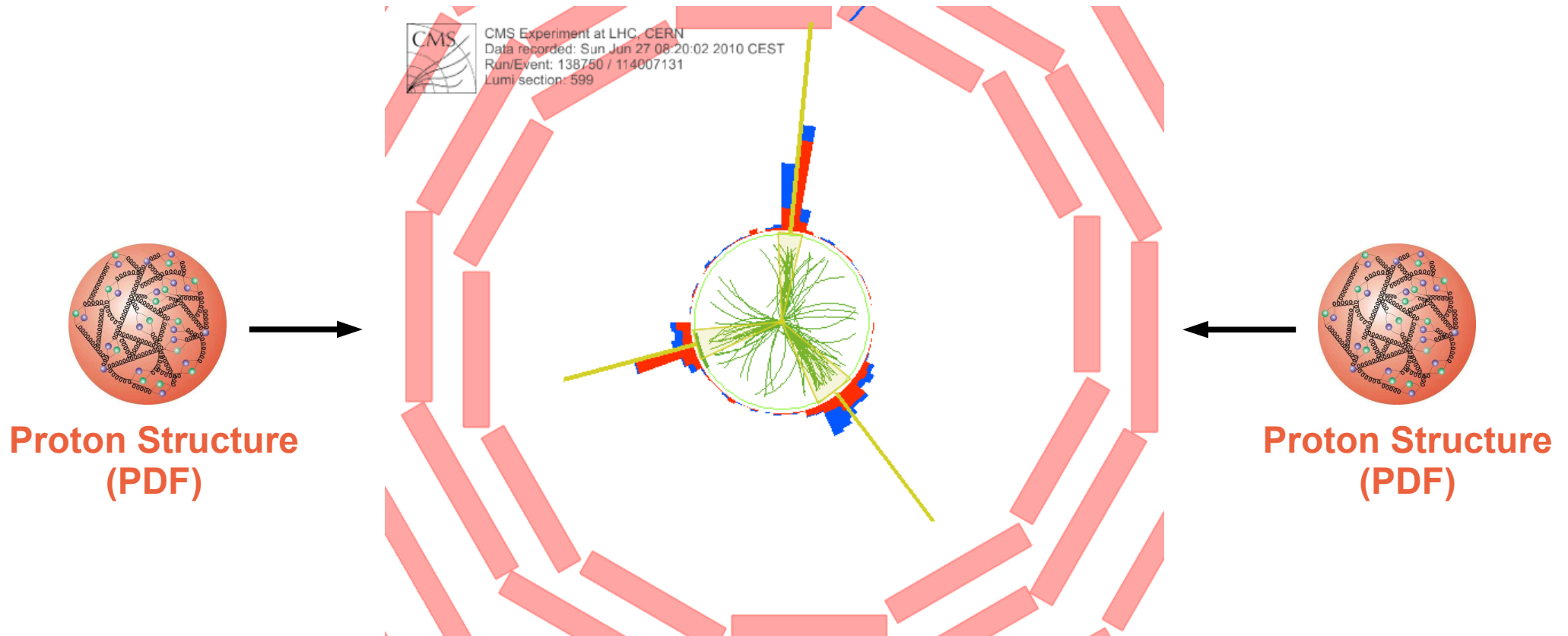
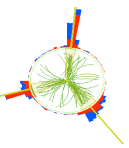


## Jet Measurements at the LHC



K. Rabbertz





## • Lecture 1

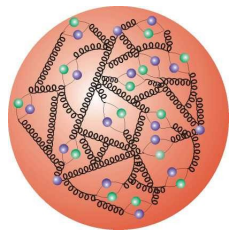
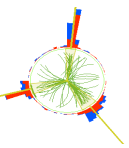
- ➔ **A bit of history**
- ➔ **Jet algorithms**
- ➔ **Jet energy calibration**
- ➔ **A first jet analysis:**
  - ➔ **Inclusive jet cross section**

## • Lecture 2

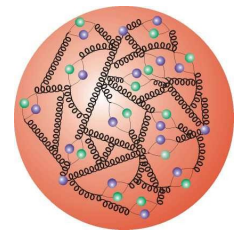
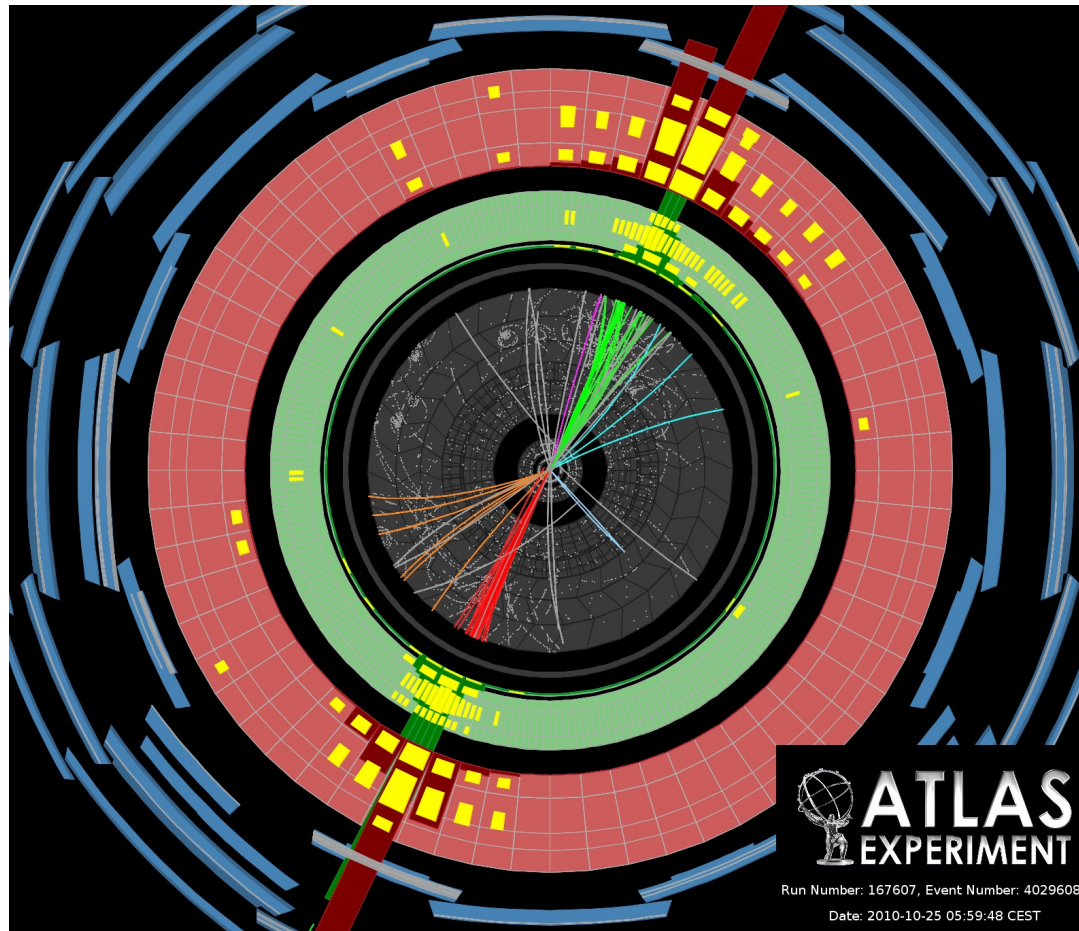
- ➔ **More cross sections**
- ➔ **Reducing uncertainties**
- ➔ **Ratios and shape comparisons**
- ➔ **Some selected observables**
- ➔ **Strong coupling**



# 2+ Jet Production



Proton

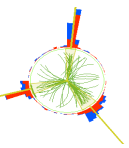


Proton





# Dijet Mass



Compatible with QCD

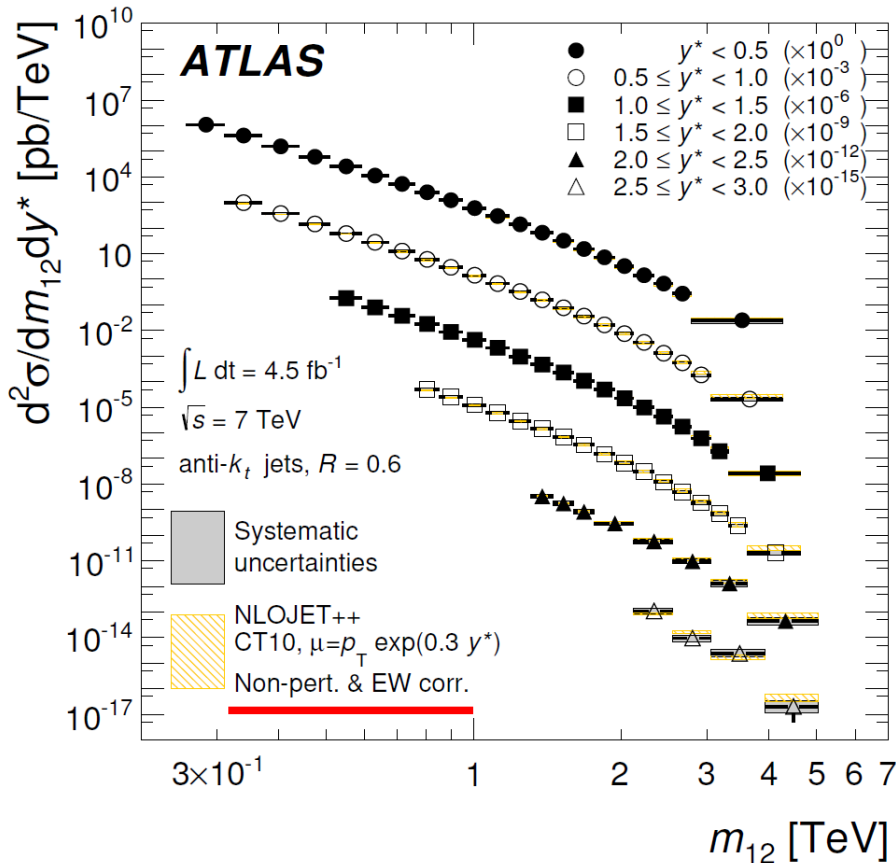
- over many orders of magnitude in  $\sigma$
- over 2 orders of magnitude in  $M_{jj}$
- up to rapidities of  $\sim 5$

$$\frac{d^2\sigma}{dM_{JJ}d|y_{max}|} \propto \alpha_s^2$$

pQCD  $\otimes$  nonperturbative and electroweak corrections

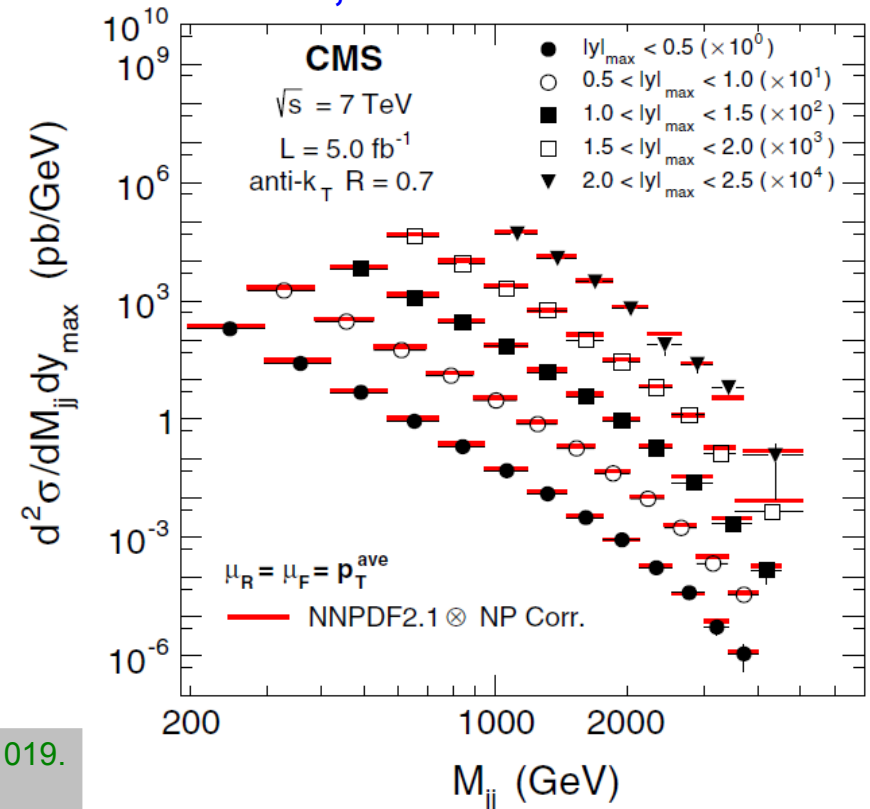
$$\frac{d^2\sigma}{dM_{jj}dy_{max}} = \frac{1}{\epsilon \cdot \mathcal{L}_{eff}} \cdot \frac{N}{\Delta M_{jj}(2 \cdot \Delta |y|_{max})}$$

anti-kT, R=0.6



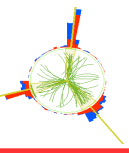
ATLAS, JHEP05 (2014) 019.  
CMS, PRD87 (2013)

anti-kT, R=0.7



No EW for older CMS study.

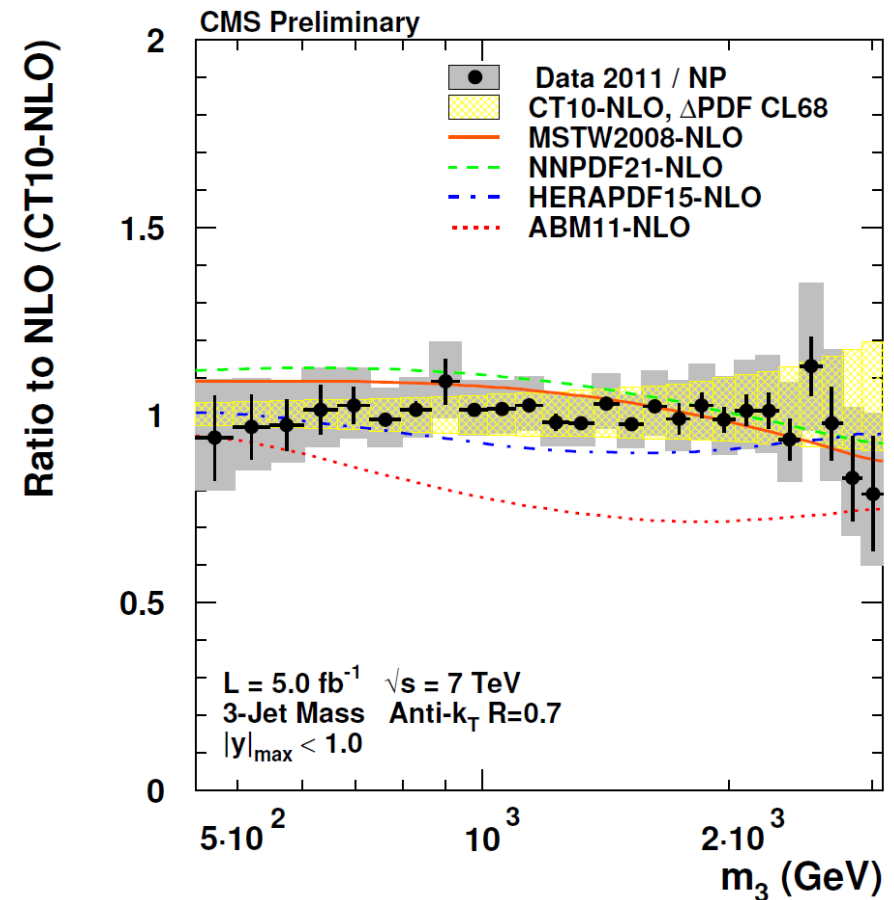
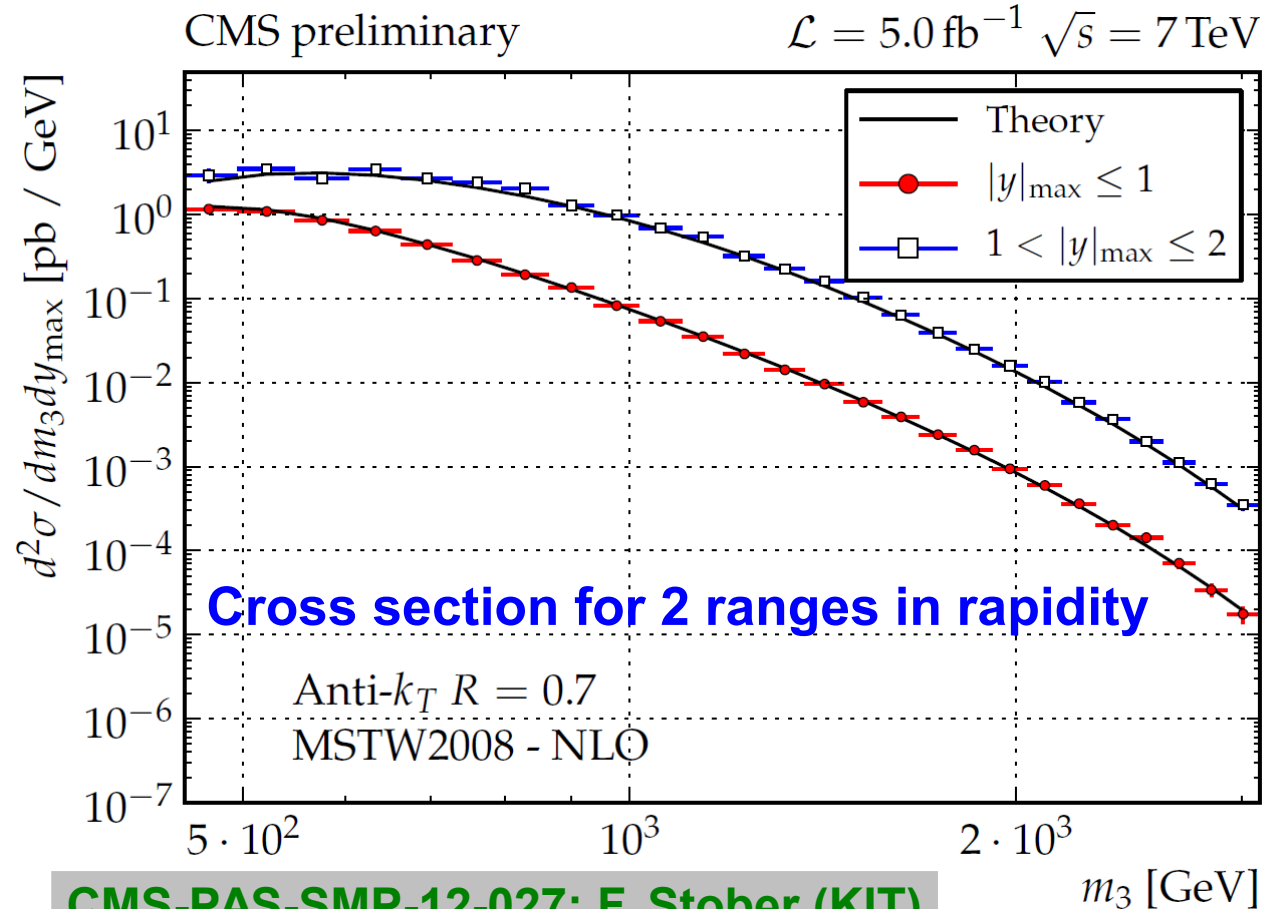
# 3-Jet Mass



- Sensitive to  $\alpha_s$  beyond  $2 \rightarrow 2$
- Sensitive to PDFs
- Involves further scale  $p_{T,3}$
- NLO with 3-4 partons (NLOJet++)

$$\frac{d\sigma_{3jet}}{dM_{3jet}} \propto \alpha_s^3$$

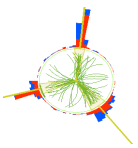
## Ratio to theory for various PDFs



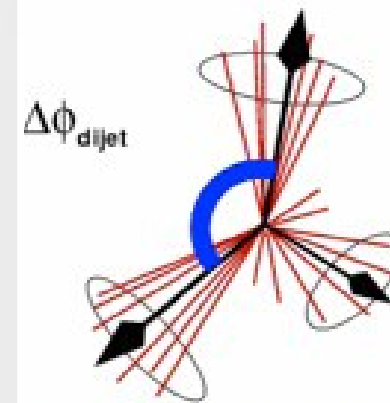
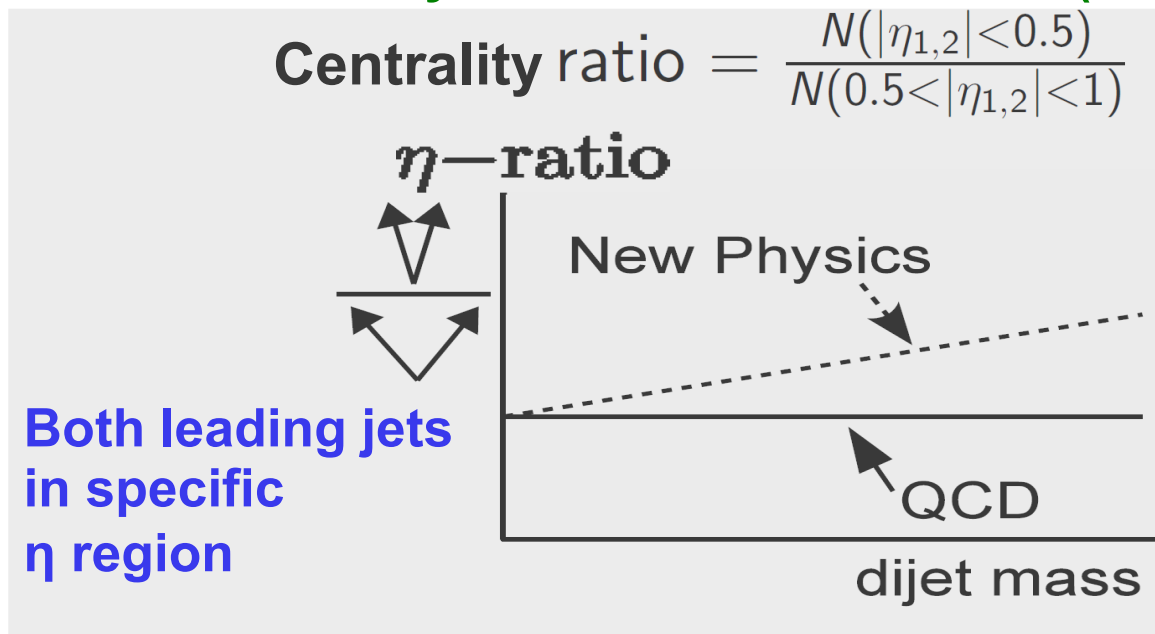
CMS-PAS-SMP-12-027: F. Stober (KIT)



# Reducing Uncertainties 1

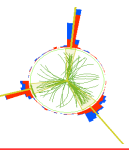


- **Measurements so far: Absolute jet cross sections**
  - ➔ Inclusive jet pT or dijet and 3-jet mass cross sections:
    - ➔ **Most complicated, require all uncertainties to be under control!**
- **Reduction strategy 1: Jet cross section ratios**
  - ➔ Dijet mass cross section ratios in rapidity  $\longrightarrow$  new physics ?
  - ➔ 3-jet to 2-jet cross section ratio  $\longrightarrow$  strong coupling  $\alpha_s$
  - ➔ **Many uncertainties cancelled (luminosity, ...) or reduced (JES, ...)**



$\sim$  strong coupling  $\alpha_s$   
jet 3

# Reducing Uncertainties 2



## ● Reduction strategy 2: Jet angular measurements

- ➔ Dijet chi distribution  $\longrightarrow$  new physics ?
- ➔ Dijet azimuthal decorrelation  $\longrightarrow$  deviations from QCD radiation ?
  - ➔ Reduced sensitivity to jet energy scale (JES) or resolution (JER)

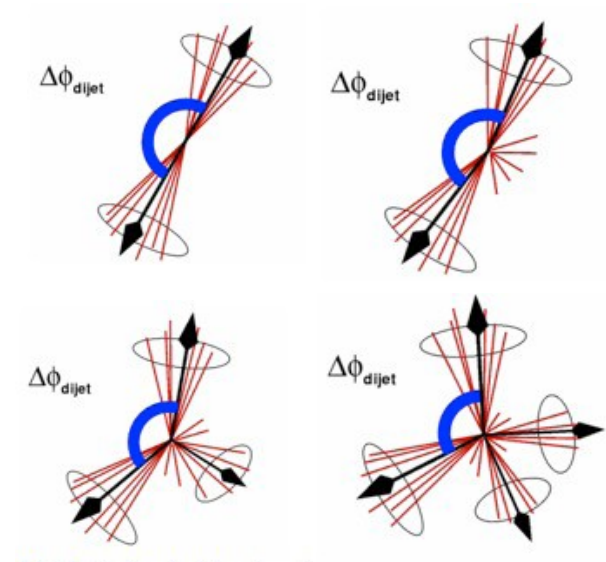
## ● In addition: Normalized distributions

- ➔ Event shapes  $\longrightarrow$  Test of QCD, MC tuning
  - ➔ Less sensitive to JES, not dependent on luminosity

Transverse global thrust

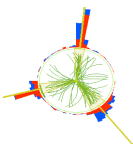
Thrust

Thrust minor

$$T_{\perp,g} = \max_{\vec{n}_T} \frac{\sum_i |\vec{p}_{\perp,i} \cdot \vec{n}_T|}{\sum_i p_{\perp,i}}$$




# Inclusive Jet Ratios: 2.76 / 7.0



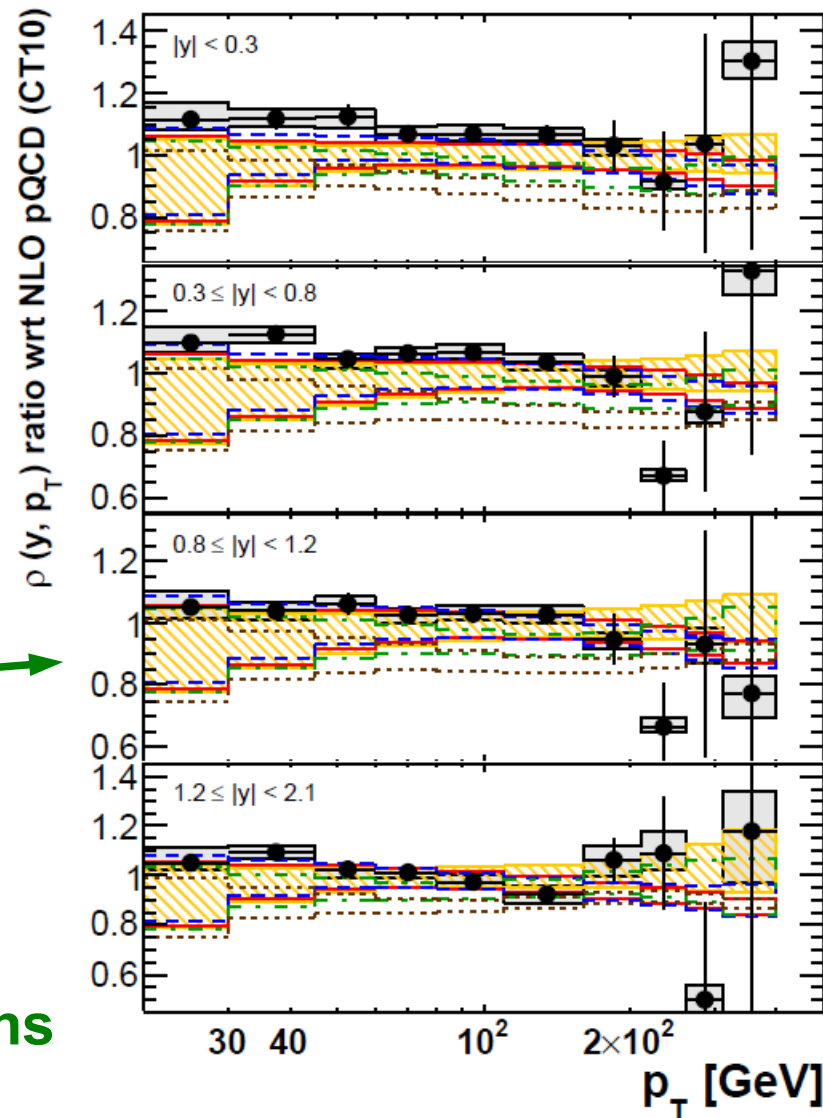
Here:  
Ratio at different energies  
 $E_{\text{cms}} = 2.76$  and  $7.0$  TeV

## Result from ATLAS:

- cross sections at 2.76 TeV
- ratios to 7 TeV
- ratio to 7 TeV divided by theory prediction (NLO, CT10, X NP)
- **Shown**
- study on PDF impact

At least partial cancellation of uncertainties

→ more precise comparisons



## ATLAS

$$\int L dt = 0.20 \text{ pb}^{-1}$$

$$\rho = \sigma_{\text{jet}}^{2.76\text{TeV}} / \sigma_{\text{jet}}^{7\text{TeV}}$$

anti- $k_t$   $R = 0.6$

- Data with statistical uncertainty
- Systematic uncertainties

NLO pQCD ⊗ non-pert. corrections

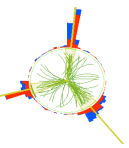
- ▨ CT10
- MSTW 2008
- - - NNPDF 2.1
- · - · HERAPDF 1.5
- · · · ABM 11 NLO

ATLAS, arXiv:1304.4739.





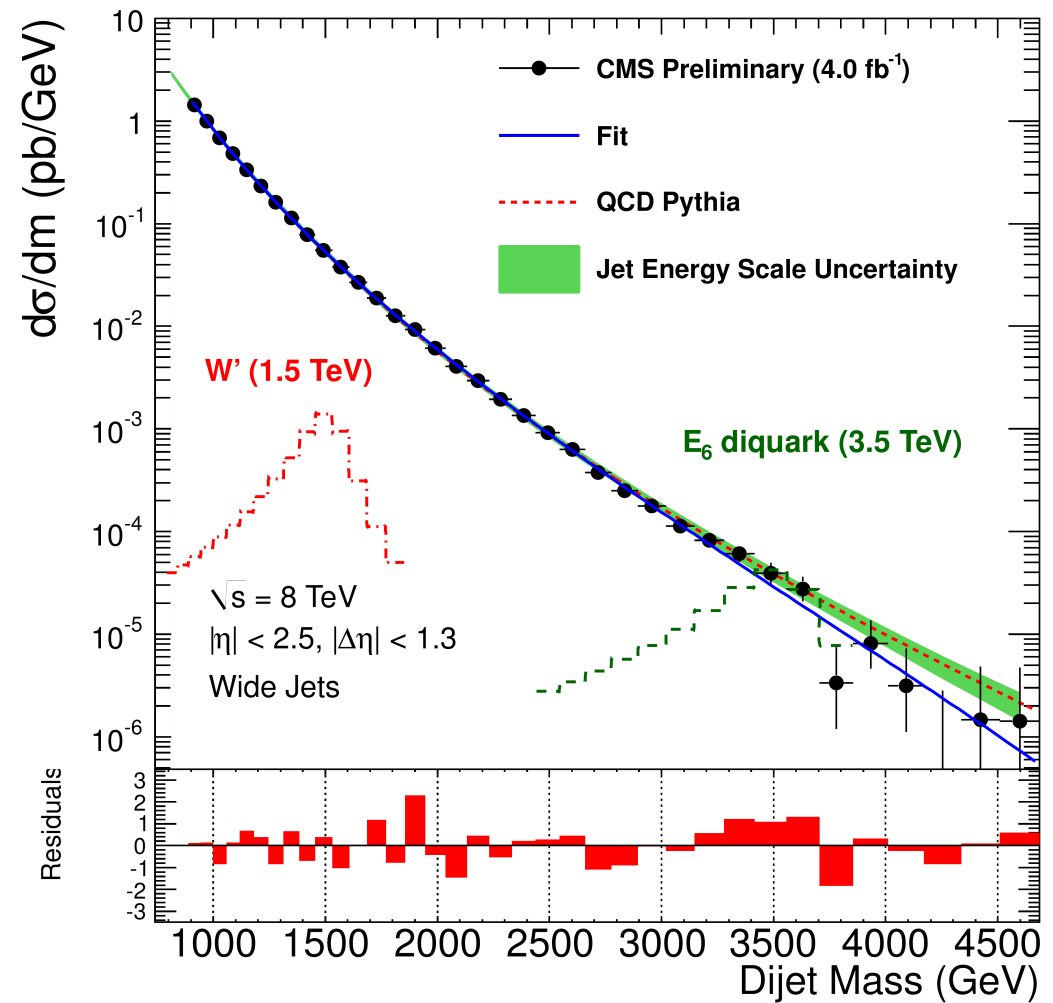
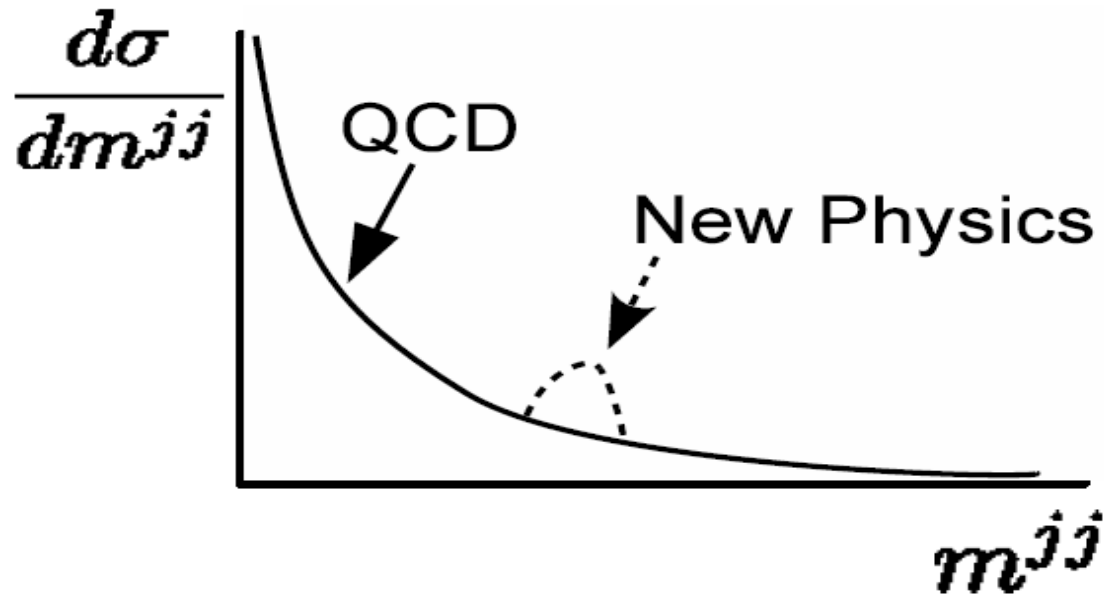
# Bump Hunt



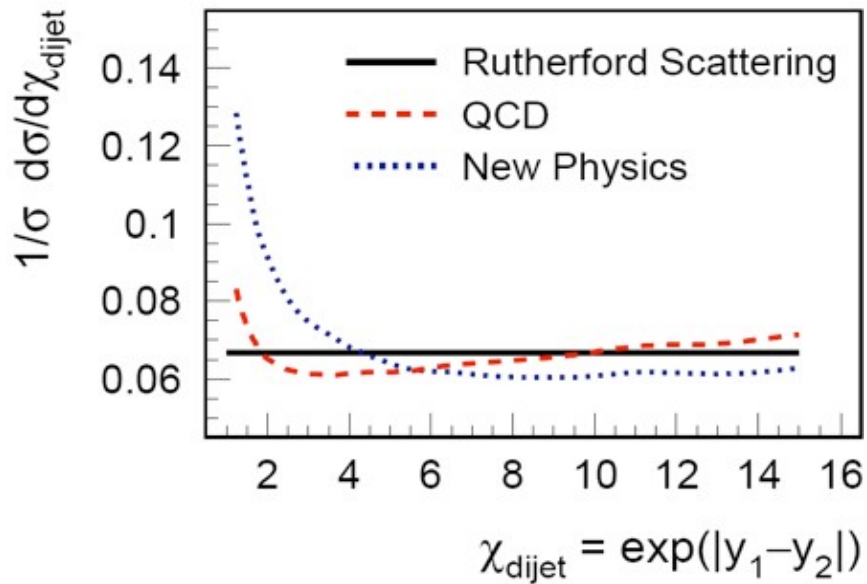
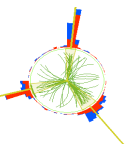
## Simple search for new physics: Dijet resonance

Absolut QCD cross sections not required, only shape needs to be described.

So far nothing found.  
CMS result @ 8 TeV, 4.0 / fb:

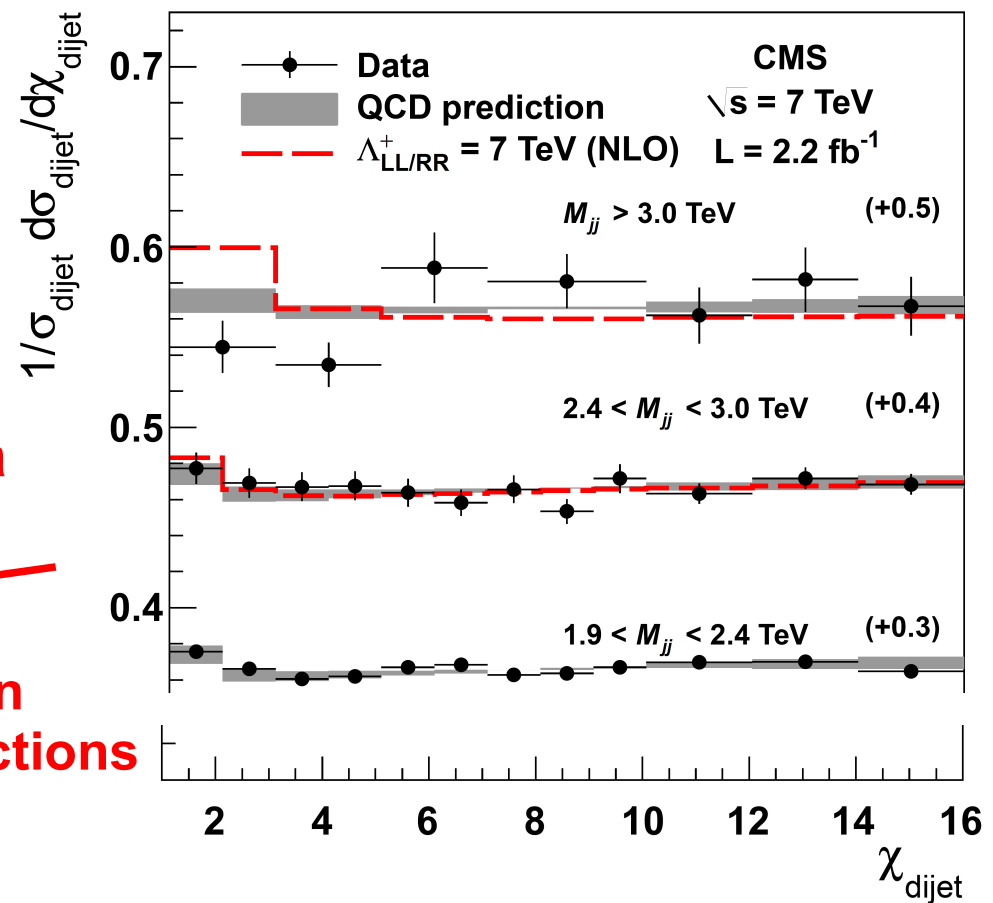
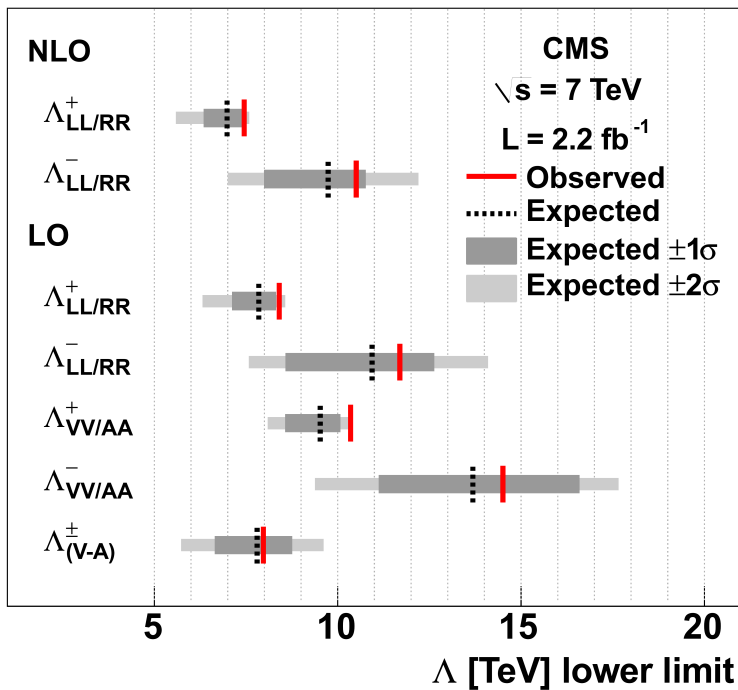


# Dijet angular distribution

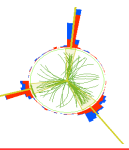


$$\frac{d^2\sigma}{dM_{JJ}d\chi_{JJ}} \propto \alpha_s^2$$

$$\chi = \exp(|\eta_1 - \eta_2|) = \frac{1 + |\cos(\hat{\theta})|}{1 - |\cos(\hat{\theta})|}$$



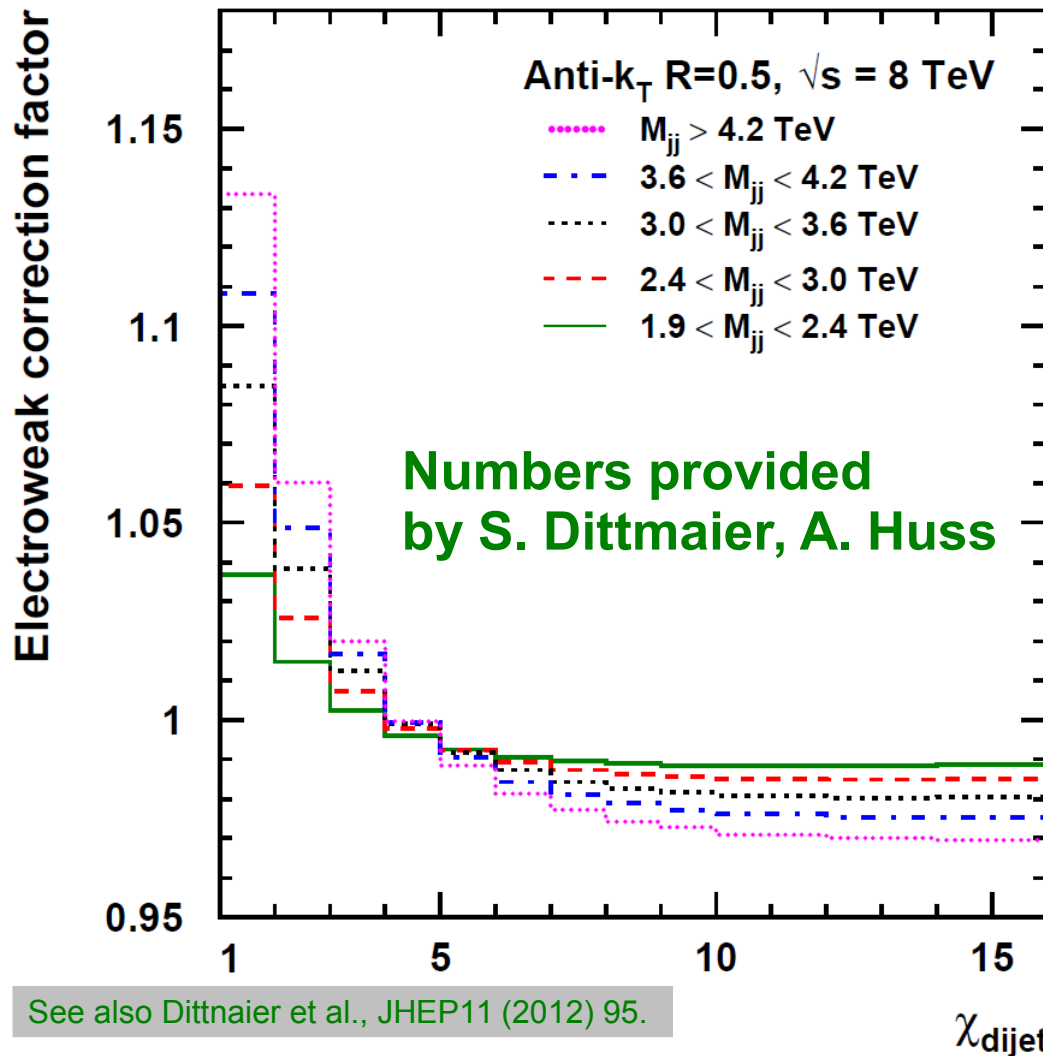
# Dijet angular distribution



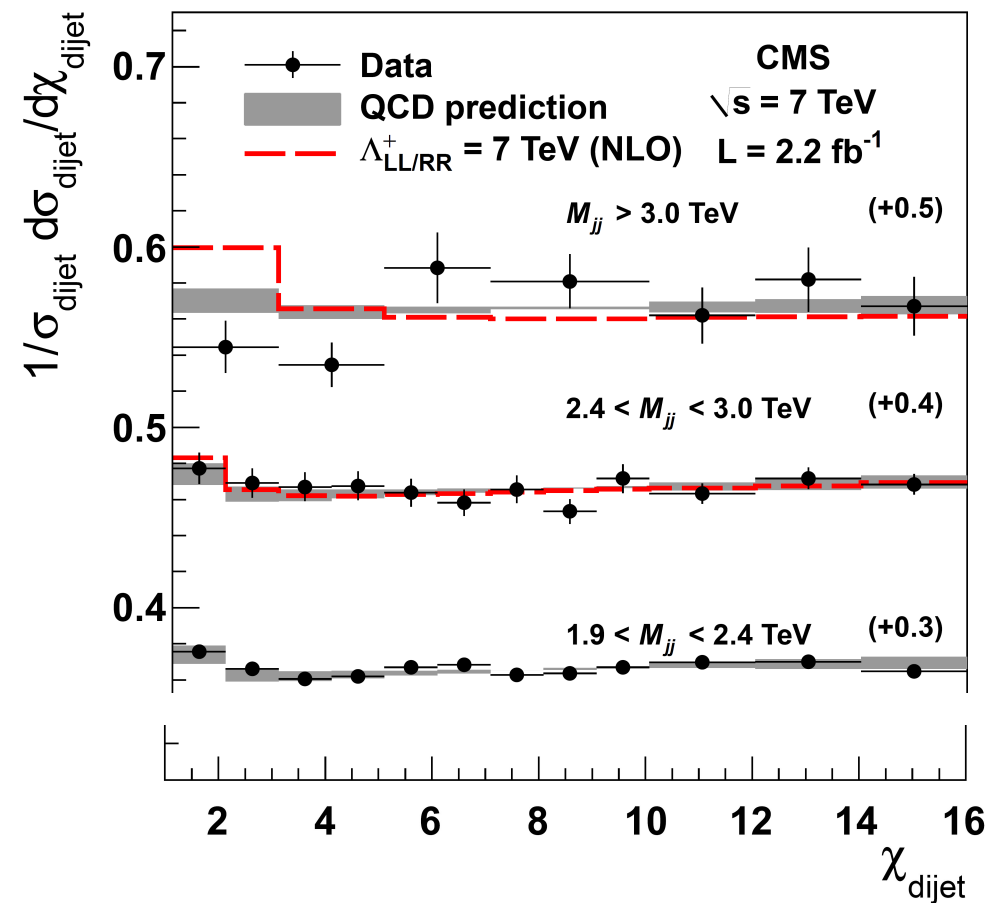
Update for full 2012 luminosity in progress  
Accounts for electroweak corrections

$$\frac{d^2\sigma}{dM_{JJ}d\chi_{JJ}} \propto \alpha_s^2$$

$$\chi = \exp(|\eta_1 - \eta_2|) = \frac{1 + |\cos(\hat{\theta})|}{1 - |\cos(\hat{\theta})|}$$

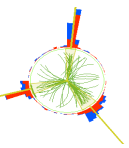


See also Dittmaier et al., JHEP11 (2012) 95.





# Azimuthal Decorrelation



## Jet-pairs in pp collisions:

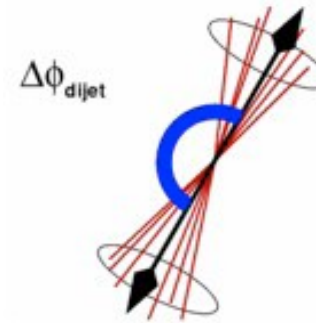
$\Delta\phi_{\text{dijet}} = \pi \rightarrow$   
Exactly 2 jets, no further radiation

$\Delta\phi_{\text{dijet}} \approx \pi \rightarrow$   
Additional soft radiation

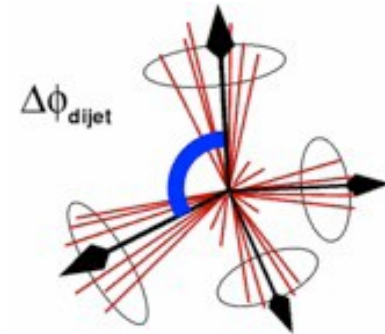
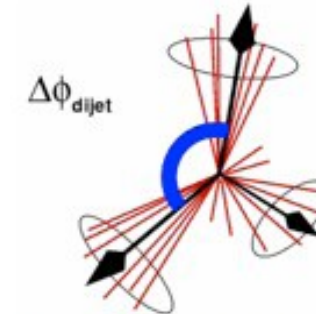
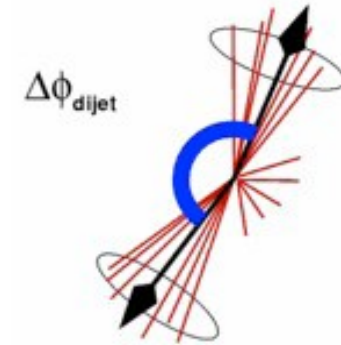
$\Delta\phi_{\text{dijet}} \approx 2\pi/3 \rightarrow$   
At least one additional high-pT jet

$\Delta\phi_{\text{dijet}} \ll 2\pi/3$   
Multiple hard jets

$$\frac{d^2\sigma}{dp_{T,\text{max}} d\Delta\phi_{JJ}} \propto \alpha_s^3$$



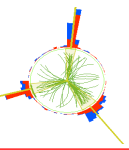
**2-jet: correlated  $\rightarrow \pi$**



M. Wobisch

**multi-jet: “uncorrelated”  $\rightarrow < \pi$**

# Azimuthal Decorrelation

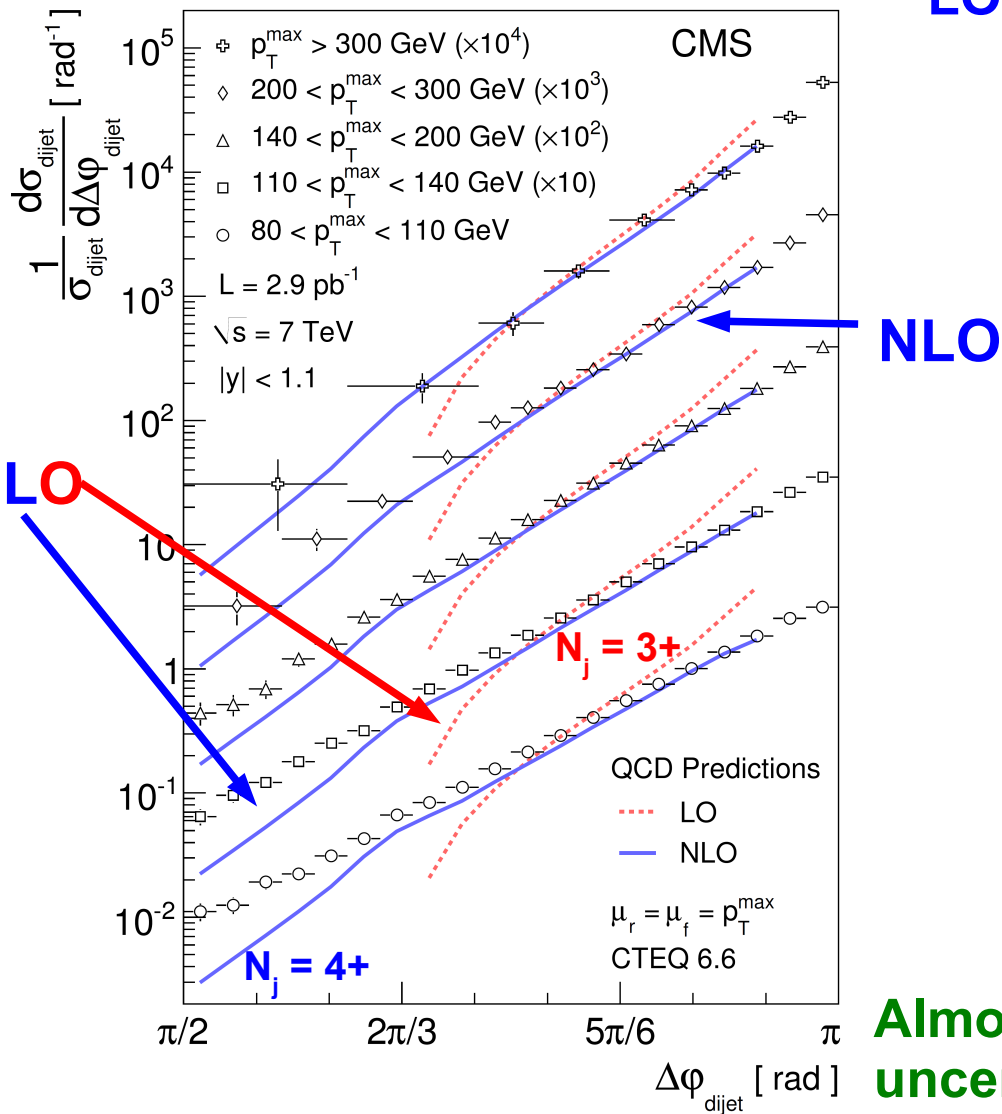


Interesting quantity to study for ISR effects (MC tuning) or multijet production

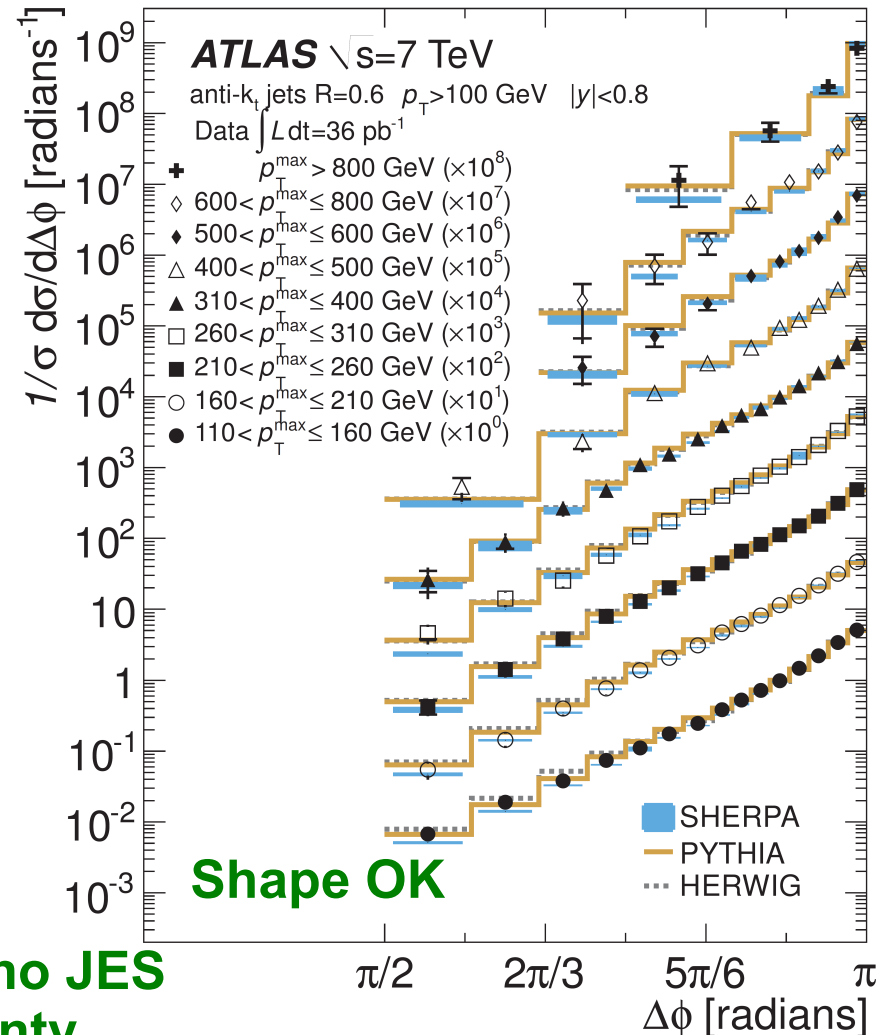
CMS comparison with pQCD

ATLAS comparison with MC predictions

LO MC Pythia, Herwig++; n-jet-improved Sherpa

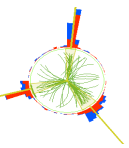


Almost no JES uncertainty





# Color Coherence



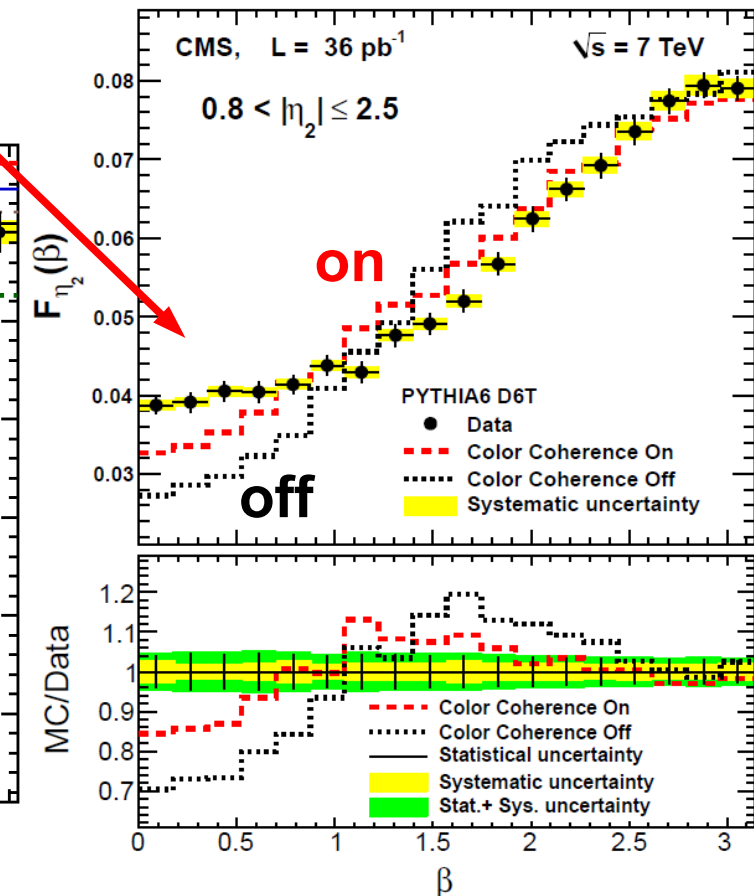
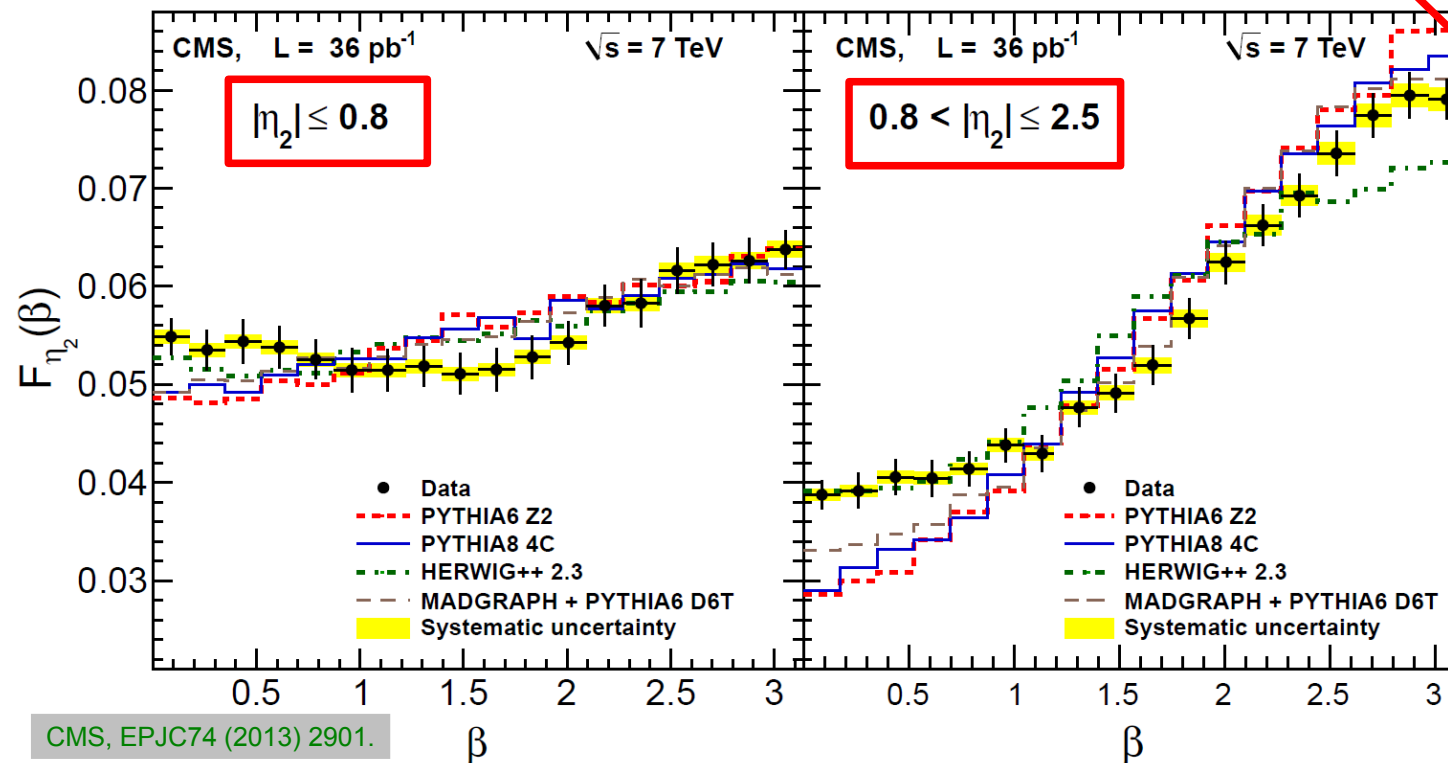
Study orientation of 3<sup>rd</sup> jet emission near 2<sup>nd</sup> → test interference in parton emissions

$$\beta = \left| \tan^{-1} \frac{\Delta\phi_{32}}{\text{sign}(\eta_2)\Delta\eta_{32}} \right|$$

$\beta \sim 0 \rightarrow$  emission between jet 2 and beam

In MC approximated by angular ordering → improves description still not perfect

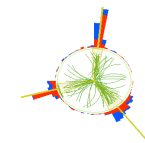
No MC really good, better tunes required



CMS, EPJC74 (2013) 2901.



# Dijet Flavours



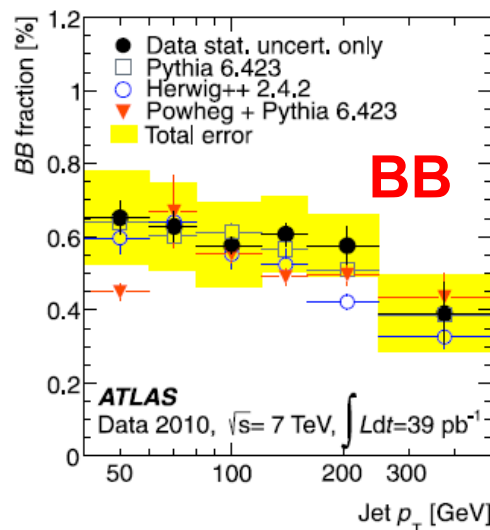
## Study of flavour decomposition of both jets in dijet events

Jet flavour determined via template fits to kinematic properties of secondary vertices inside jets

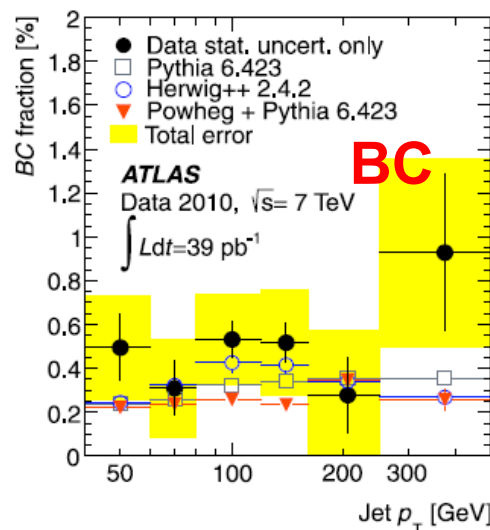
Templates differentiate between B, C and light (U) quarks

Well described by MC For most flavour pairs

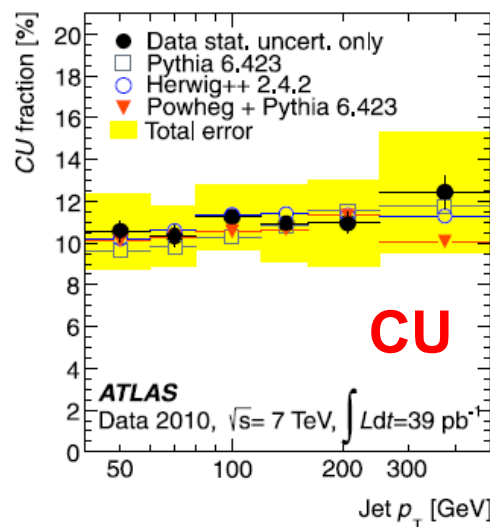
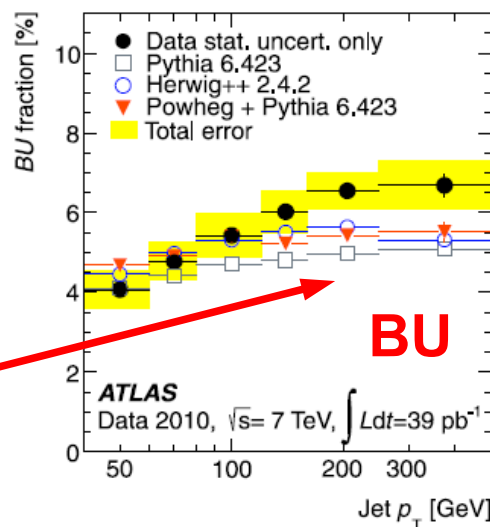
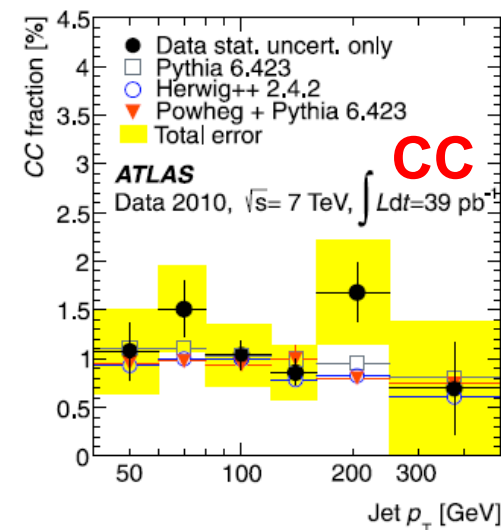
Some discrepancy for B-light (U) contribution at high  $p_T$



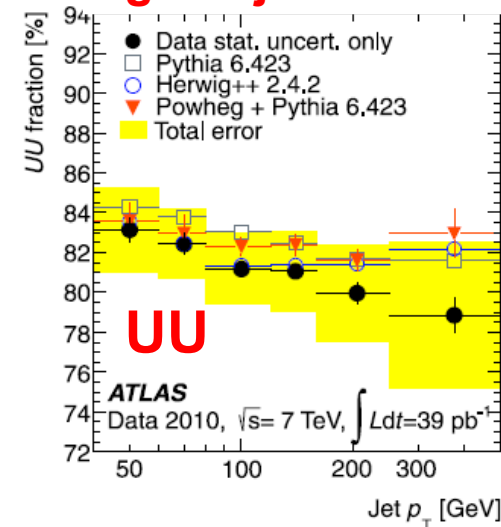
(a)



(b)



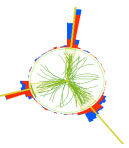
light dijets ~ 80%



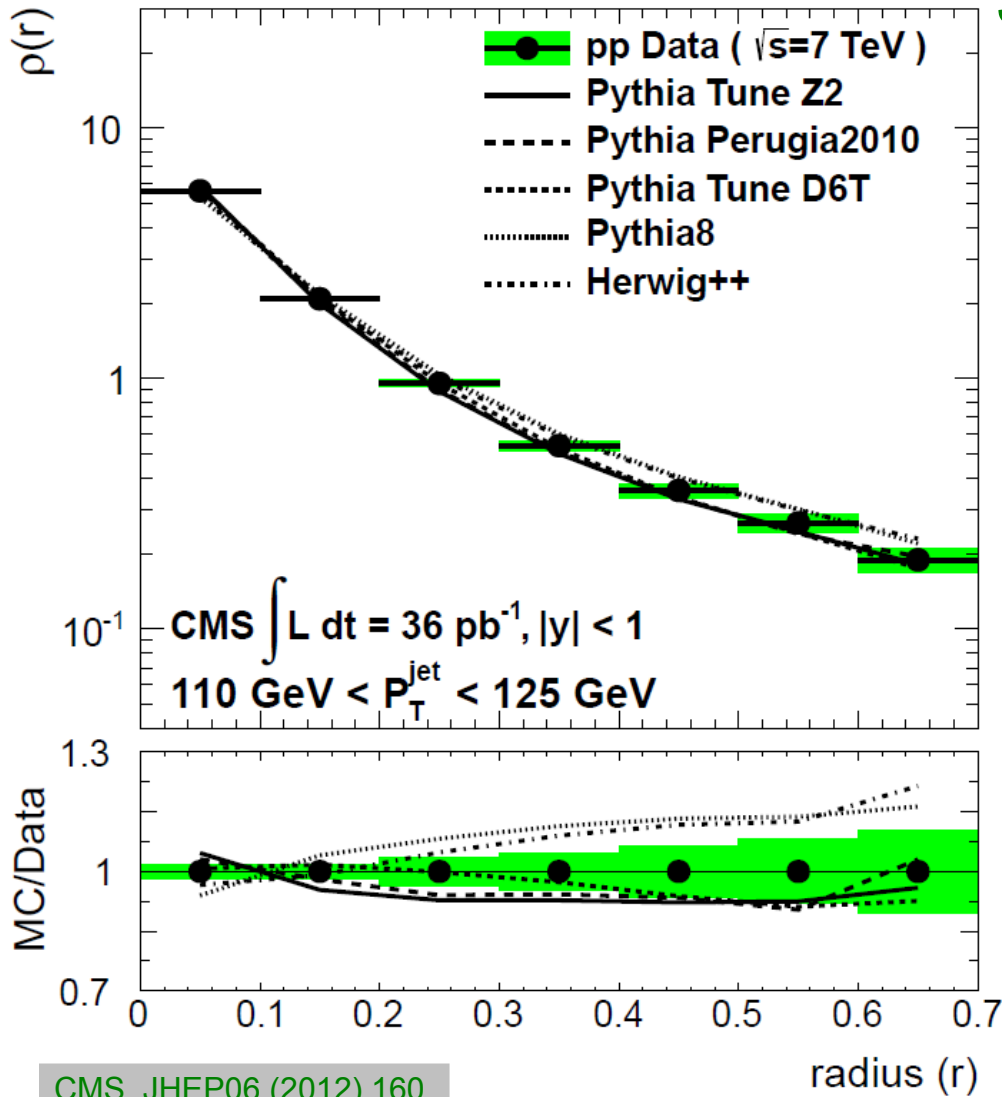
ATLAS, EPJC73, 2013



# Jet Shapes

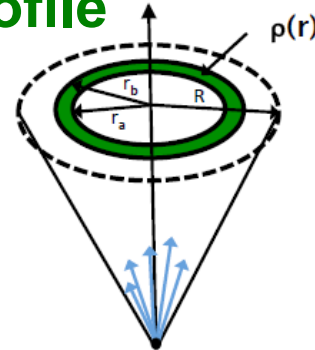


Jet substructure: Differentiate among g, q jets and heavy boosted  $Z'$ ,  $t'$ , ...  
Here: "Traditional" jet profiles, sensitive to g-, q-jet differences

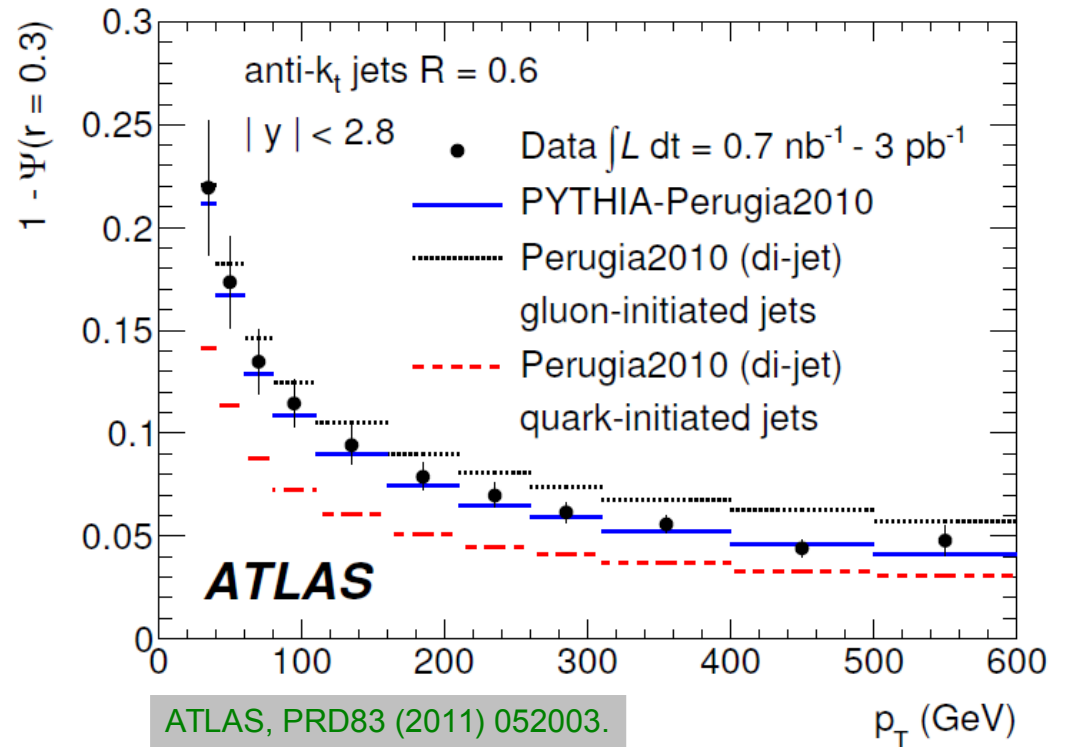
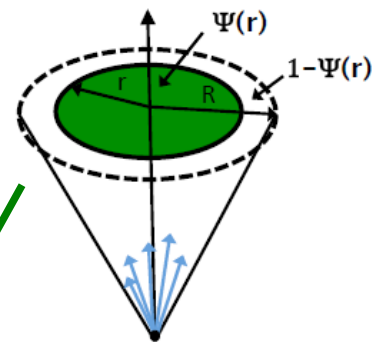


CMS, JHEP06 (2012) 160.

Jet  $p_T$  profile



Integrated

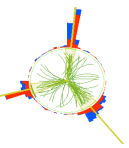


ATLAS, PRD83 (2011) 052003.





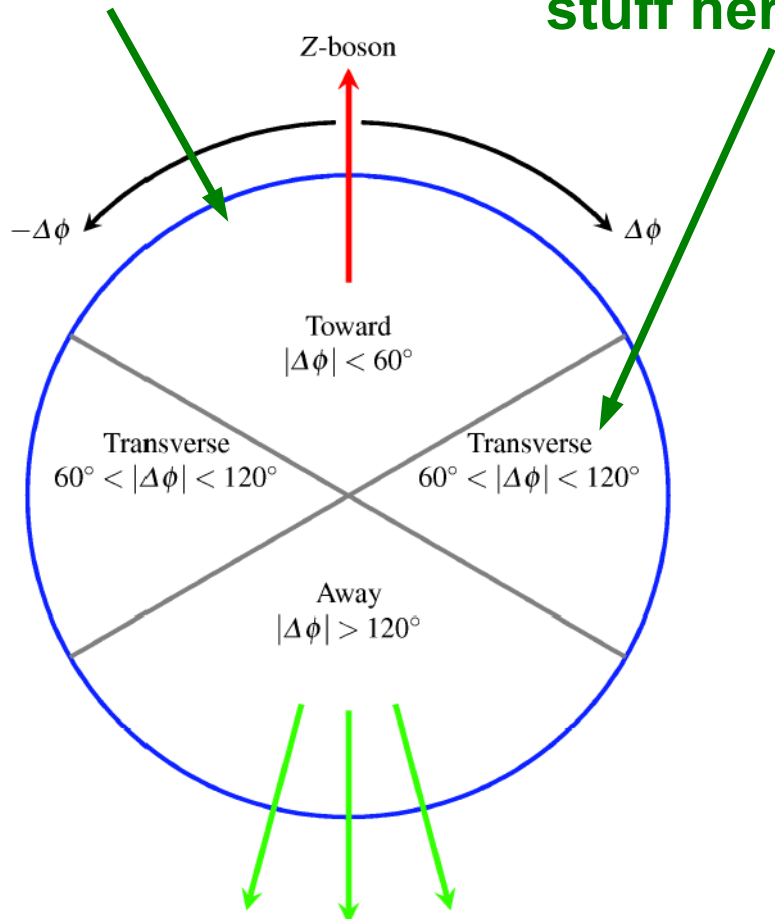
# Underlying Event



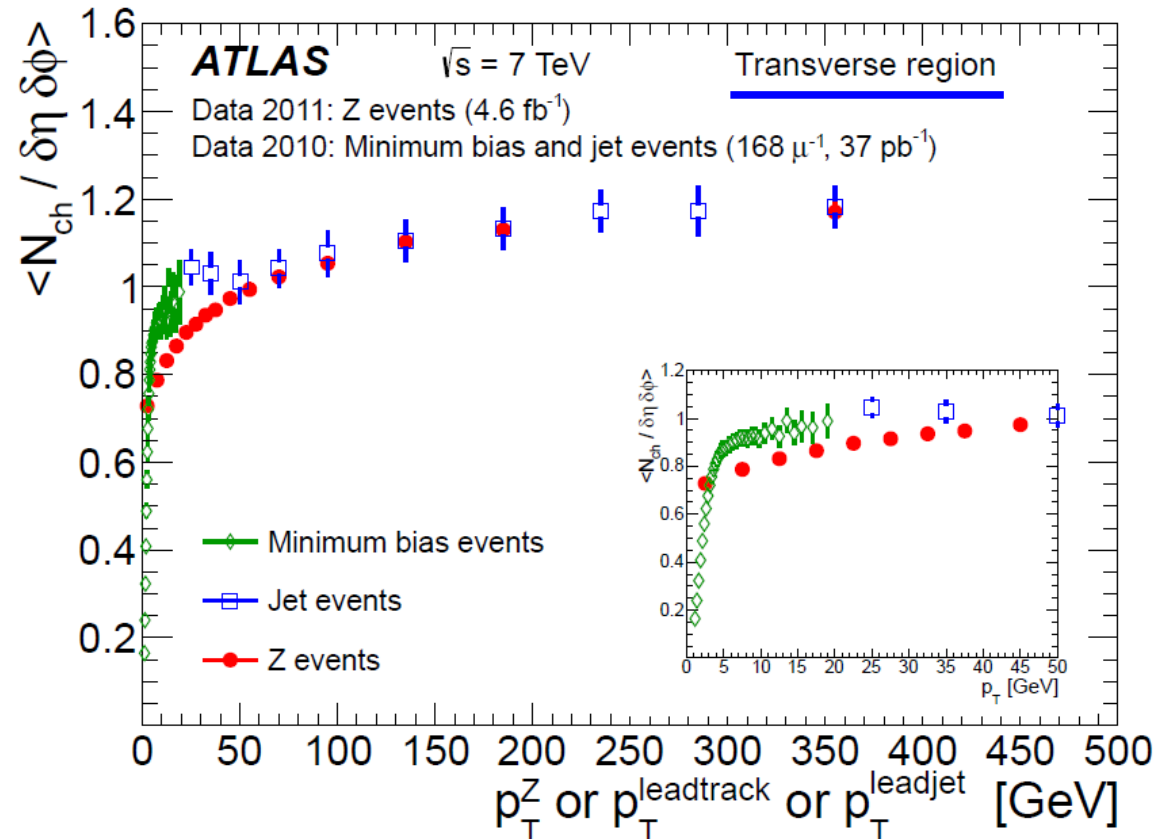
## New ATLAS result investigating the UE in Z+jet events

Also here  
if  $Z \rightarrow \mu\mu$

Look for soft  
stuff here



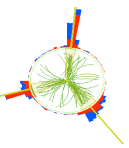
No indication of unexpected differences  
among UE in MinBias, jet, or Z+jet events



ATLAS, arXiv:1409.3334



# Jet-radius Ratio



G. Soyez,  
PLB698 (2011).

ALICE study  
R=0.2 / R=0.4

ALICE, PLB722 (2013).

Cross section ratio for R = 0.5/0.7

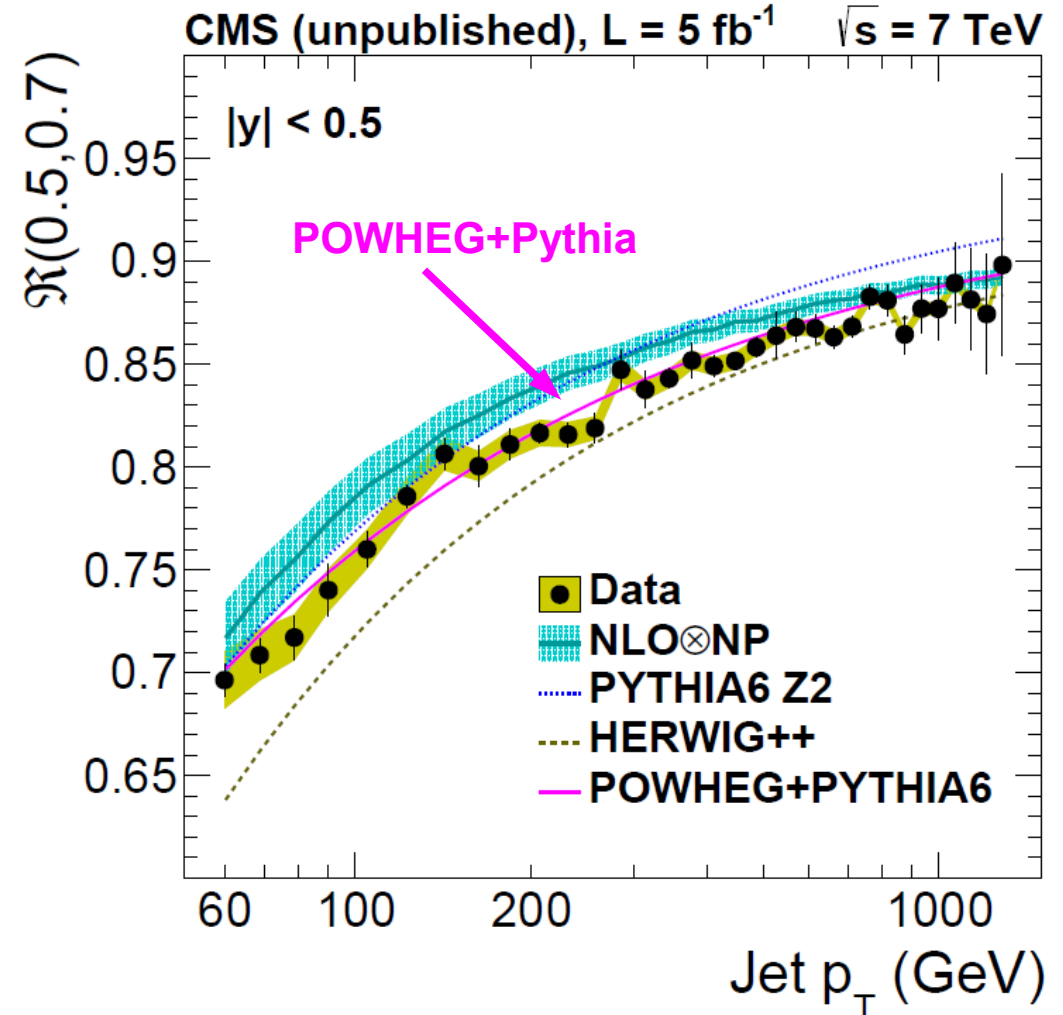
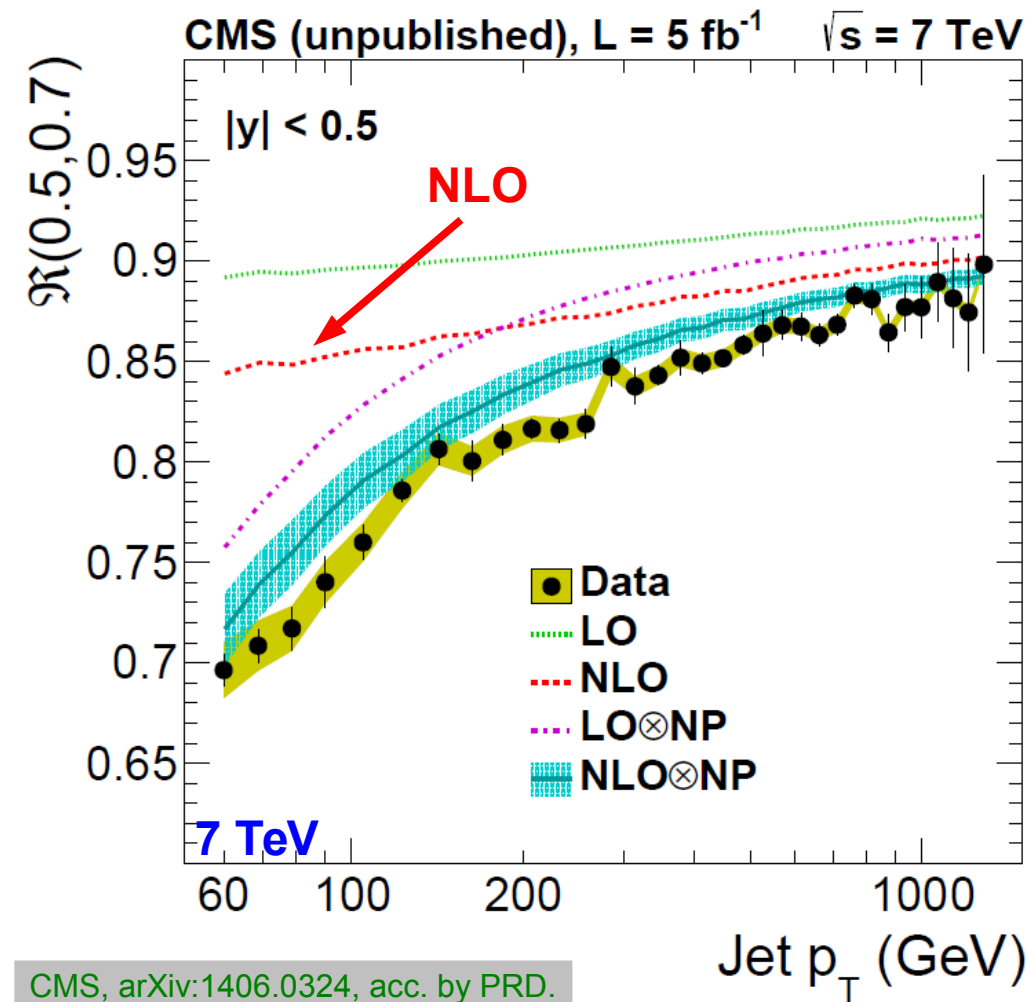
Emphasizes effects of  
showering and hadronization

→ NLO insufficient to describe data!

Requires event generators:

LO+PS+HAD → better  
(Pythia6, Herwig++)

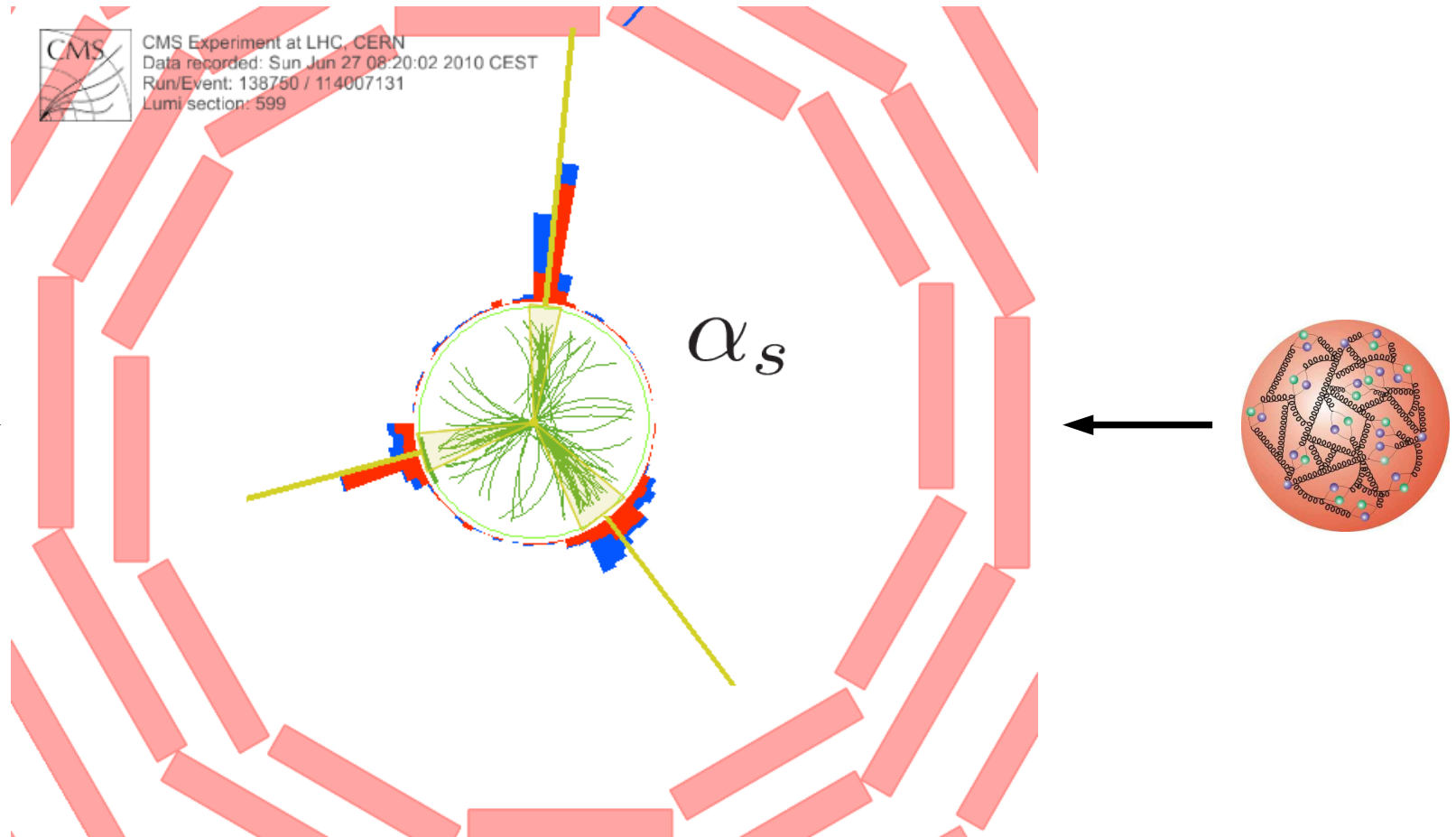
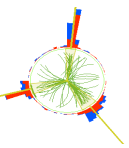
NLO+PS+HAD → best  
(POWHEG+Pythia)



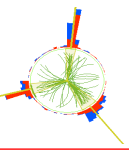
CMS, arXiv:1406.0324, acc. by PRD.



# $\alpha_s (1 \text{ TeV}) ?$

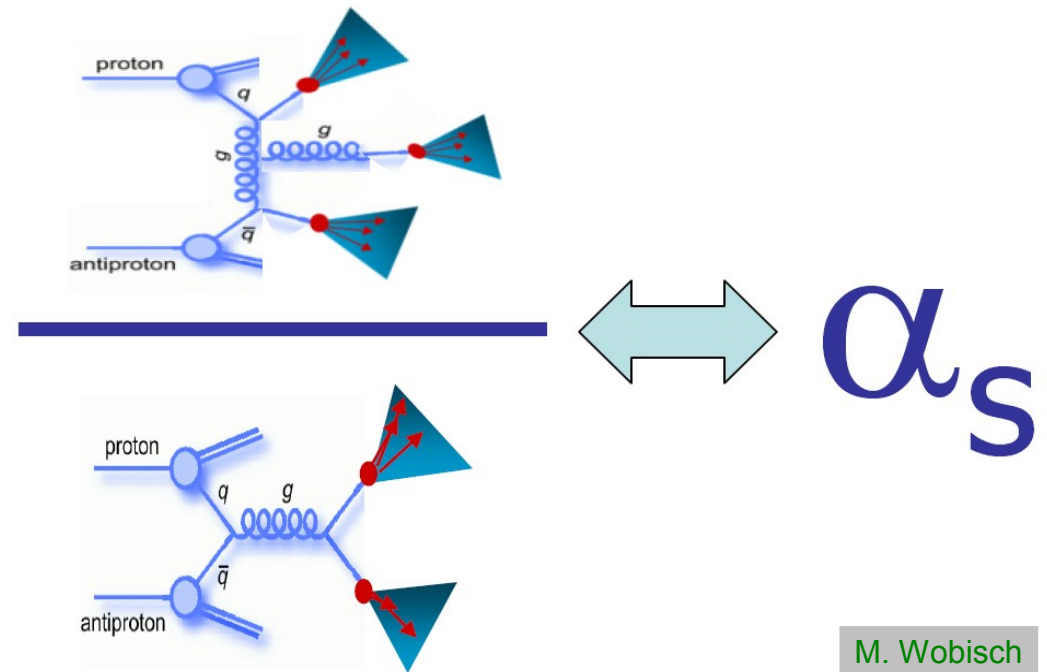


# 3-Jet Ratios and $\alpha_s$ in $hh$



Normalization or ratios for different multiplicity  $N_{\text{jet}} = 3$  over 2:

- Similar as in H1 normalized cross Sections, see later.
- Reduce exp. and scale uncertainties
- Eliminate luminosity dependence
- Avoid direct dependence on PDFs and the RGE



M. Wobisch

Three observables investigated:

**D0:  $R_{\Delta R}$**

- Average no. of neighbor jets within  $\Delta R$  in incl. sample
- D0 midpoint cone  $R=0.7$
- Min. jet  $p_T$ : 50 GeV
- Max. rap.:  $|y| < 1.0$
- Scale: Jet  $p_T$
- Data 0.7/fb

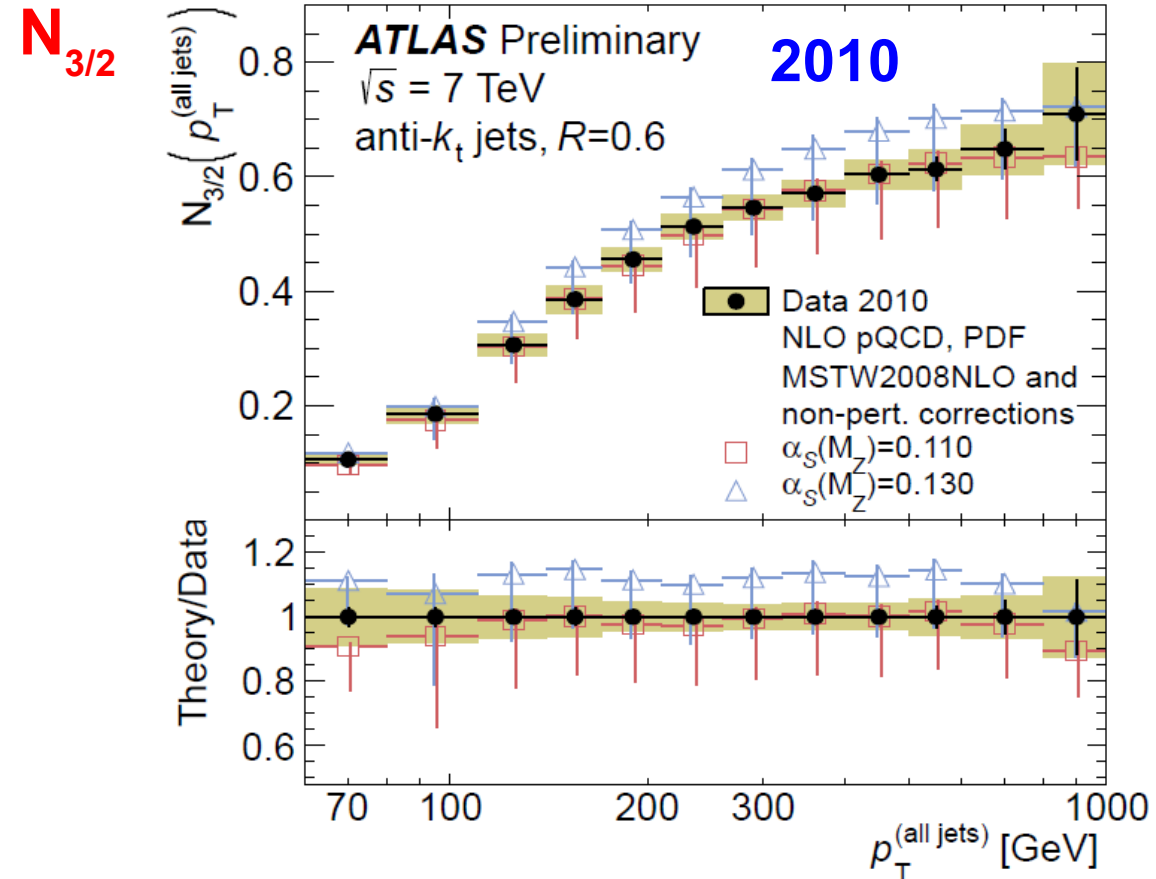
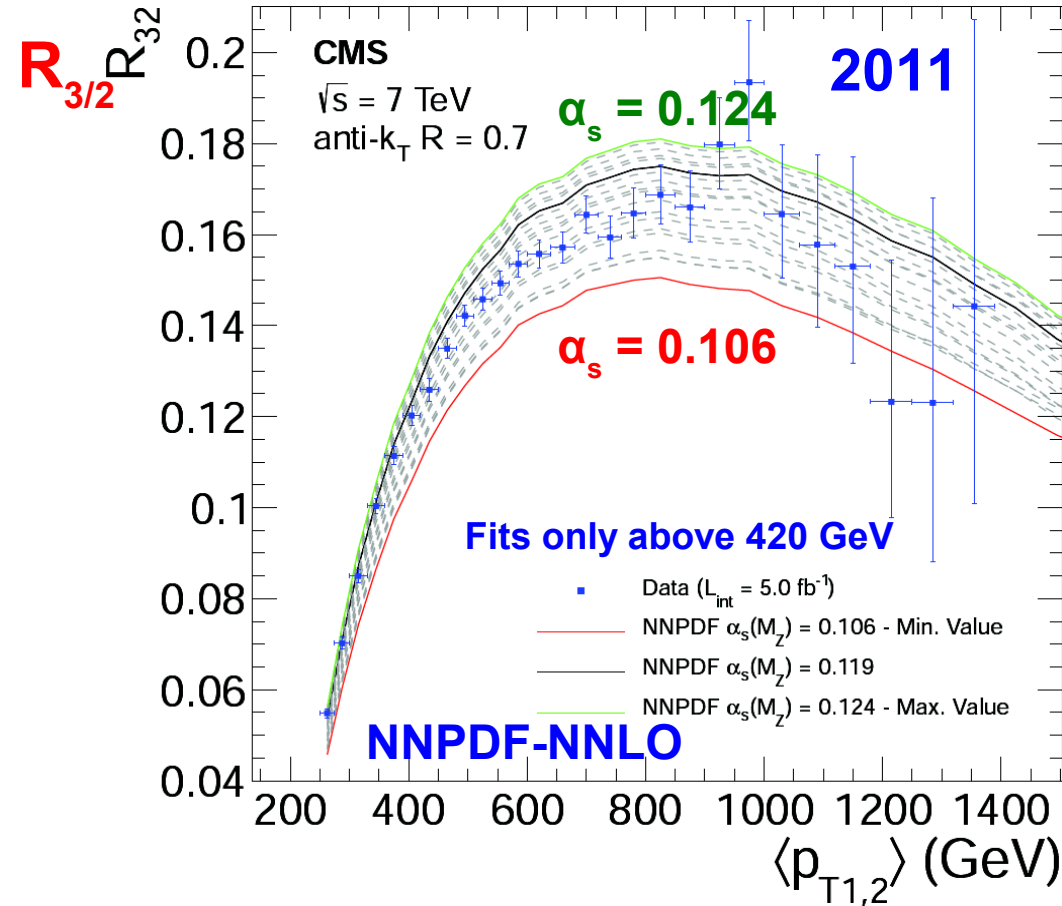
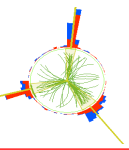
**CMS:  $R_{3/2}$**

- Ratio of inclusive 3- to inclusive 2-jet **events**
- anti-kT  $R=0.7$
- Min. jet  $p_T$ : 150 GeV
- Max. rap.:  $|y| < 2.5$
- Scale: Average dijet  $p_T$
- Data 2011, 5/fb

**ATLAS:  $N_{3/2}$**

- Ratio of inclusive 3- to inclusive 2-**jets**
- anti-kT  $R=0.6$
- Min. jet  $p_T$ : 40 GeV
- Max. rap.:  $|y| < 2.8$
- Scale: Jet  $p_T$
- Data 2010, 36/pb

# 3- to 2-Jet Ratios



Similarly described by CT10 or MSTW2008  
 Discrepancies observed with ABM11

$$\alpha_s(M_Z) = 0.1148 \pm 0.0014 \text{ (exp)} \\
 \pm 0.0018 \text{ (PDF)} \pm 0.0050 \text{ (theory)}$$

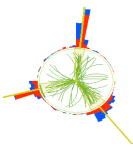
$$\alpha_s(M_Z) = 0.111 \pm 0.006 \text{ (exp)} \\
 \pm_{0.003}^{0.016} \text{ (theory)}$$

CMS, EPJC 73 (2013) 2604

**Dominated by theory uncertainty!**

ATLAS-CONF-2013-041 (2013)

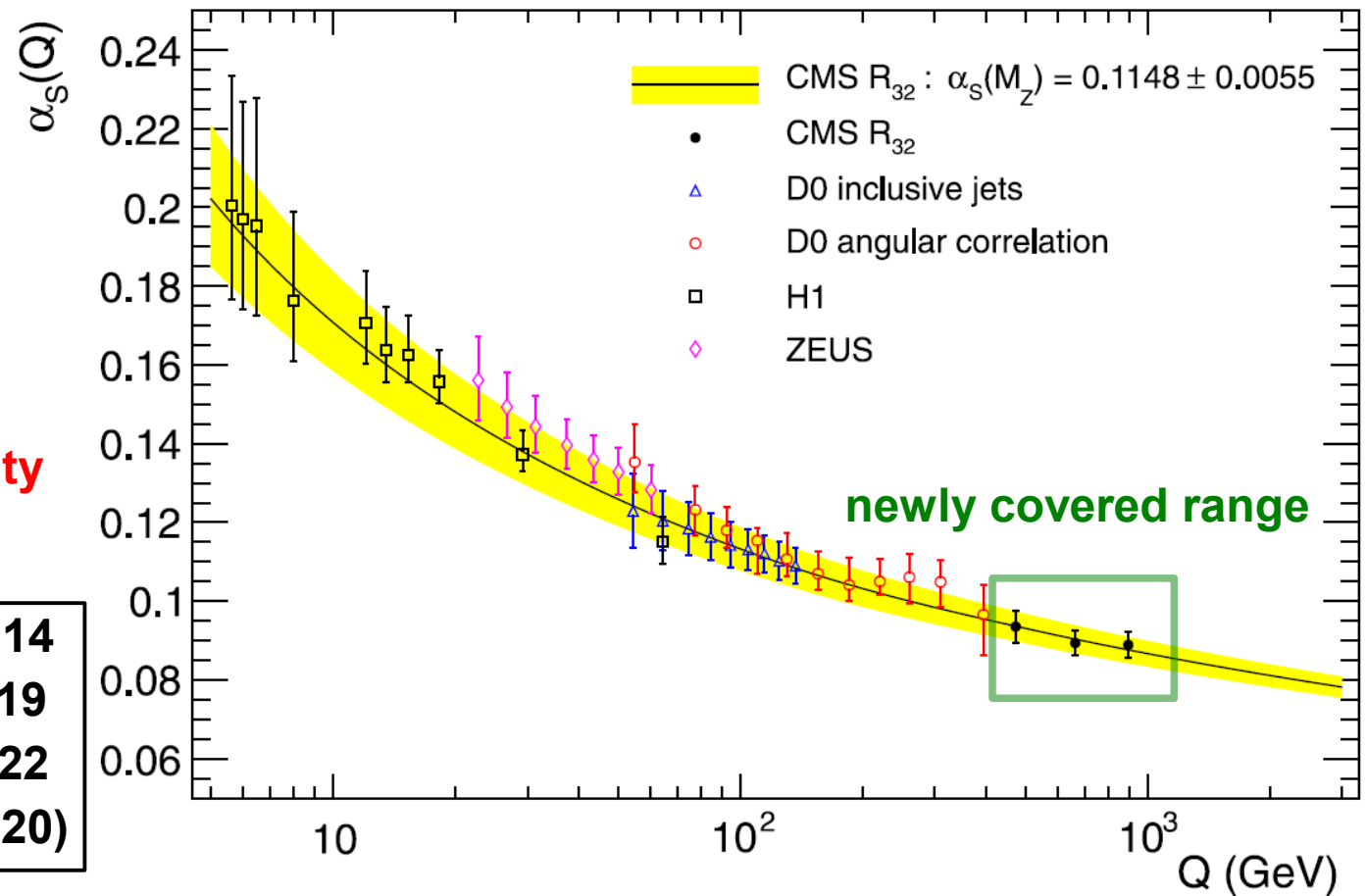
# Determination of $\alpha_s$ from $R_{3/2}$ (NLO)



CMS, EPJC 73 (2013) 2604

- Comparison to other hadron collider experiments
- Extraction also performed for three subranges in Q
- Small exp. uncertainty
- Dominated by th. uncertainty:
  - ➔ asymmetric scale uncertainty
  - ➔ PDF uncertainty

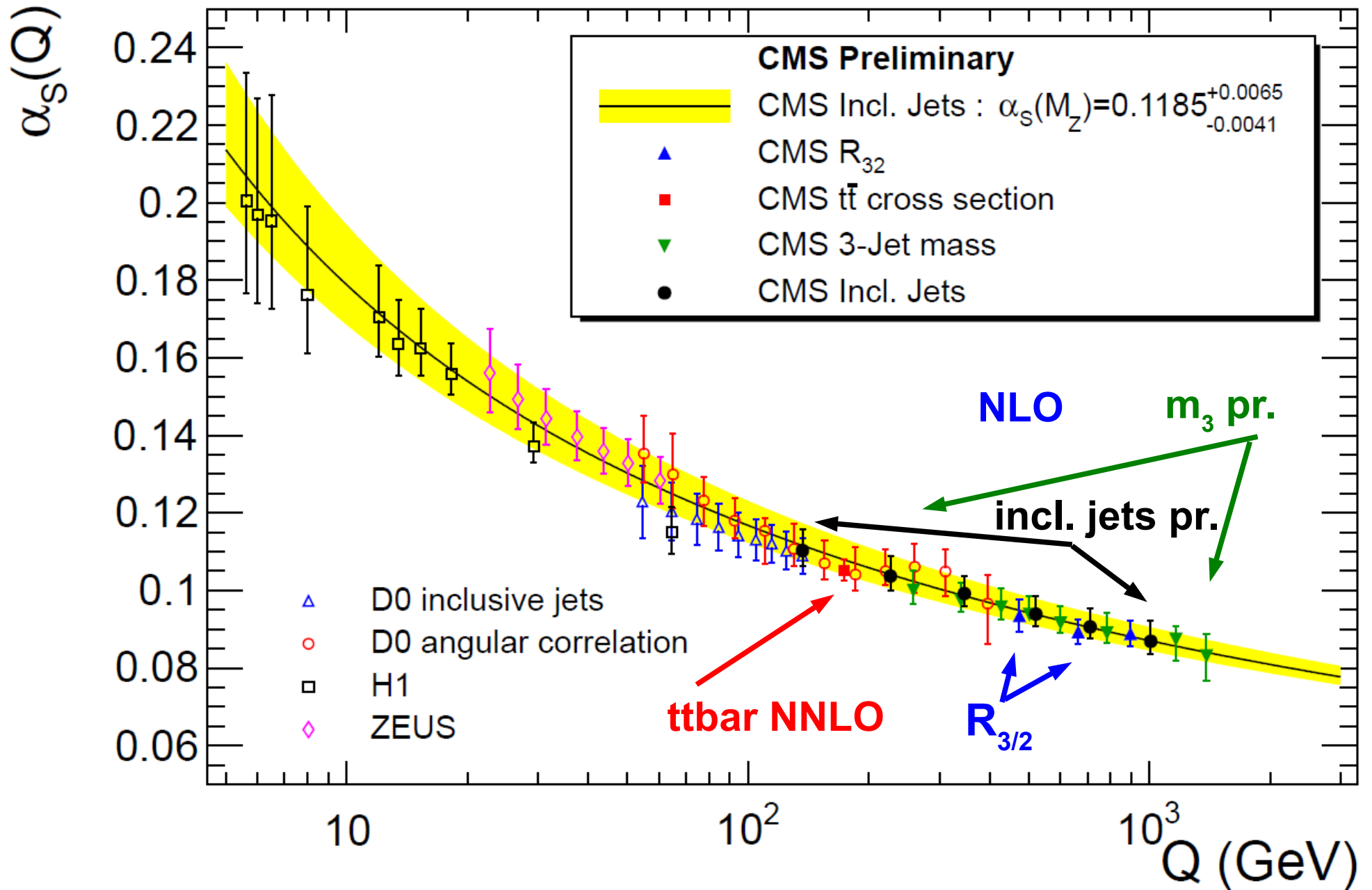
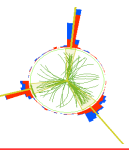
<b>NNPDF21:</b>	$\alpha_s(M_Z) = 0.1148 \pm 0.0014$
<b>CT10:</b>	$\alpha_s(M_Z) = 0.1135 \pm 0.0019$
<b>MSTW2008:</b>	$\alpha_s(M_Z) = 0.1141 \pm 0.0022$
<b>(ABM11:</b>	$\alpha_s(M_Z) = 0.1214 \pm 0.0020)$



**PDF uncertainty:** Repeat fit for each NNPDF replica → get estimators for  $\mu$  and  $\sigma$   
**Scale uncertainty:** Repeat fit for six variations of  $(\mu_r, \mu_f)$  → get maximal deviation

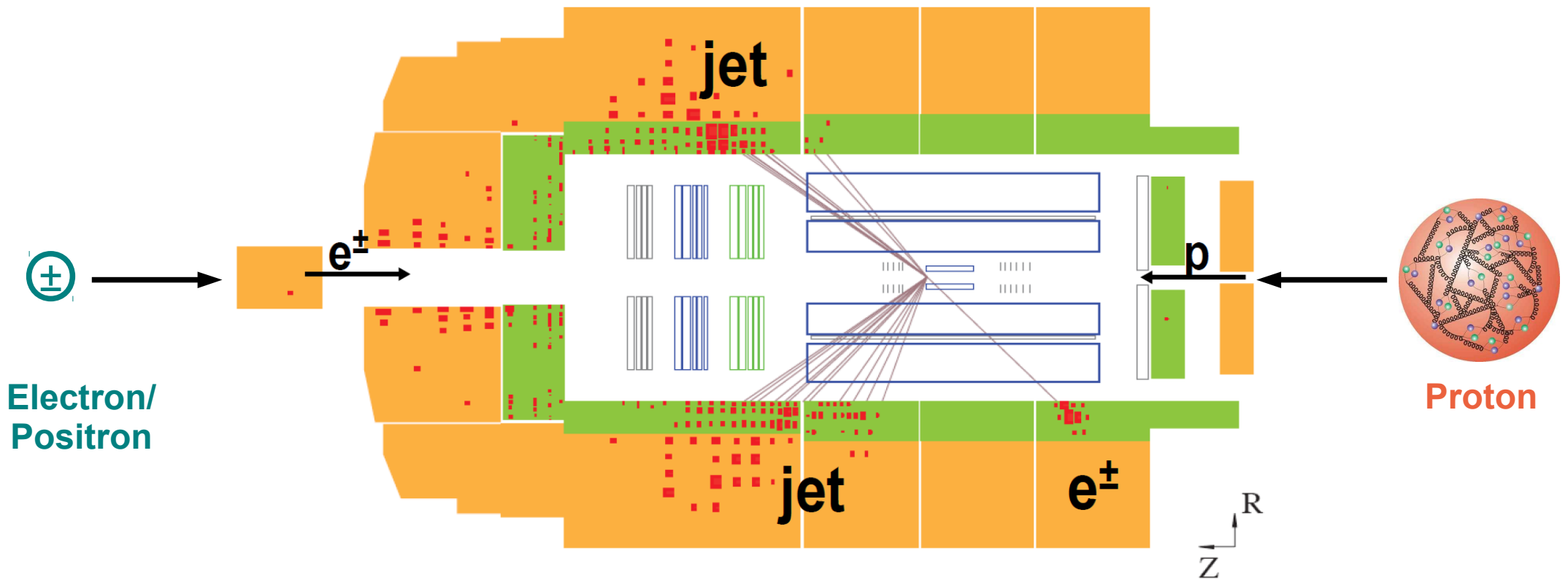
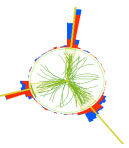
$$\alpha_s(M_Z) = 0.1148 \pm 0.0014 (\text{exp}) \pm 0.0018 (\text{PDF}) \pm 0.0050 (\text{theory})$$

# CMS $\alpha_s$ Summary



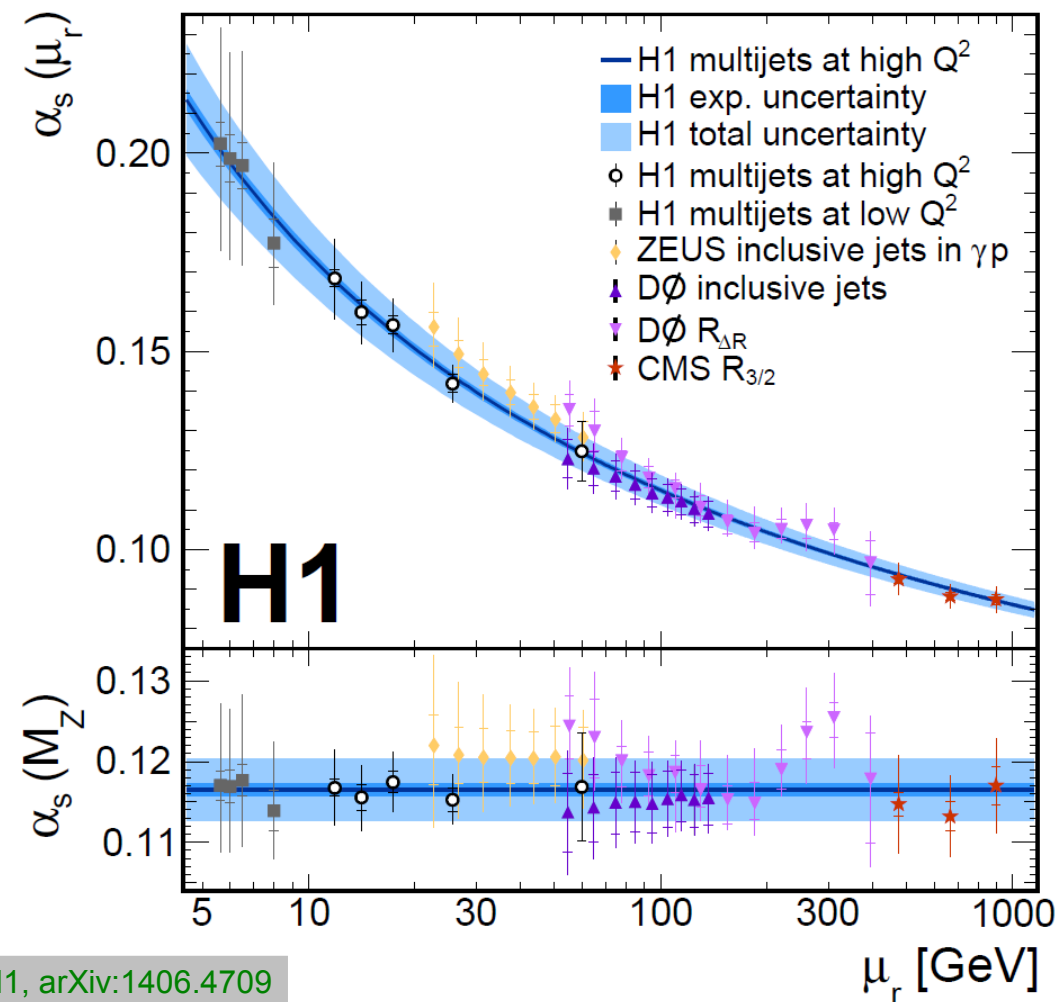
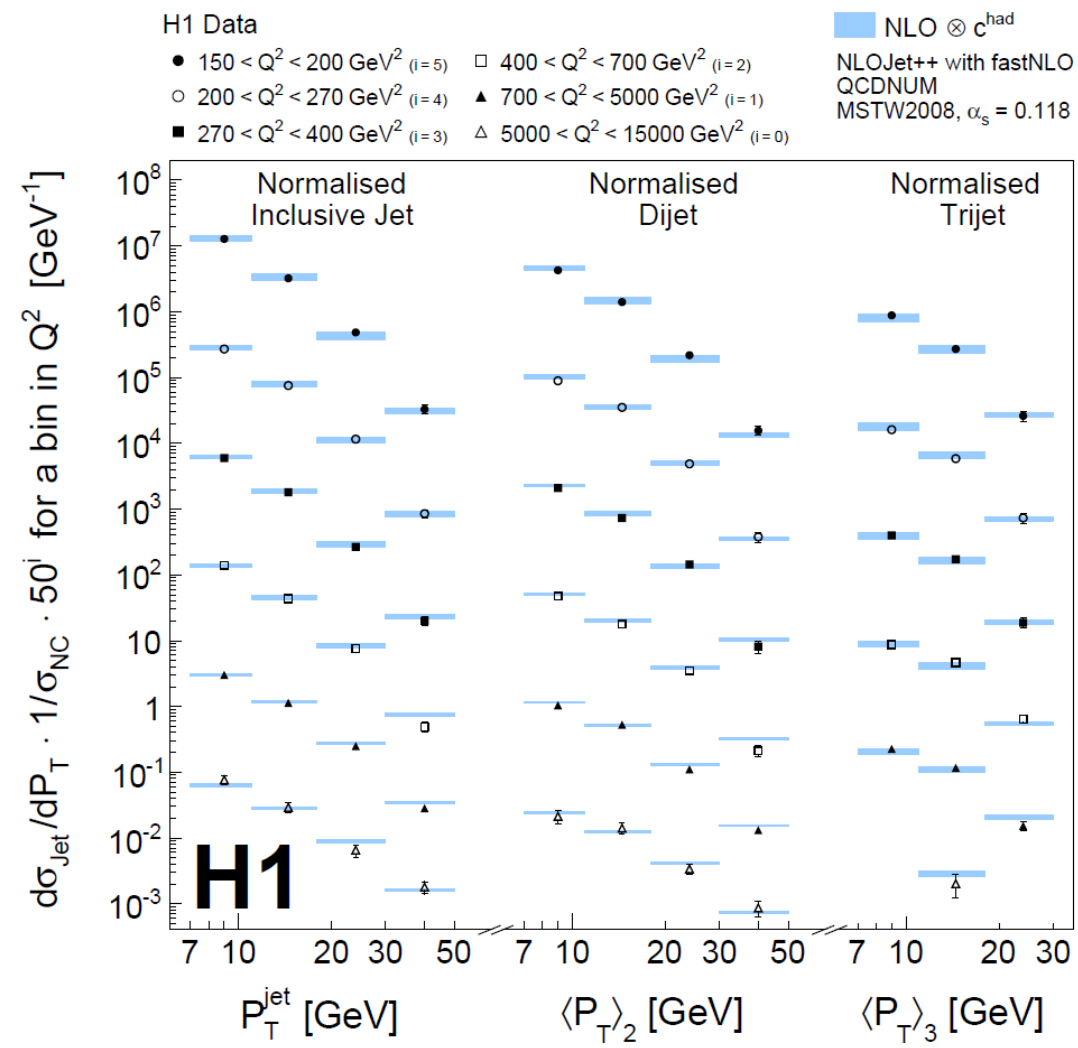
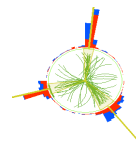


# Normalized Multi-Jets and $\alpha_s$





# Normalized Multi-Jets in DIS



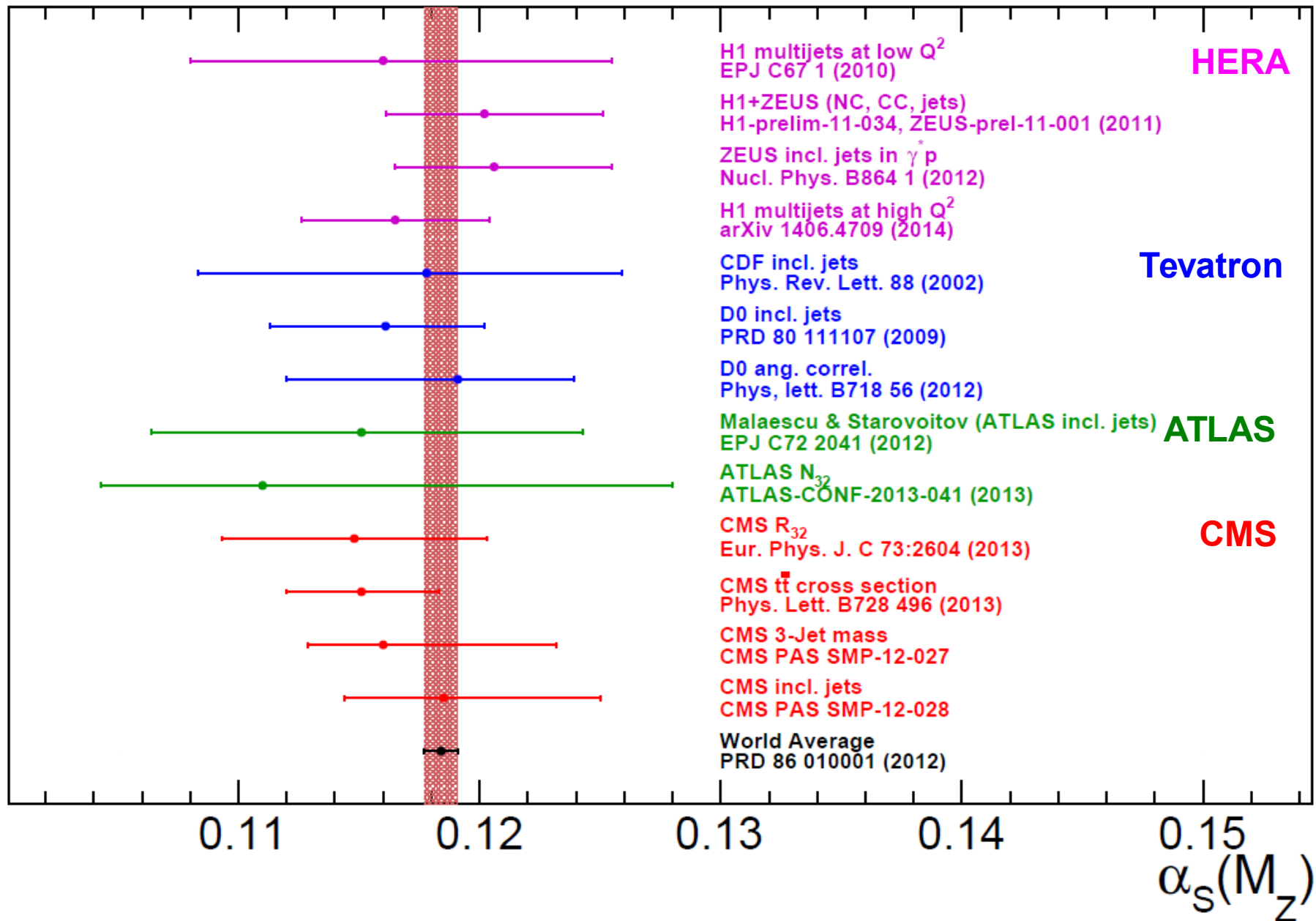
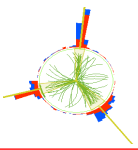
$$\alpha_s(M_Z) = 0.1165 \pm \boxed{0.0008(\text{exp.})} \pm \boxed{0.0038(\text{theor.})}$$

**NLO: Dominated by theory uncertainty!**

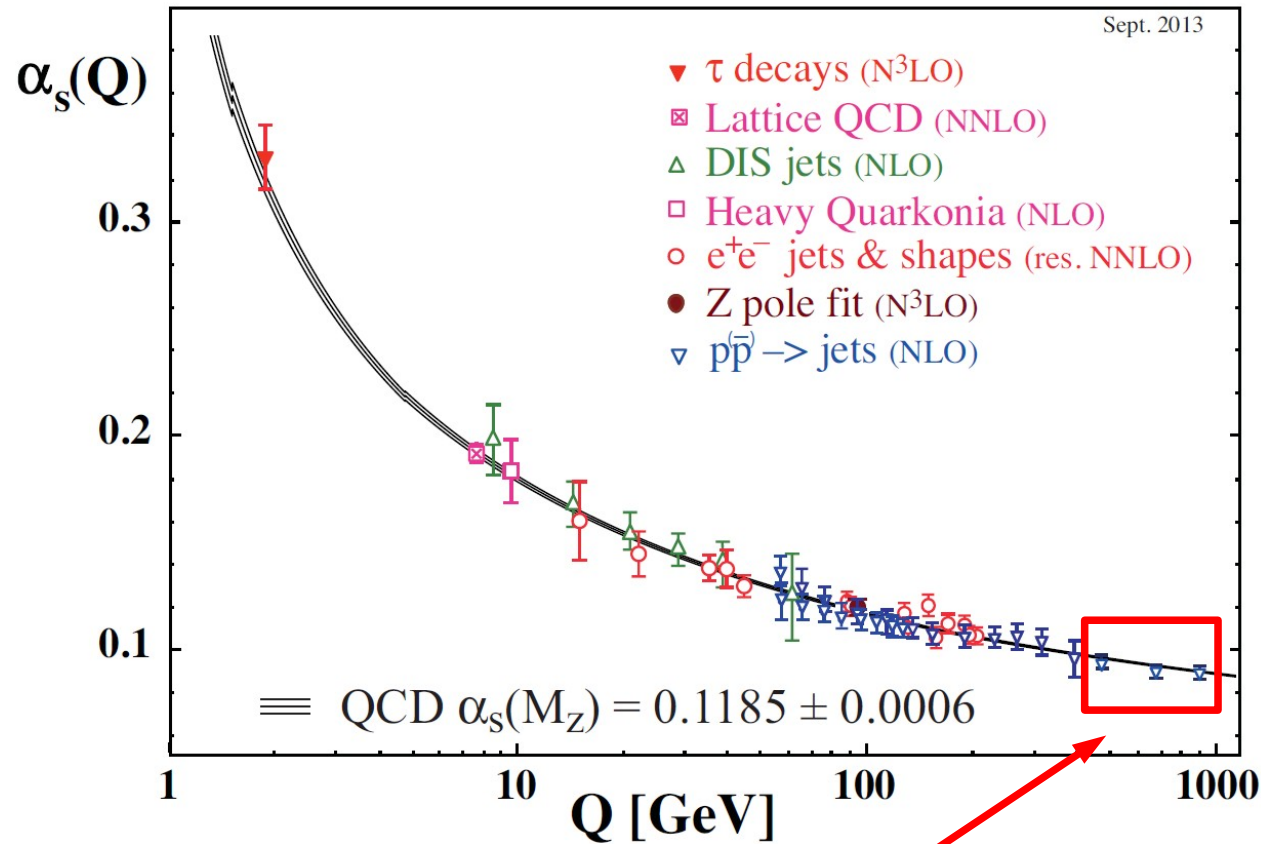
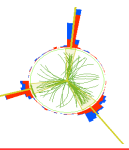
## Jet phase space:

- Jets incl.:  $-1.0 < \eta_{\text{lab}} < 2.5$
- $7 < p_T < 50 \text{ GeV}$
- 2-,3-Jets:  $5 < p_T < 50 \text{ GeV}$

# Hadron Collider Summary

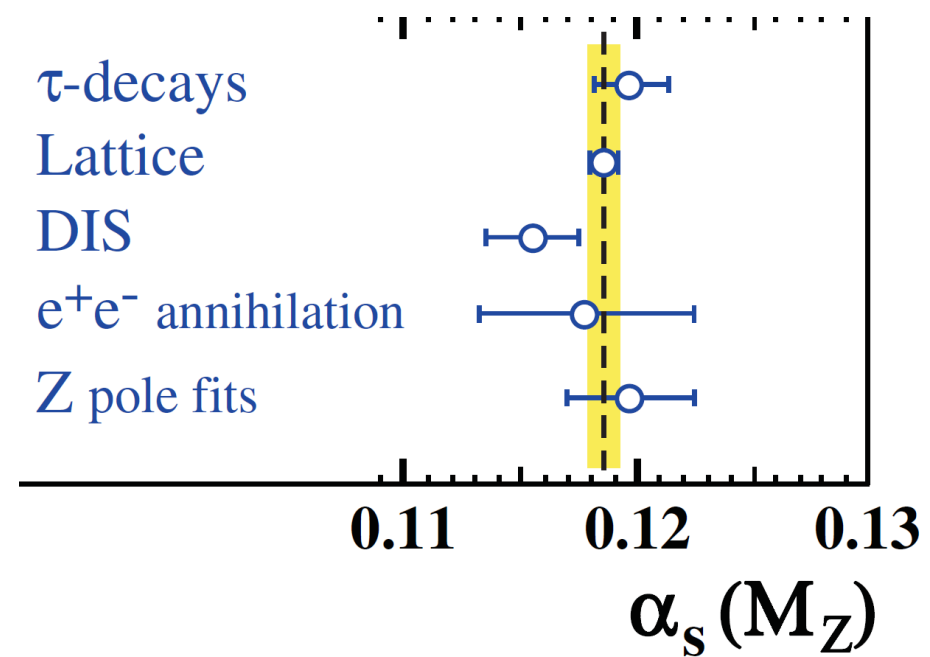


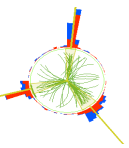
# PDG $\alpha_s$ Summary



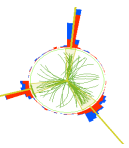
**CMS data, but not in average since only NLO theory!**

$$\alpha_s(M_Z) = 0.1185 \pm 0.0006$$





- Still new precise measurements from HERA (and Tevatron)!
- Huge new phase space opened up at 7-8 TeV LHC ...  
13 TeV will be another very interesting step, not only for searches
- Data quality makes jet measurements **PRECISION PHYSICS**  
→ better determine gluon PDF, strong coupling, and ...  $gg \rightarrow H$
- Theory definitely entered regime of NLO as Standard
- More precise theory required (NNLO, EW) ...
- ... and under heavy development → will be very welcome!
- Mentioned only briefly other exciting topics like jet substructure, or not at all, gap fractions,  $W$ +jets,  $Z$ +jets
- New ideas for analyses are explored

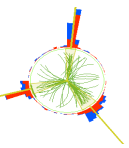


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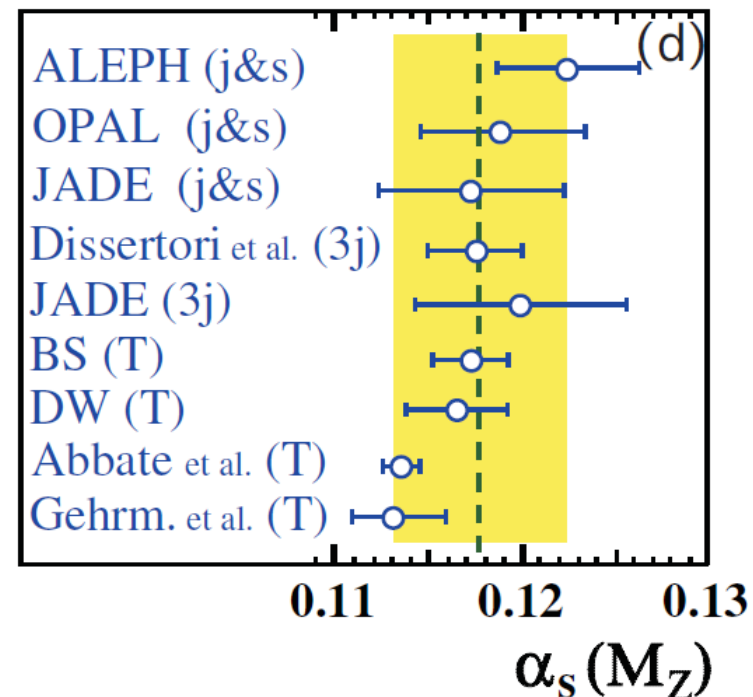
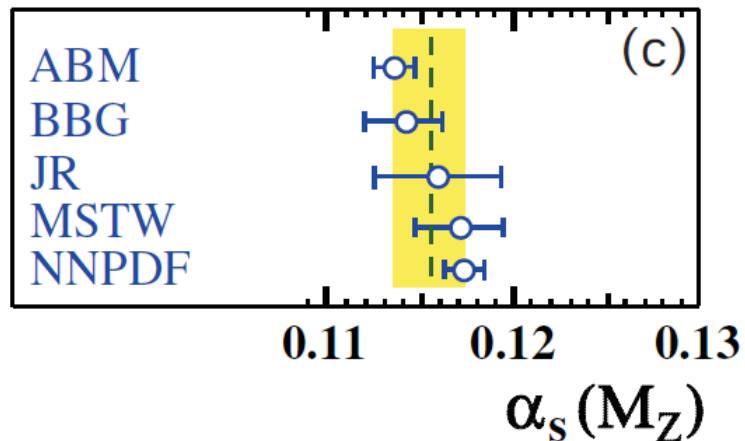
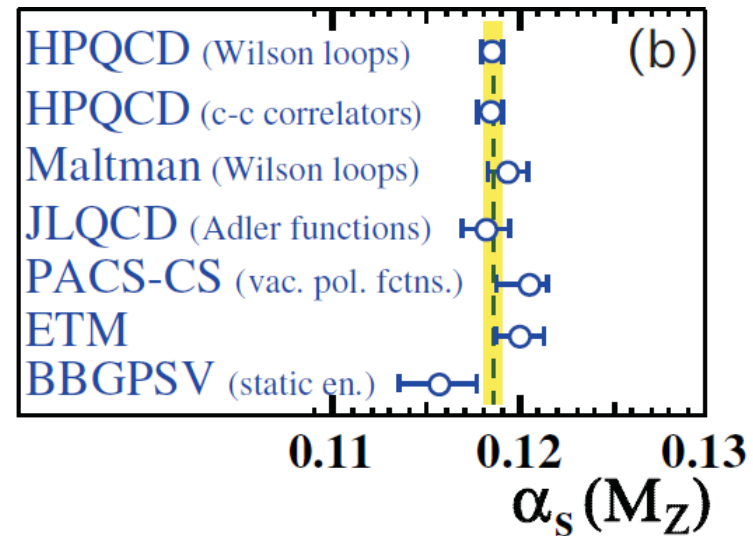
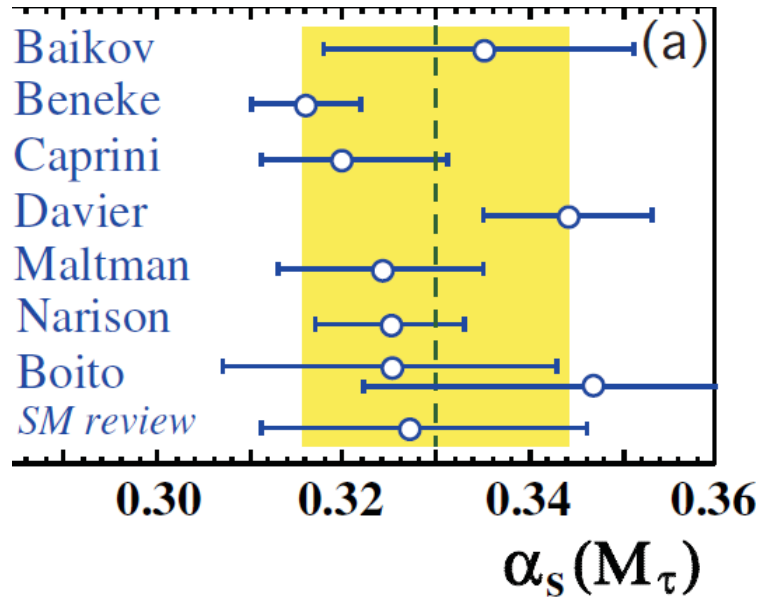
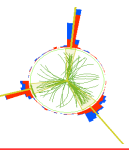
**Thank you for your attention!**



# *Backup Slides*

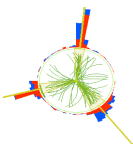


# PDG Pre-averages





# Table of PDF sets with $\alpha_s$ series

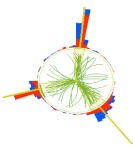


Base set	Reference(s)	Evol. order	$N_f$	$\alpha_s(M_Z)$	$\alpha_s(M_Z)$ variations
ABM11	[24]	NLO	5	0.1180	0.110–0.130
ABM11	[24]	NNLO	5	0.1134	0.104–0.120
CT10	[25]	NLO	$\leq 5$	0.1180	0.112–0.127
CT10	[25]	NNLO	$\leq 5$	0.1180	0.110–0.130
HERAPDF1.5	[26]	NLO	$\leq 5$	0.1176	0.114–0.122
HERAPDF1.5	[26]	NNLO	$\leq 5$	0.1176	0.114–0.122
MSTW2008	[27, 28]	NLO	$\leq 5$	0.1202	0.110–0.130
MSTW2008	[27, 28]	NNLO	$\leq 5$	0.1171	0.107–0.127
NNPDF2.1	[29]	NLO	$\leq 6$	0.1190	0.114–0.124
NNPDF2.1	[29]	NNLO	$\leq 6$	0.1190	0.114–0.124





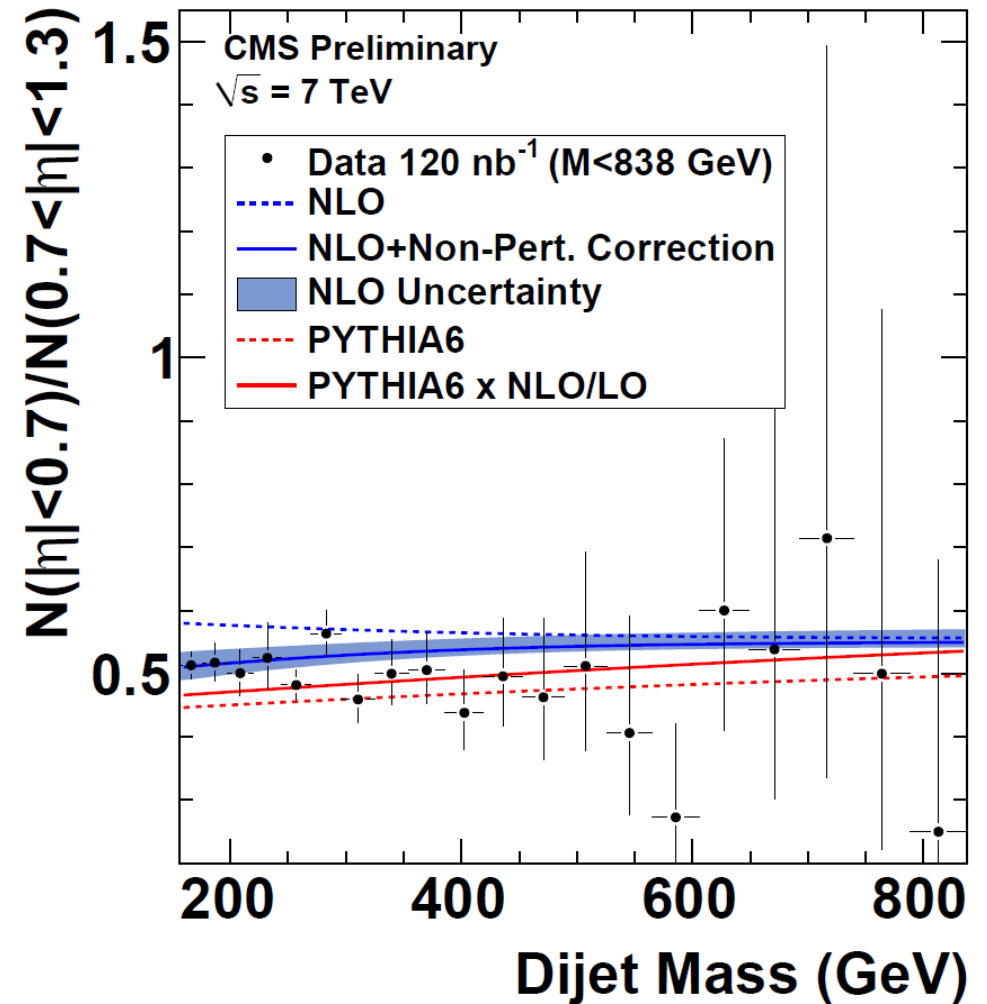
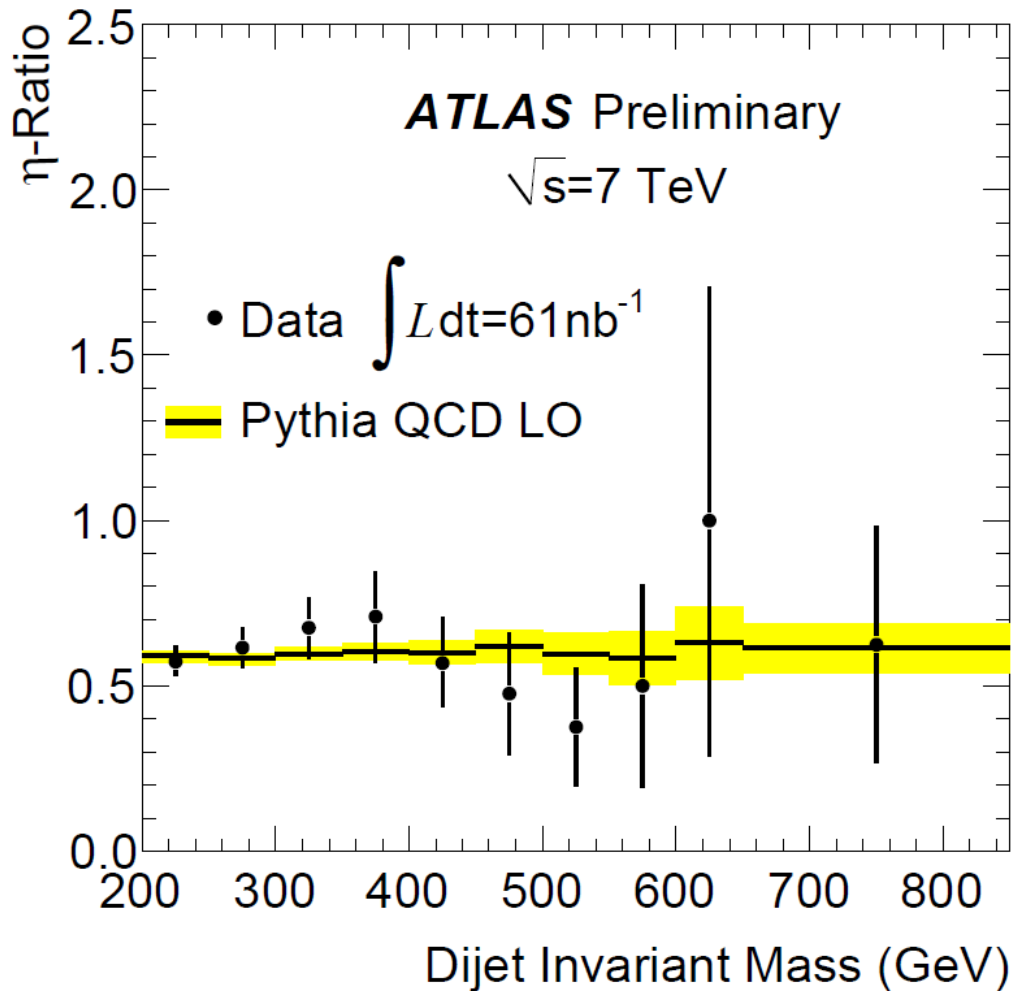
# Dijet Centrality Ratio



Outdated figures, anyway no deviations from QCD observed!

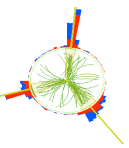
$$\eta\text{-ratio} = \frac{N(|\eta_{1,2}| < 0.5)}{N(0.5 < |\eta_{1,2}| < 1)}$$

$$R = \frac{N(|\eta| < 0.7)}{N(0.7 < |\eta| < 1.3)}$$





# Event Shapes



## Originally:

### Event Shapes in $e^+e^-$ (and ep)

Played a key role in the discovery of the gluon at DESY in 1978!

Old but still-used definition since collinear and infrared safe:

Thrust S. Brandt et al., PL12 (1964),  
E. Farhi, PRL39 (1977).

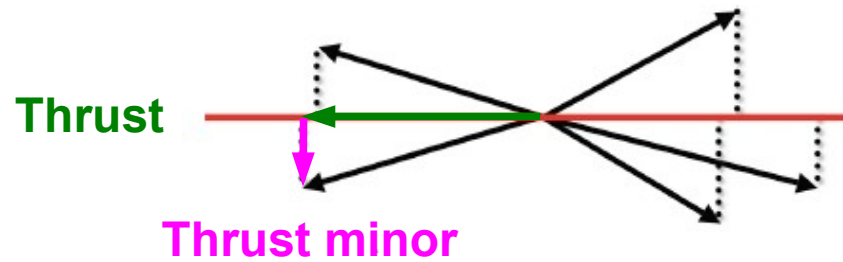
### At LHC: Transverse global thrust

→ In praxis, need to restrict rapidity range:  $|\eta| < \eta_{\max}$  →

### Transverse central thrust

## Definition:

### Transverse global thrust



$$T_{\perp,g} = \max_{\vec{n}_T} \frac{\sum_i |\vec{p}_{\perp,i} \cdot \vec{n}_T|}{\sum_i p_{\perp,i}}$$

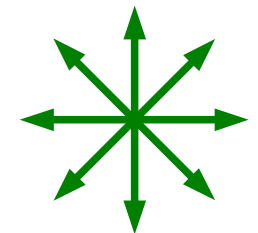
### Redefine to get

$$\tau_{\perp,g} \equiv 1 - T_{\perp,g}$$



linear ~ dijet

$$\tau_{\perp,g} \rightarrow 0$$

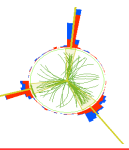


spherical ~ multijet

$$\tau_{\perp,g} \rightarrow 1 - 2/\pi$$

See also A. Banfi et al., JHEP06, 2010

# Central Transverse Thrust



Basic description by MC ok

Some deviations visible

→ good for tuning!

Great tools in e+e-, known to NNLO+NLLA resummation

→ precise determination of  $\alpha_s$

Dissertori et al, JHEP0908 (2009).

Also used successfully in ep

In hh collisions:

- only NLO so far

- in praxis, need to restrict rapidity

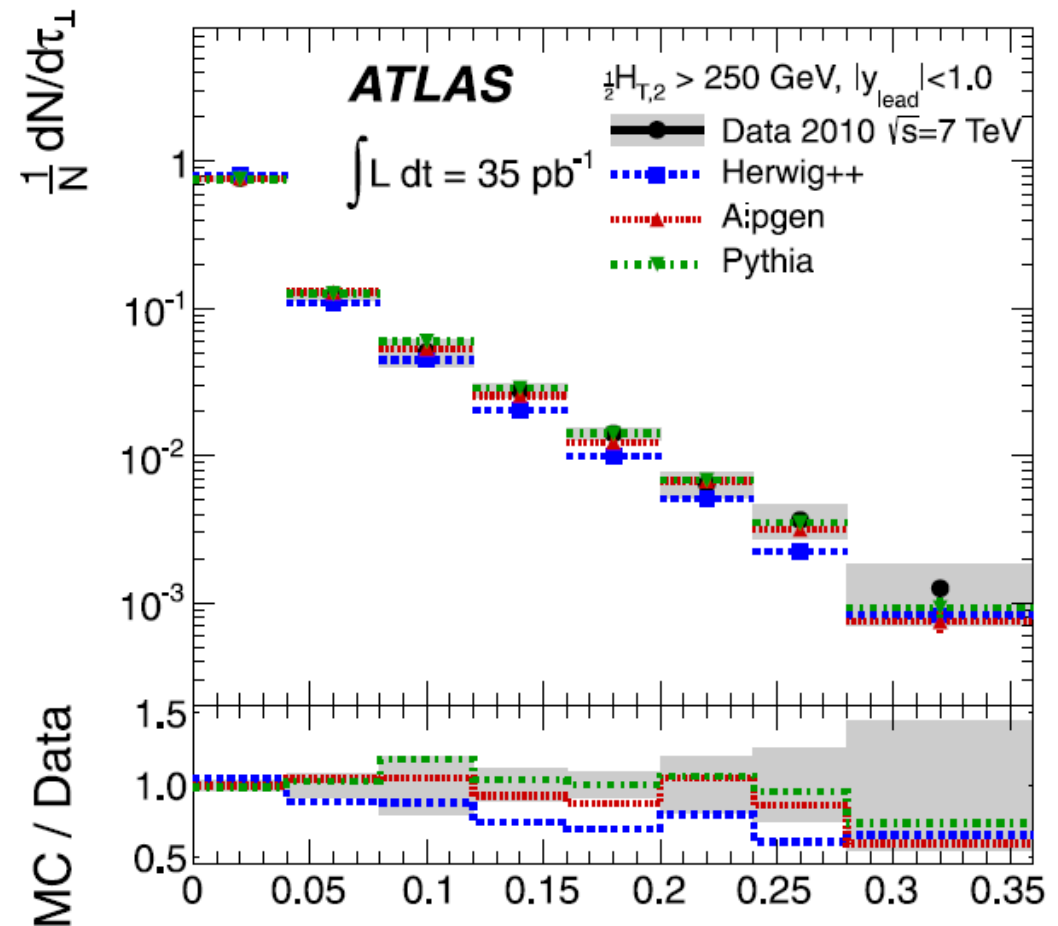
range:  $|\eta| < \eta_{\max}$

→ central transverse thrust

→ spoils resummation

Banfi et al., JHEP06 (2010).

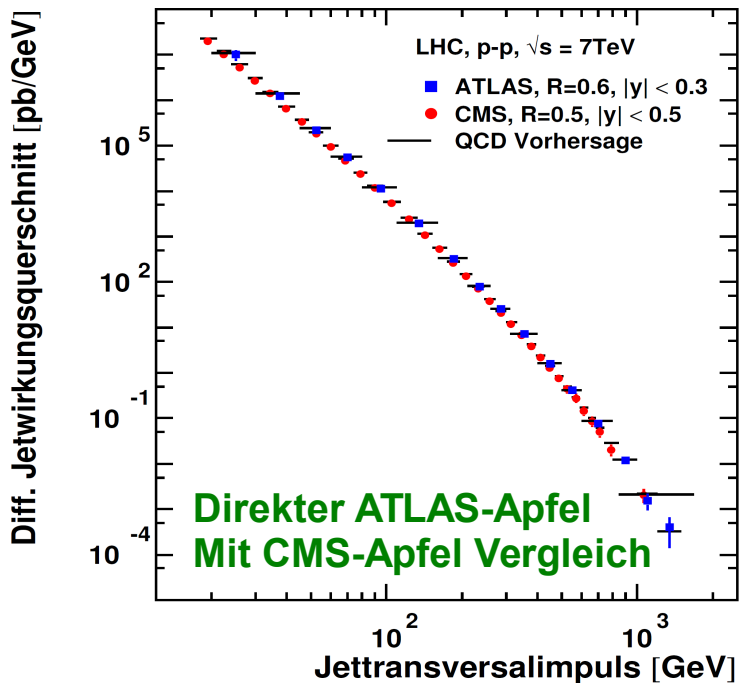
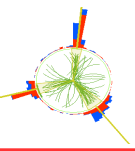
$$\tau_{\perp,C} \equiv 1 - \max_{\vec{n}_T} \frac{\sum_i |\vec{p}_{\perp,i} \cdot \vec{n}_T|}{\sum_i p_{\perp,i}}$$



ATLAS, EPJC72, 2012

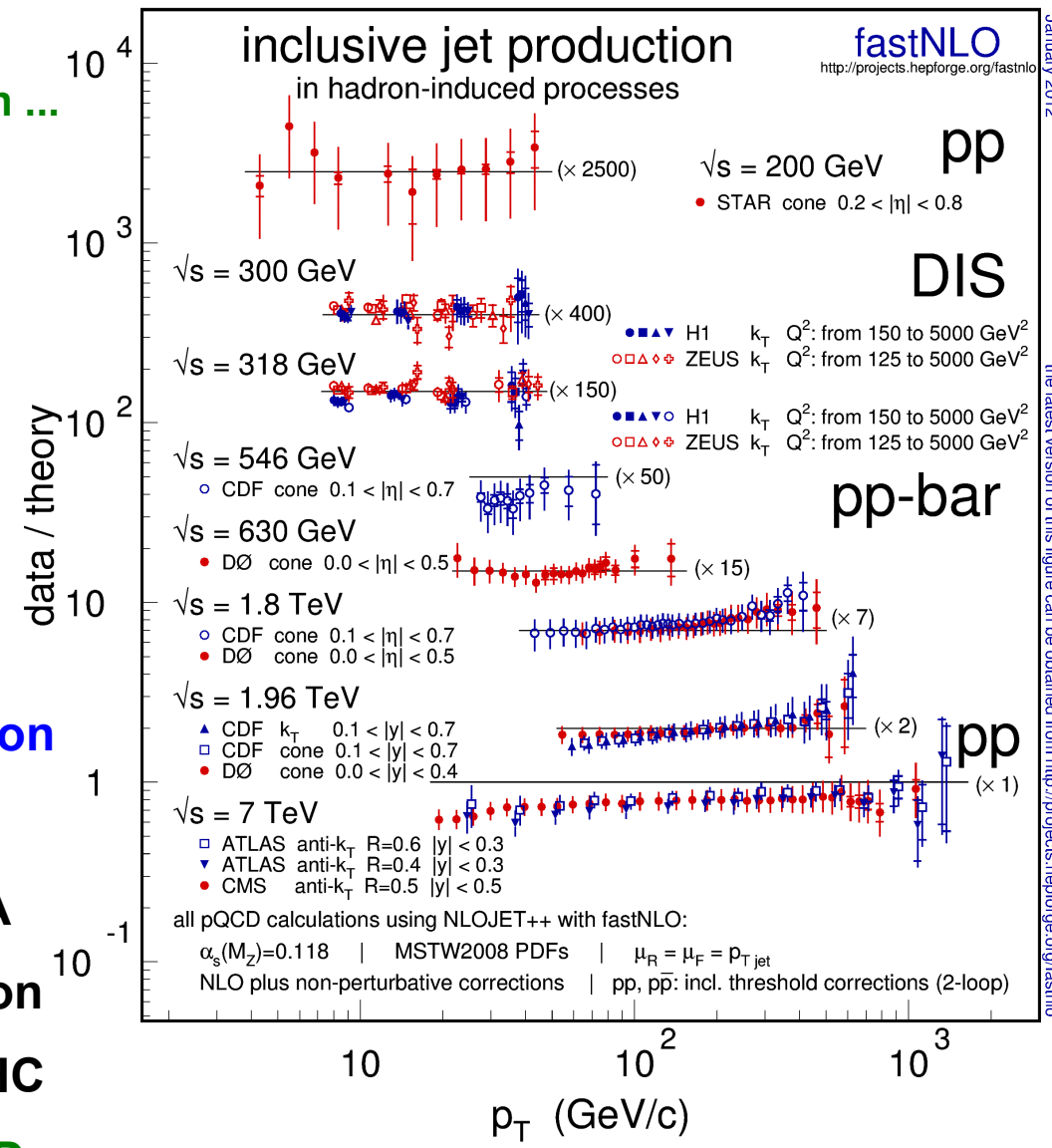
$\tau_{\perp} = 1 - T_{\perp}$

# Jets Daten / Theorie



**ATLAS und CMS  
Stimmen überein ...  
auf log. Skala :-)**

- **Vergleich von Jet-Daten von**
- ➔ **STAR am RHIC**
- ➔ **H1 und ZEUS bei HERA**
- ➔ **CDF und D0 am Tevatron**
- ➔ **ATLAS und CMS am LHC**
- **Kompatibel mit NLO pQCD**



January 2012  
the latest version of this figure can be obtained from <http://projects.hepforge.org/fastnlo>