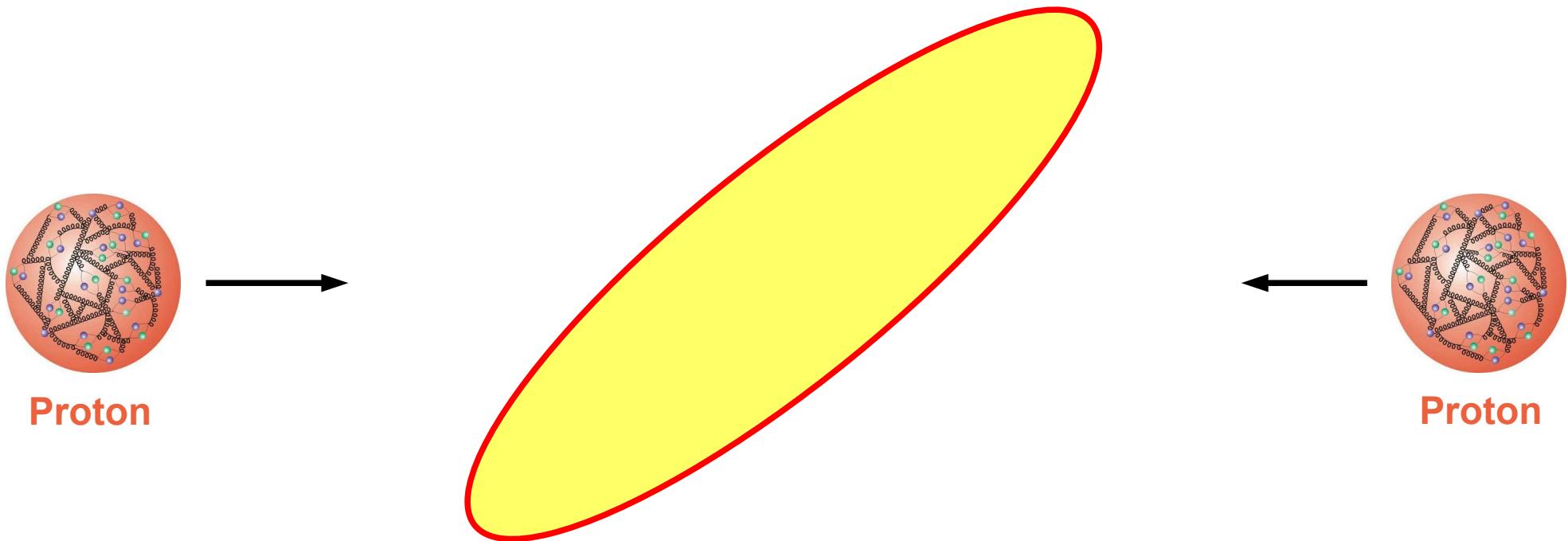
New range explored at LHC



# Normalised distributions



## Event shapes





# Normalised distributions



Pros & cons similar as for cross section ratios ...

- Determination of  $\alpha_s(M_Z)$  in single-parameter fit
- Test running of  $\alpha_s(Q)$  (reduced PDF dependence)
- Some reduction in sensitivity
- But cancellation of many systematic effects
- More scale choices



# Transverse energy-energy correlation

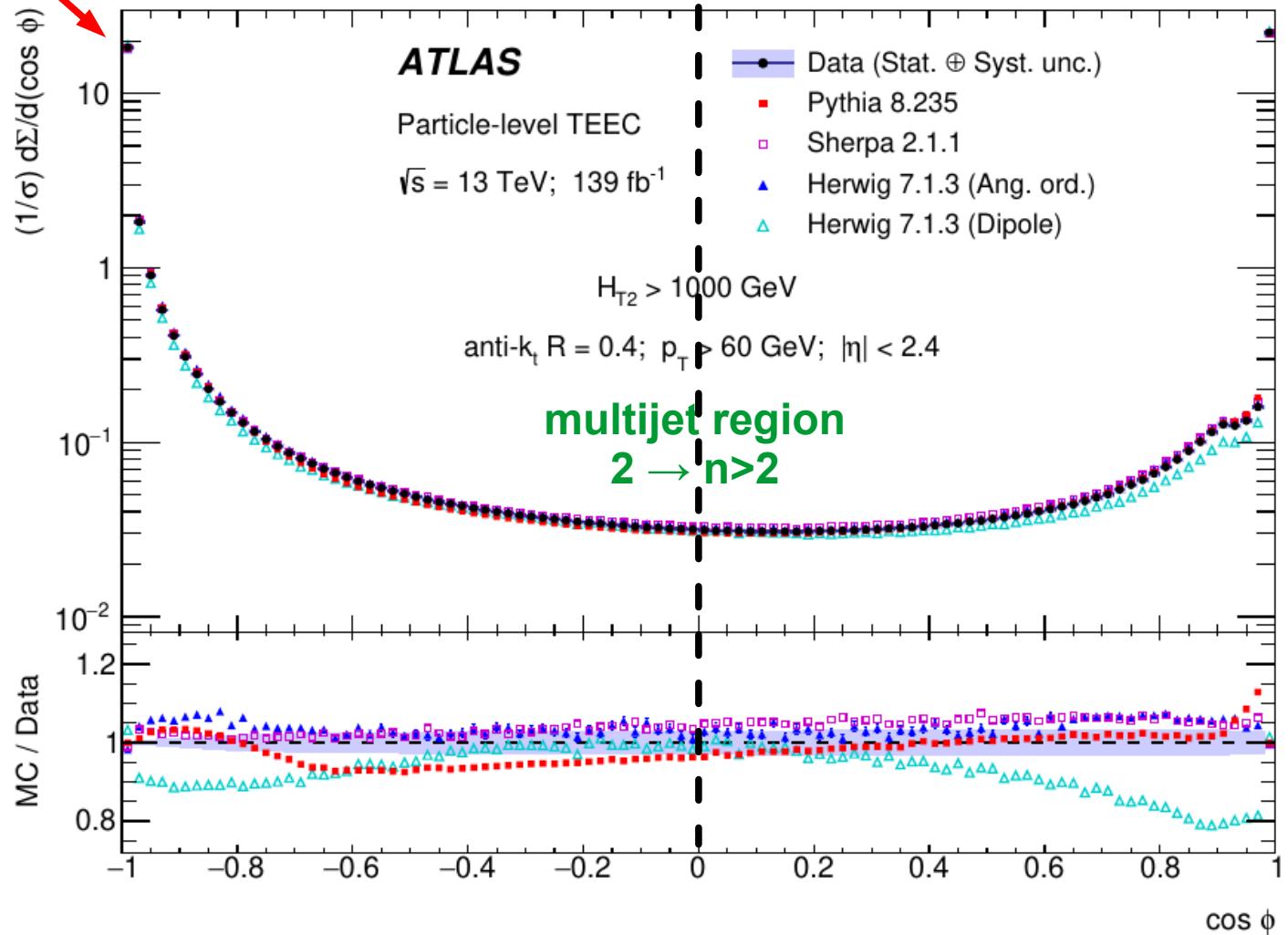


$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} = \frac{1}{N} \sum_{A=1}^N \sum_{ij} \frac{E_{Ti}^A E_{Tj}^A}{(\sum_k E_{Tk}^A)^2} \delta(\cos \phi - \cos \phi_{ij})$$

$$\text{TEEC} \propto \alpha_s$$

**2 → 2 back-to-back jets      autocorrelation i=j 2 → 2**

Normalised  
Multiple  
bins in  $H_T$



ATLAS, JHEP 07 (2023) 085.



# Transverse energy-energy correlation

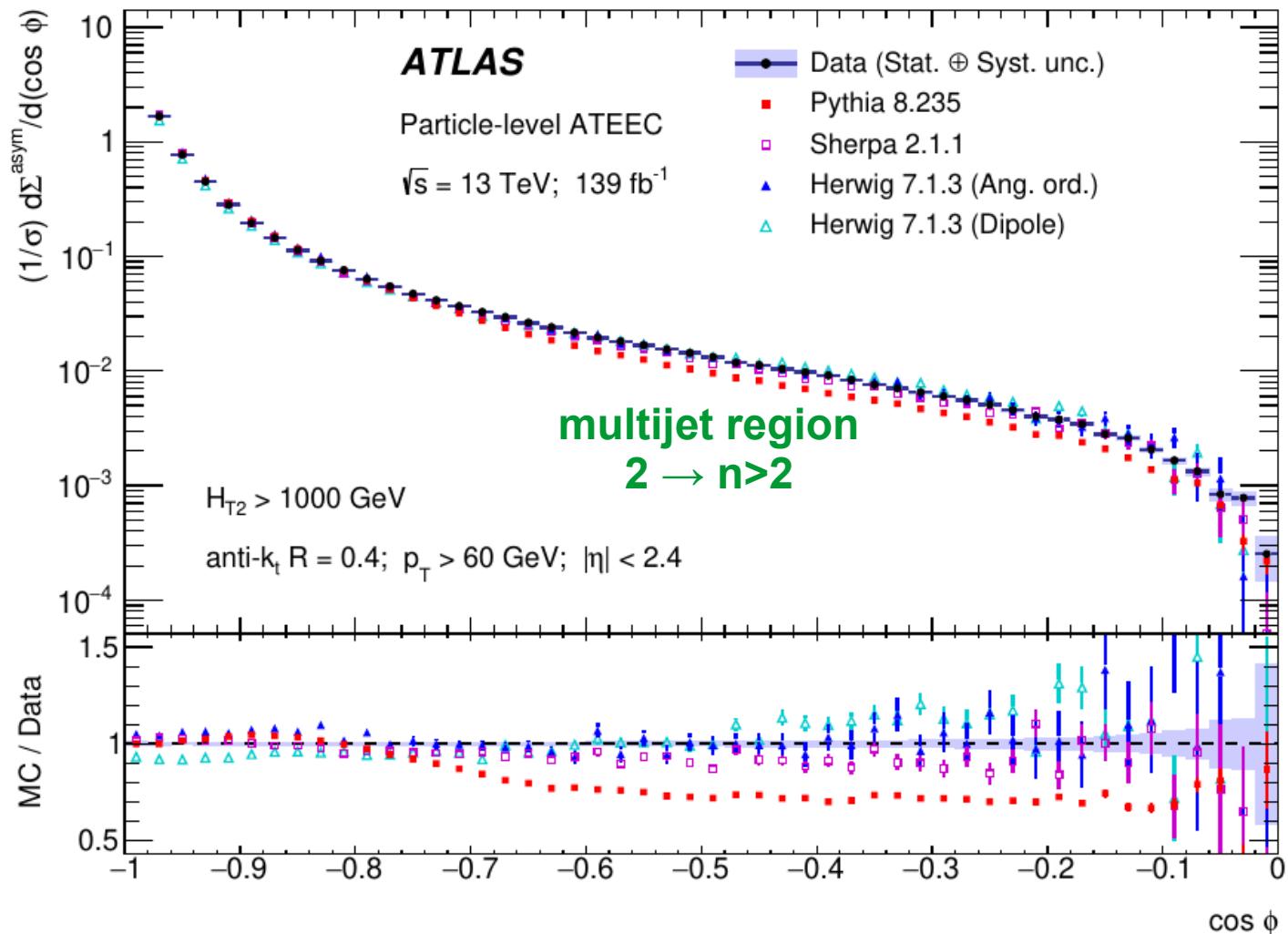


$$\frac{1}{\sigma} \frac{d\Sigma^{\text{asym}}}{d \cos \phi} = \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \left|_{\phi} - \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \right|_{\pi-\phi}$$

Asymmetry

ATEEC  $\propto \alpha_s$

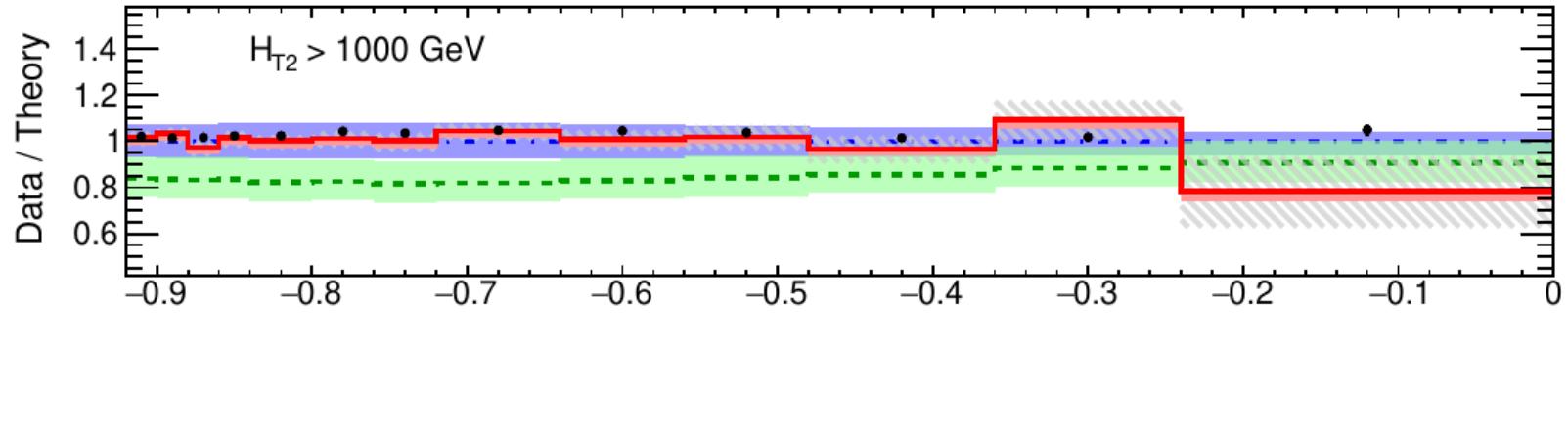
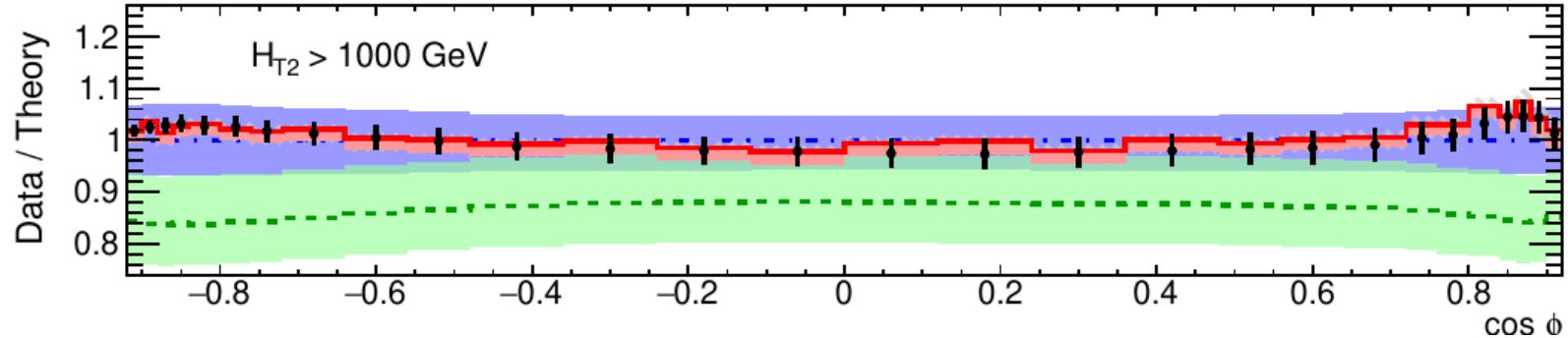
Normalised



ATLAS, JHEP 07 (2023) 085.



# Ratios to NLO



$$\alpha_s(m_Z) = 0.1175 \pm 0.0006 \text{ (exp.)}^{+0.0034}_{-0.0017} \text{ (theo.) and}$$

$$\alpha_s(m_Z) = 0.1185 \pm 0.0009 \text{ (exp.)}^{+0.0025}_{-0.0012} \text{ (theo.).}$$

3-jet NNLO:  
Czakon, Mitov, Poncelet, PRL 127 (2021) 152001.

$$\mu_{R,F} = \hat{\alpha}_T$$

$$\alpha_s(m_Z) = 0.1180$$

MMHT 2014 (NNLO)

— Data

— LO

— NLO

— NNLO



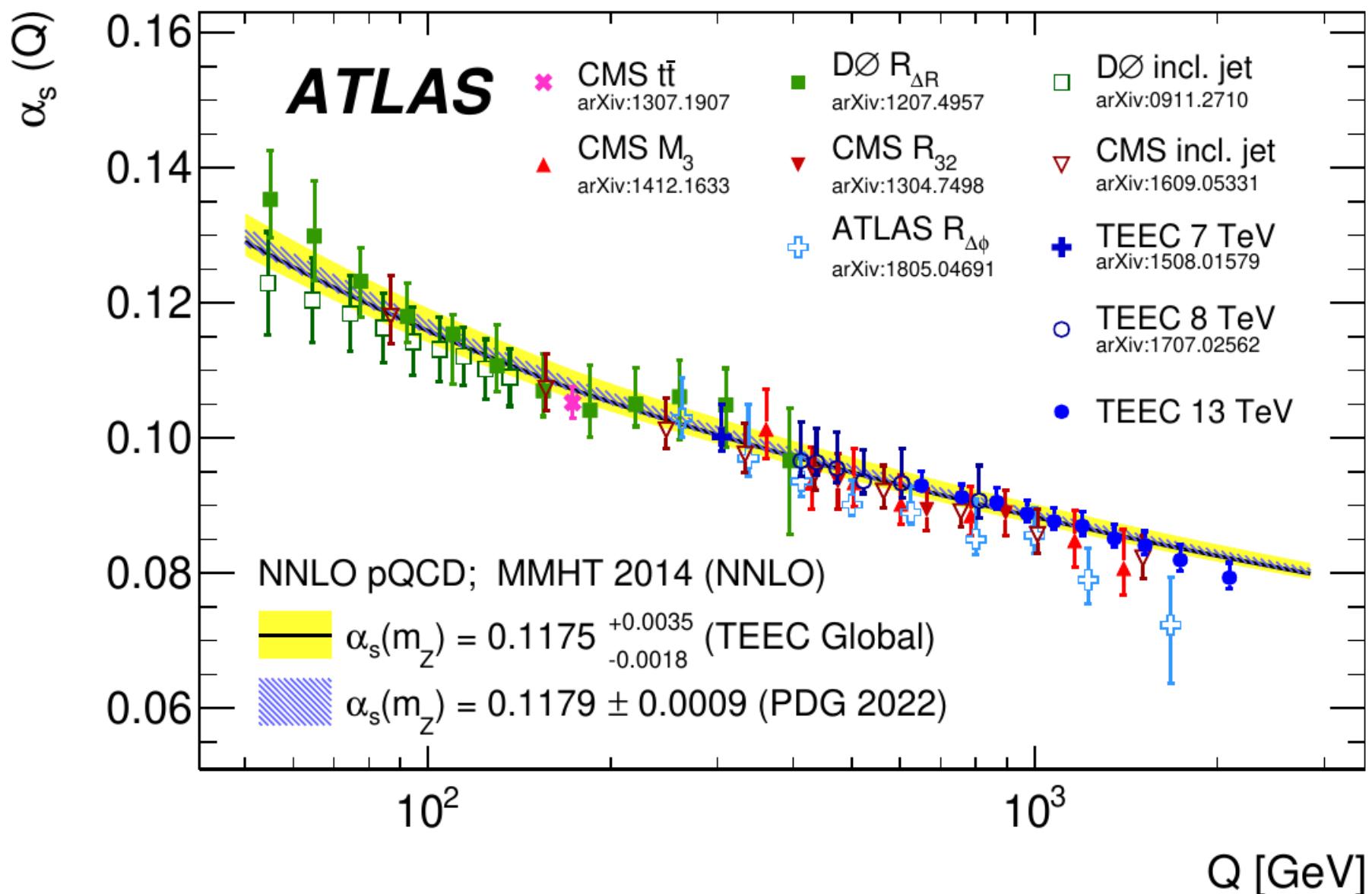
# Running of $\alpha_s(Q)$ (ATLAS style)



Theory:  
3-jet NNLO

Scale choice:

Run2 13 TeV:  
 $\mu_R = \mu_F = H_T/2$



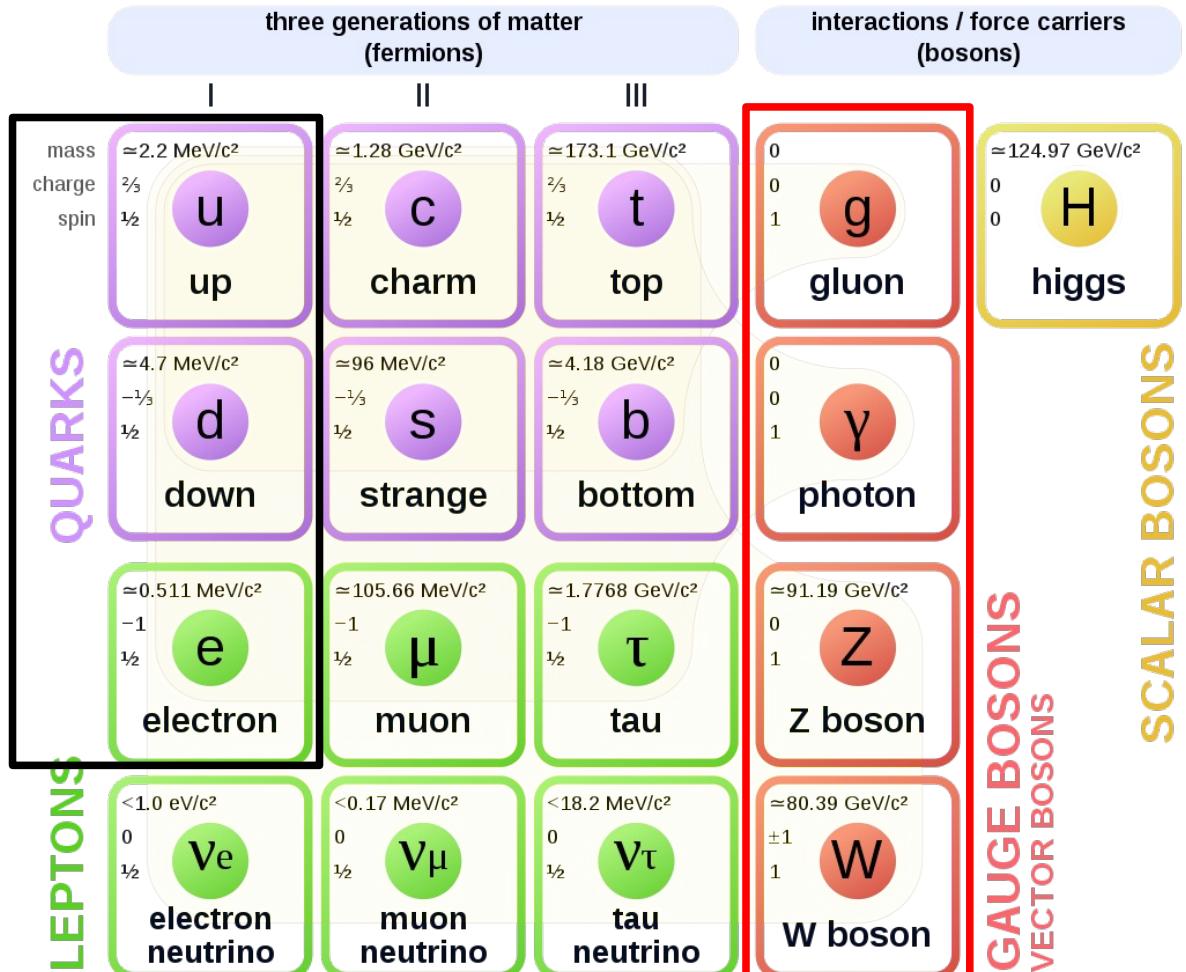


# Standard Model of Particle Physics



## Standard Model of Elementary Particles

Solid matter  
...



Cush, Wikipedia.

... and three fundamental interactions.  
(no gravity)

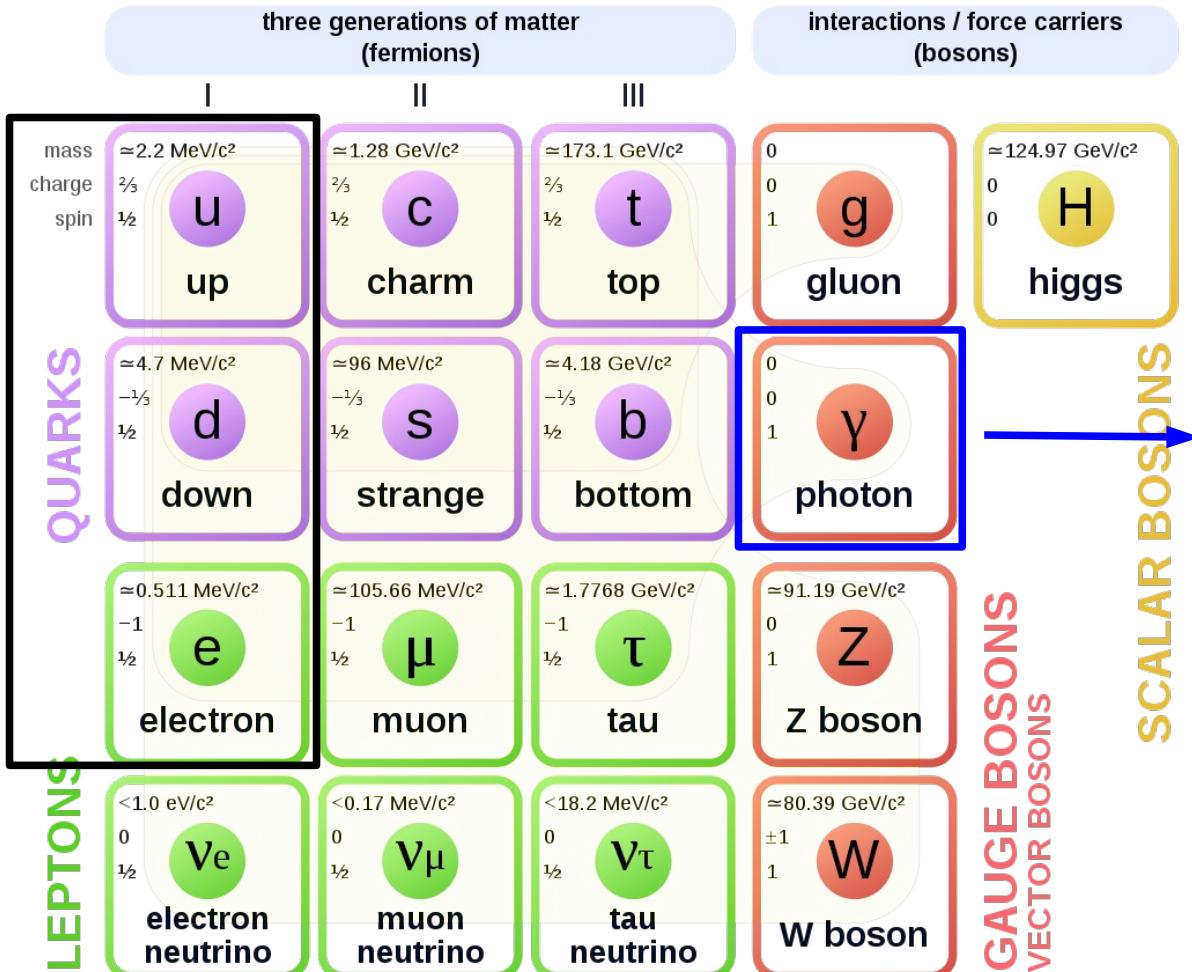


# Standard Model of Particle Physics



## Standard Model of Elementary Particles

Solid matter  
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Cush, Wikipedia.

... and three fundamental interactions.  
(no gravity)

Electromagnetic interaction  
(magnets, electricity, ...)

$$\alpha \approx 1/137$$

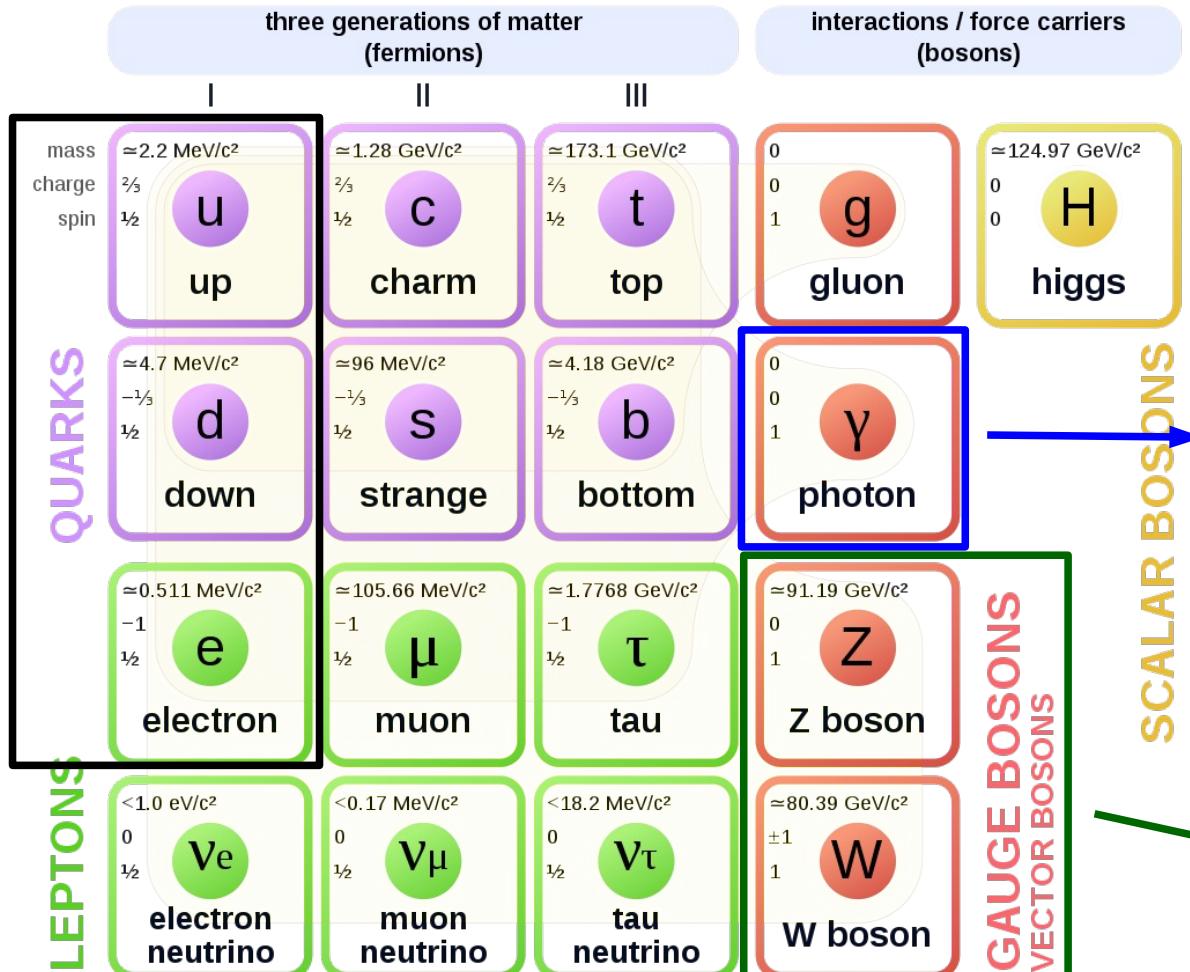
$$\Delta\alpha/\alpha = 0.15 \cdot 10^{-9}$$



# Standard Model of Particle Physics



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Electromagnetic interaction  
(magnets, electricity, ...)

$$\alpha \approx 1/137$$

$$\Delta\alpha/\alpha = 0.15 \cdot 10^{-9}$$

GAUGE BOSONS  
VECTOR BOSONS

Weak interaction  
( $\beta$  decays, sun, ...)

$$G_F \approx 1.17 \cdot 10^{-5} / \text{GeV}^2$$

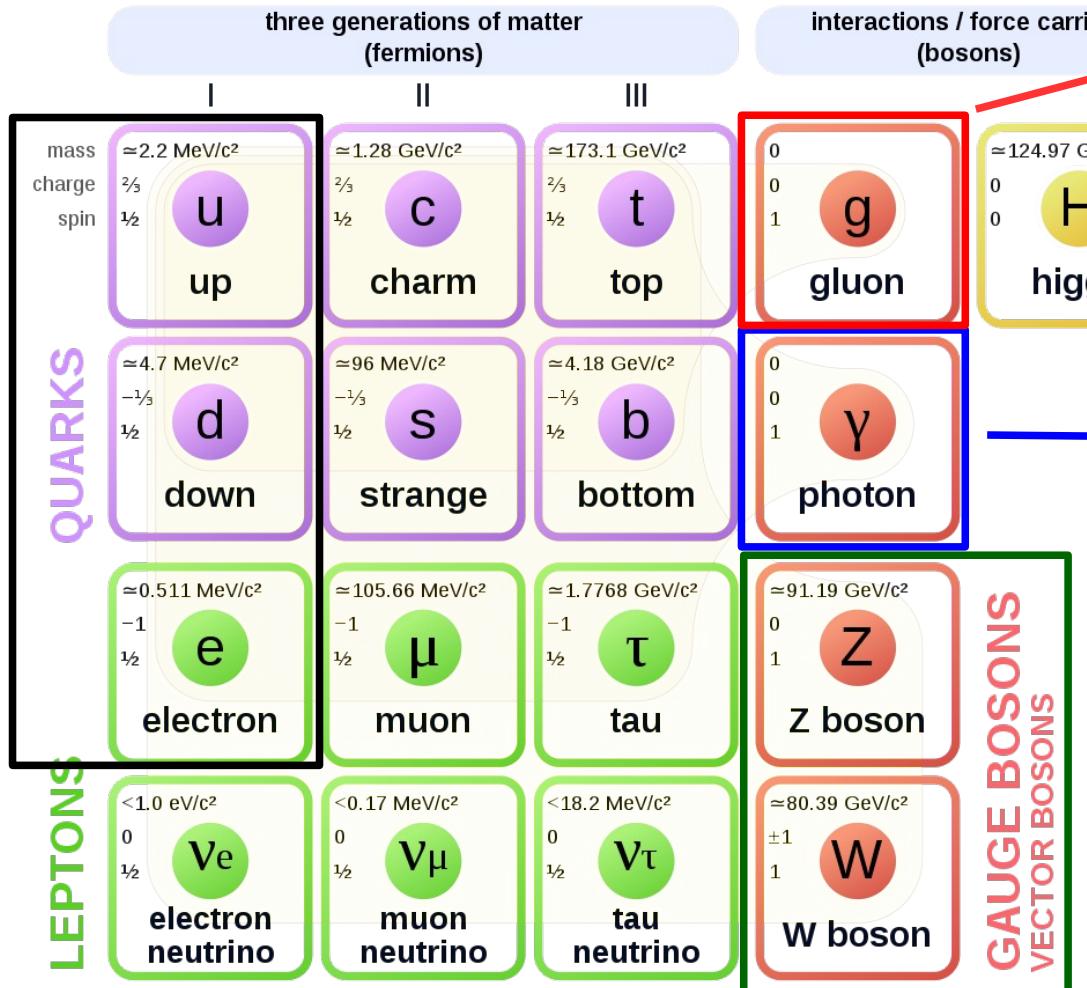
$$\Delta G_F/G_F = 0.51 \cdot 10^{-6}$$



# Standard Model of Particle Physics



## Standard Model of Elementary Particles



Cush, Wikipedia.

... and three fundamental interactions.  
(no gravity)

**Strong interaction (nuclear forces, ...)**

$$\alpha_s \approx 0.118$$

$$\Delta\alpha_s/\alpha_s = 8.5 \cdot 10^{-3}$$

**Electromagnetic interaction (magnets, electricity, ...)**

$$\alpha \approx 1/137$$

$$\Delta\alpha/\alpha = 0.15 \cdot 10^{-9}$$

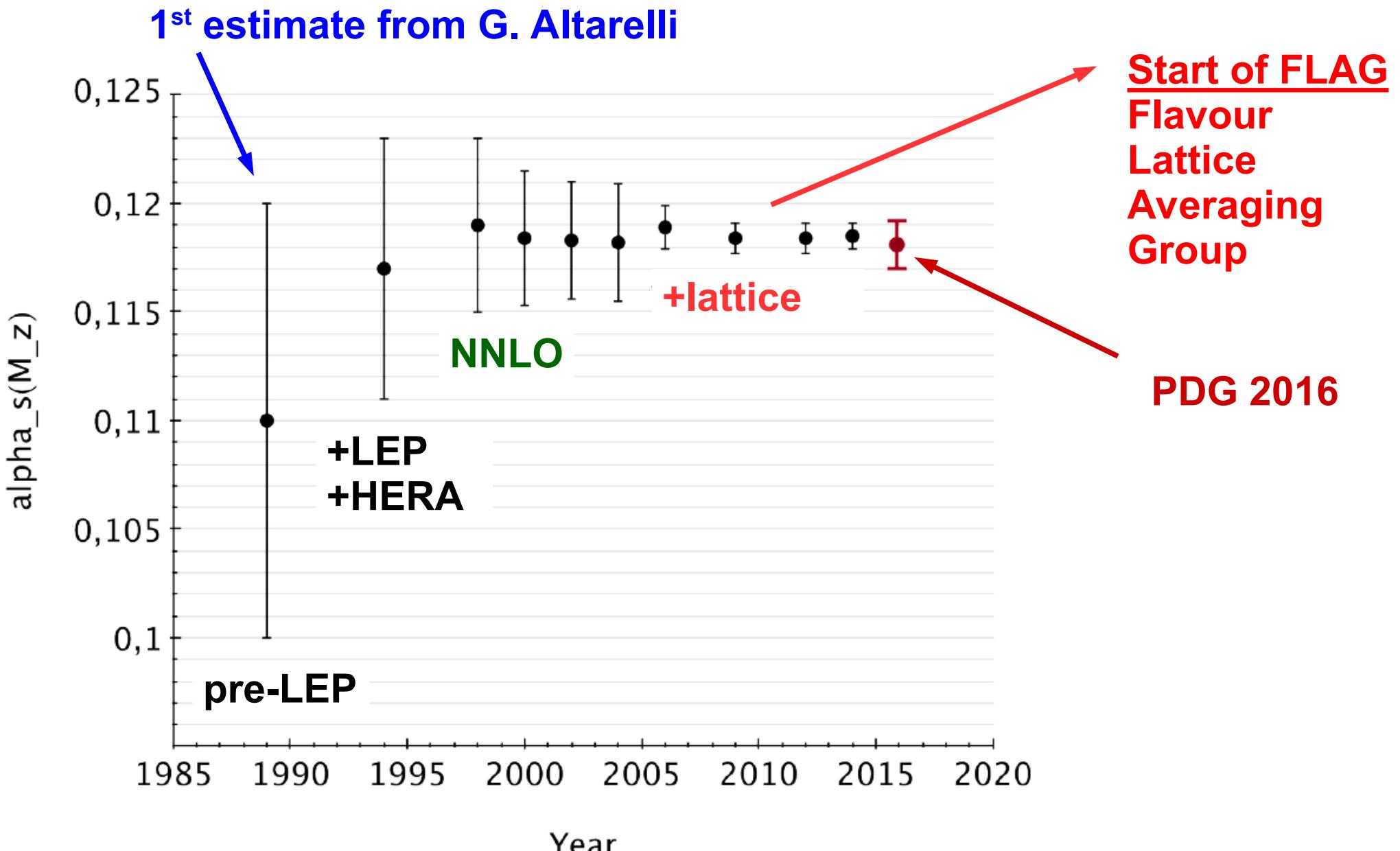
**Weak interaction ( $\beta$  decays, sun, ...)**

$$G_F \approx 1.17 \cdot 10^{-5} / \text{GeV}^2$$

$$\Delta G_F/G_F = 0.51 \cdot 10^{-6}$$



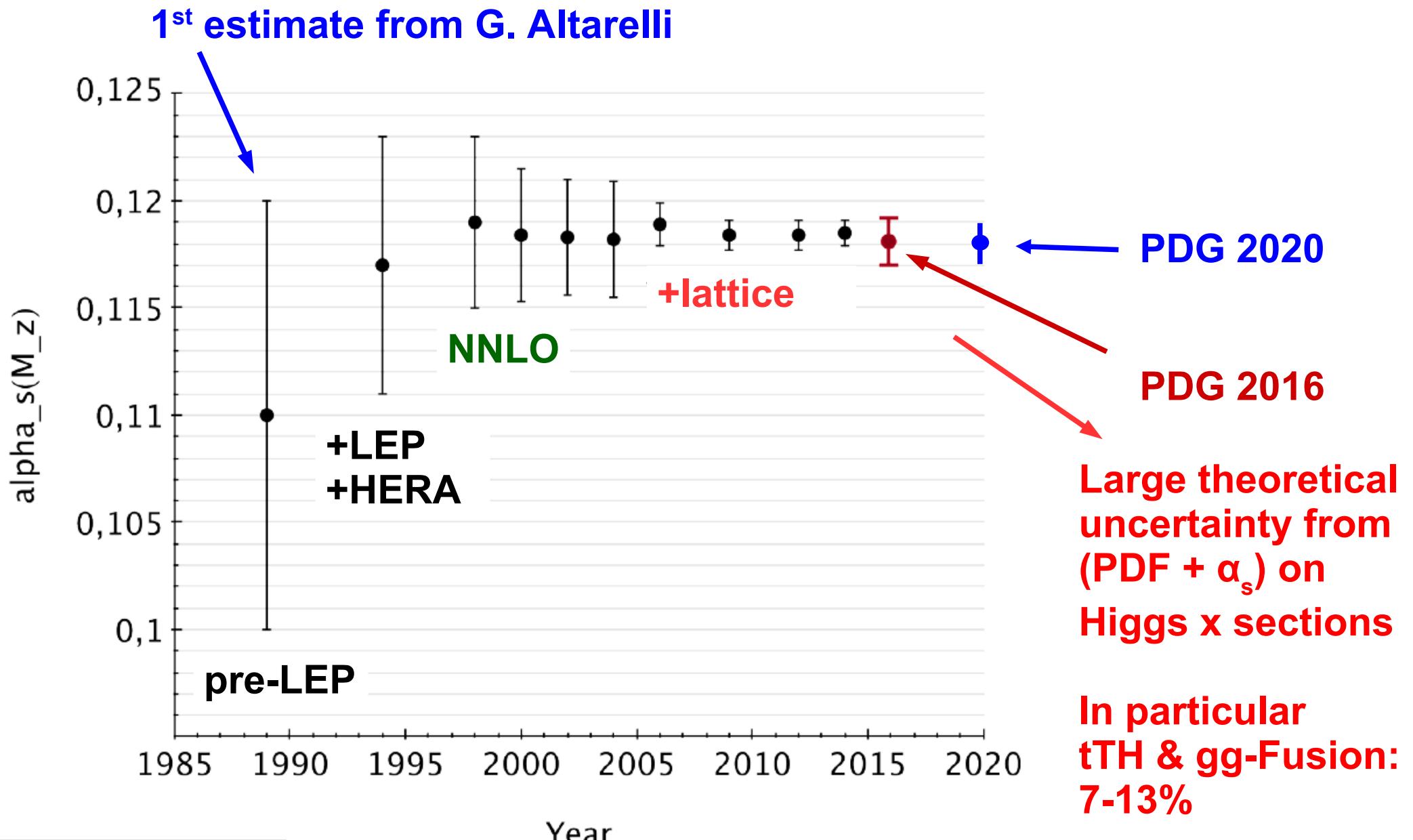
# $\alpha_s(M_z)$ world average versus time



S. Bethke, arXiv:1907.01435.



# $\alpha_s(M_Z)$ world average versus time

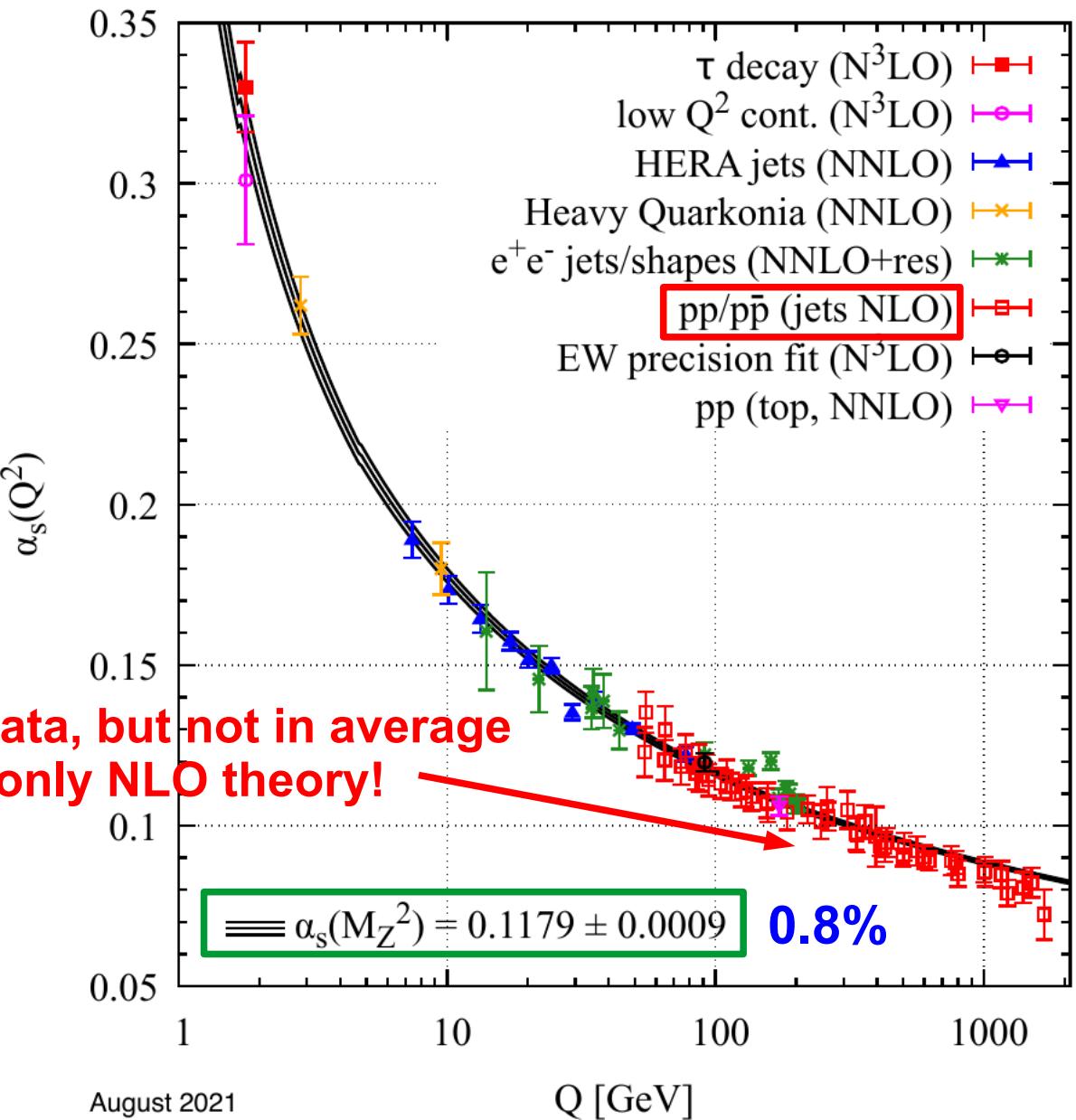
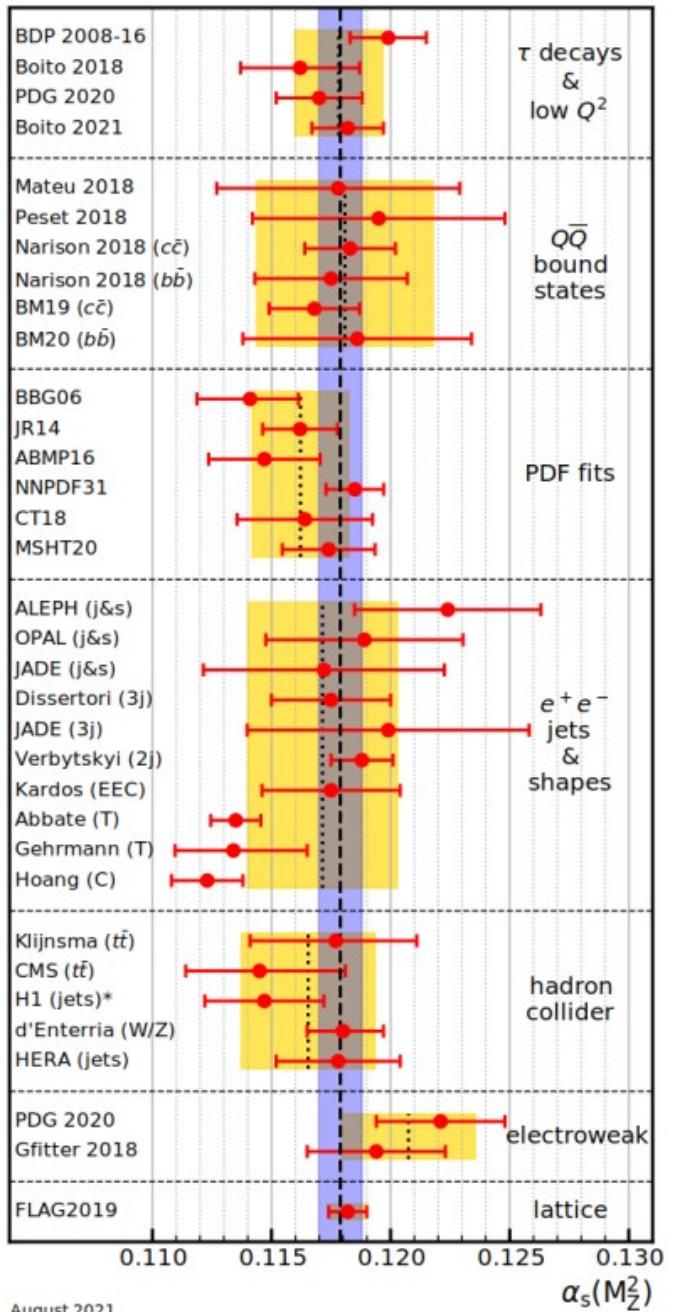


S. Bethke, arXiv:1907.01435.

CERN YR, LHC Higgs xs WG.



# PDG $\alpha_s$ average 2022



PDG, PTEP (2022) 083C01.

August 2021

Klaus Rabbertz

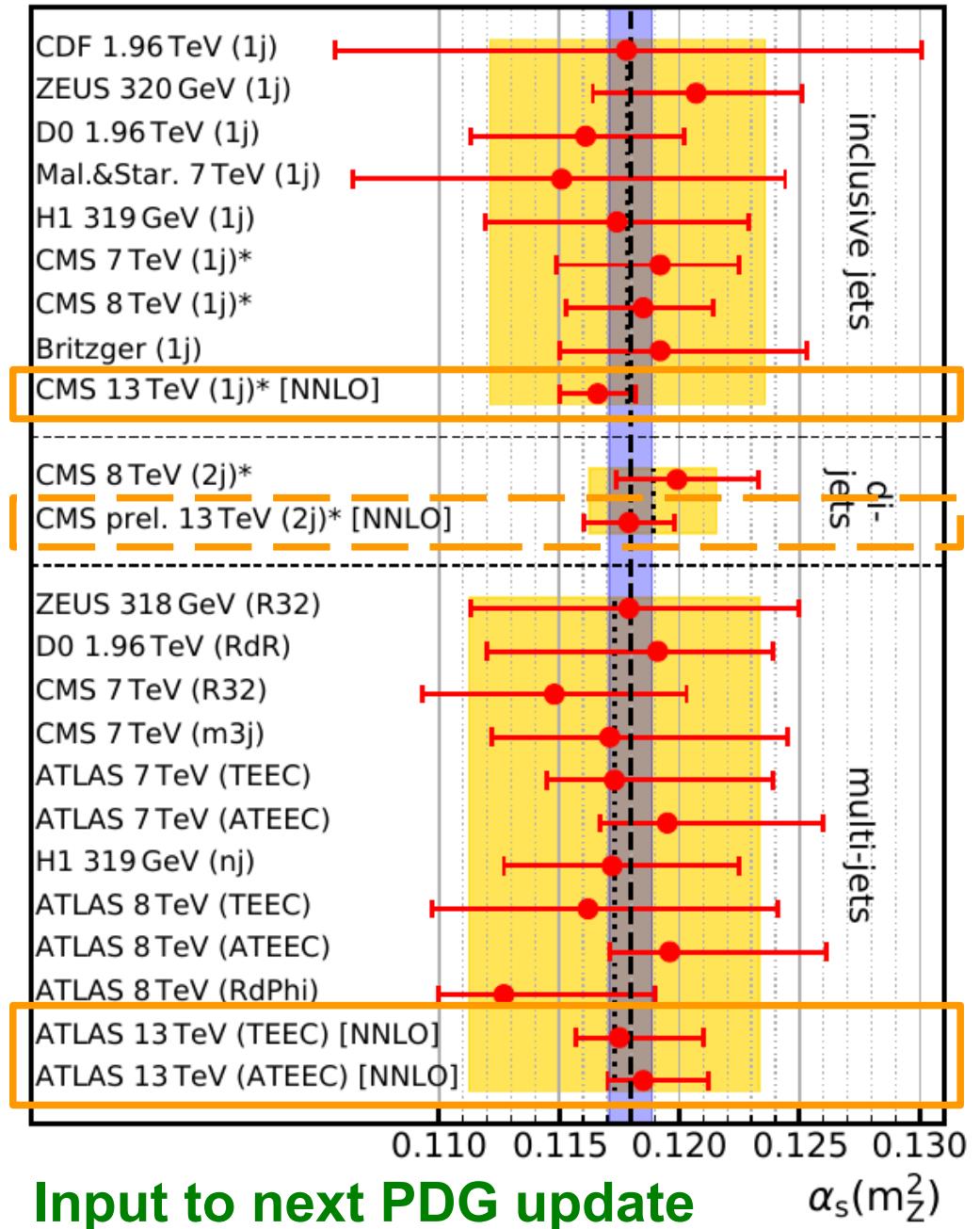
Maria Laach, 14.09.2023

54. Herbstschule 2023

63

PDG '92: 2.4%

# $\alpha_s(m^2_Z)$ from jet data



2023: new at NNLO!

Input to next PDG update

$$\alpha_s(m^2_Z)$$

# Thank you for your attention!

Thank you very much to the  
organisers for the invitation to  
this very special place

