

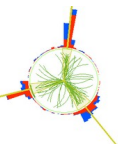
## $\alpha_s$ determination at the LHC

**K. Rabbertz**





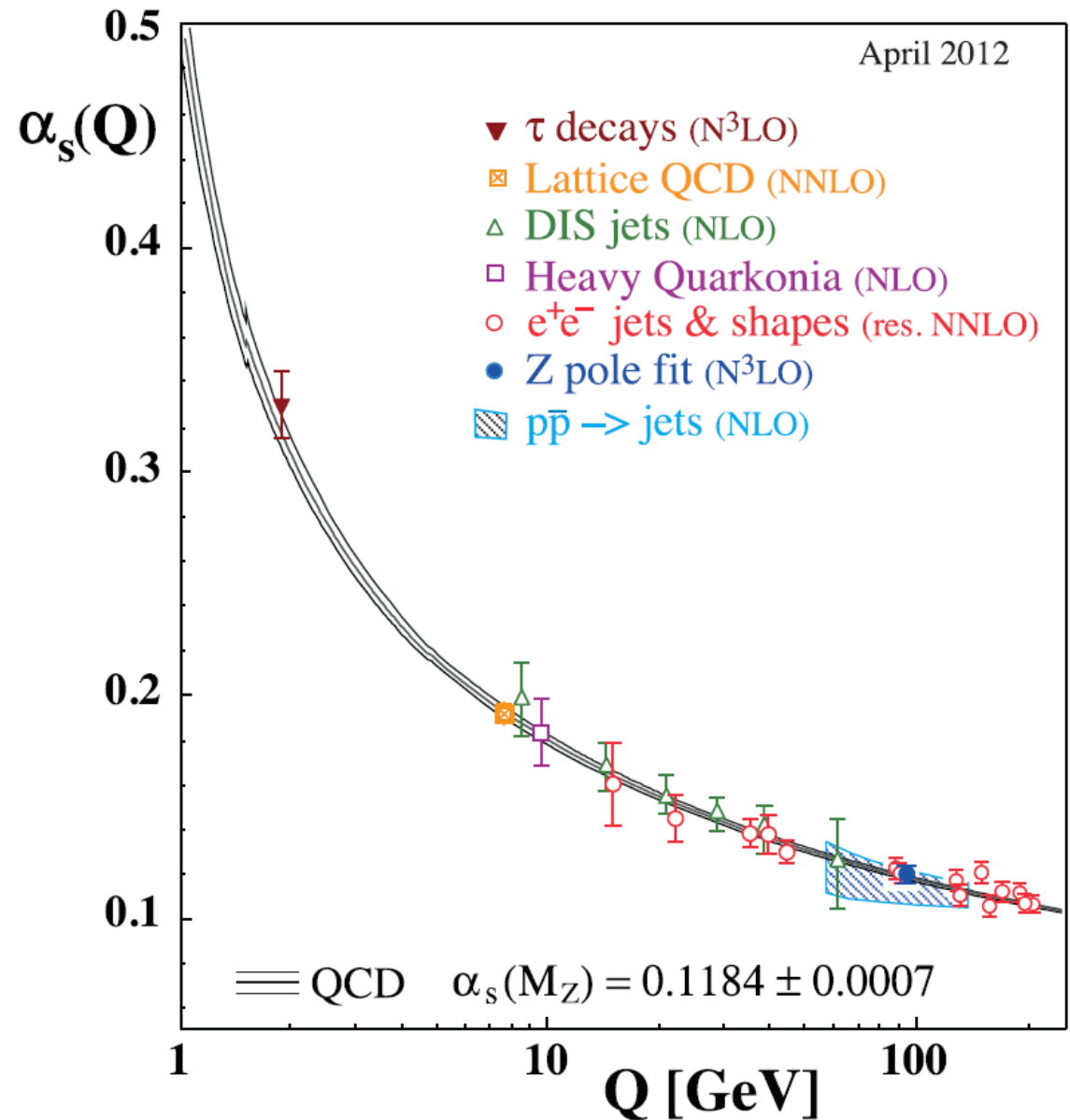
# Outline



- Introduction
- Jet-like measurements
  - + Cross sections
  - + Ratios
  - + Normalised distributions
- top-quark pair production
- W/Z bosons
- Summary & outlook

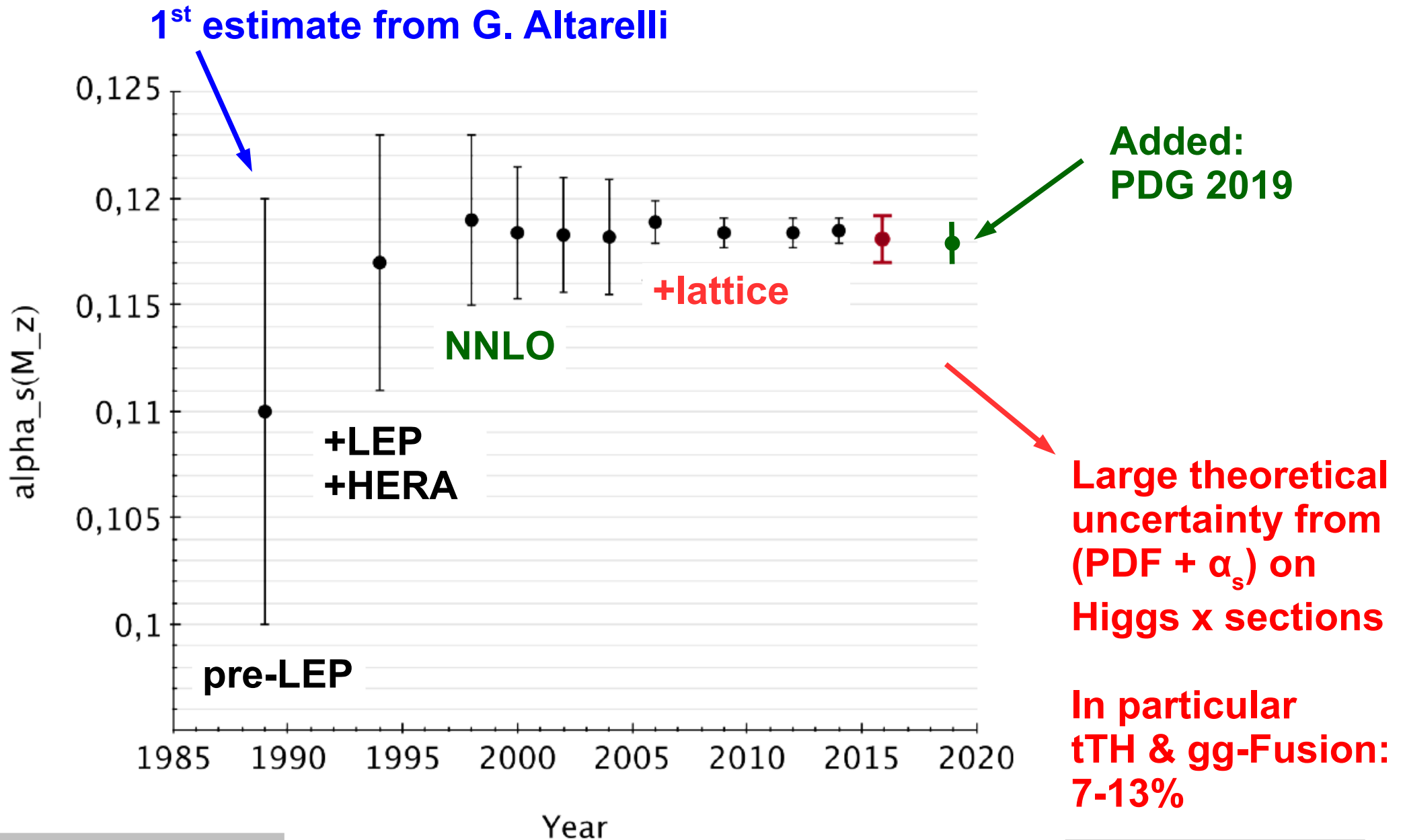
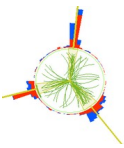
2012: No LHC results yet

PDG2012





# $\alpha_s(M_Z)$ world average versus time

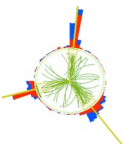


S. Bethke, arXiv:1907.01435.

CERN YR, LHC Higgs xs WG.

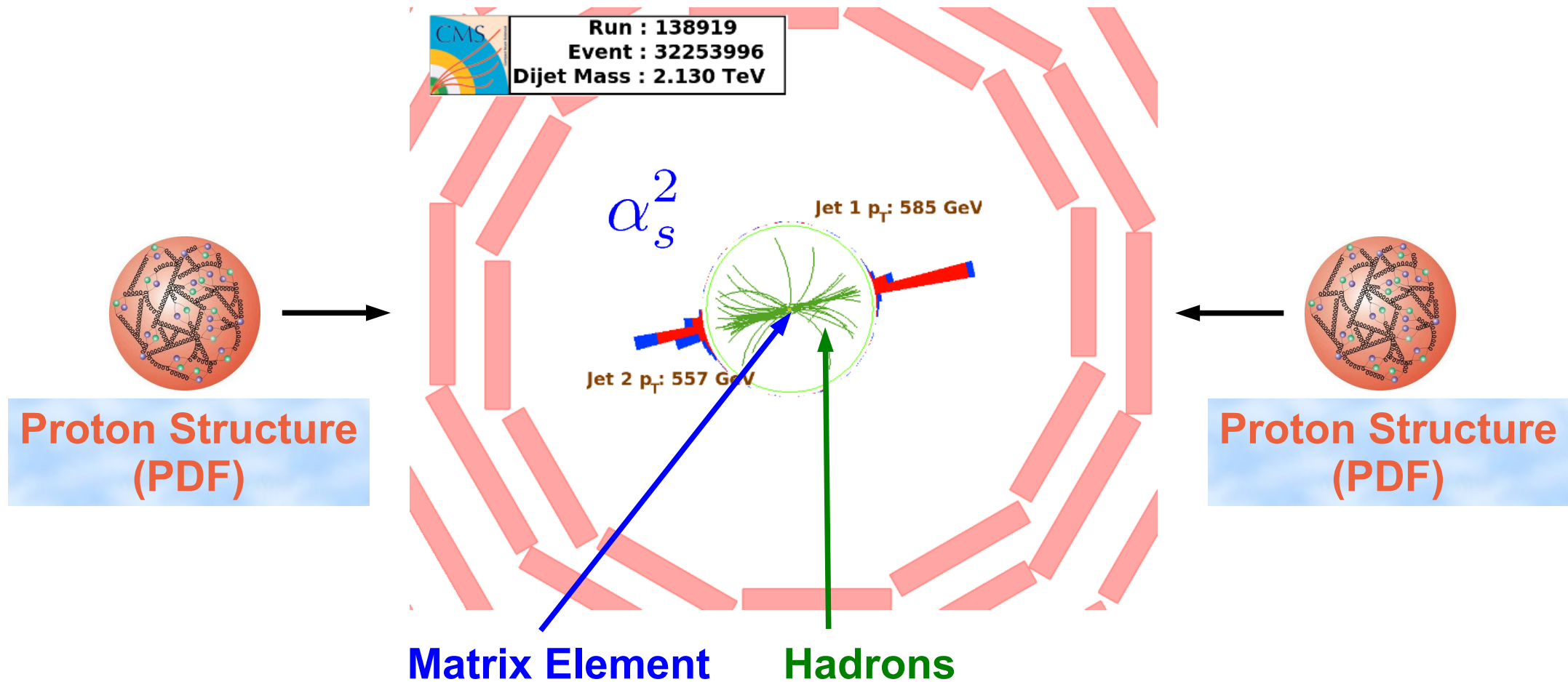


# Jets at the LHC



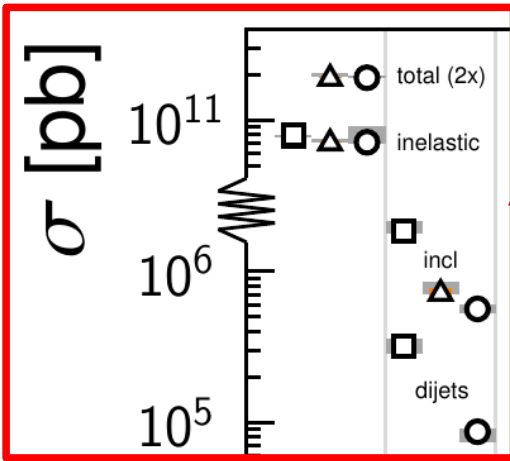
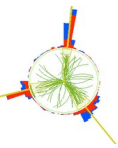
## Abundant production of jets:

- Jets at hadron colliders provide the largest dynamic range ever for  $\alpha_s(Q^2)$
- Plus insights into high- $p_T$  QCD, the proton structure, non-perturbative and electroweak effects at high  $Q$



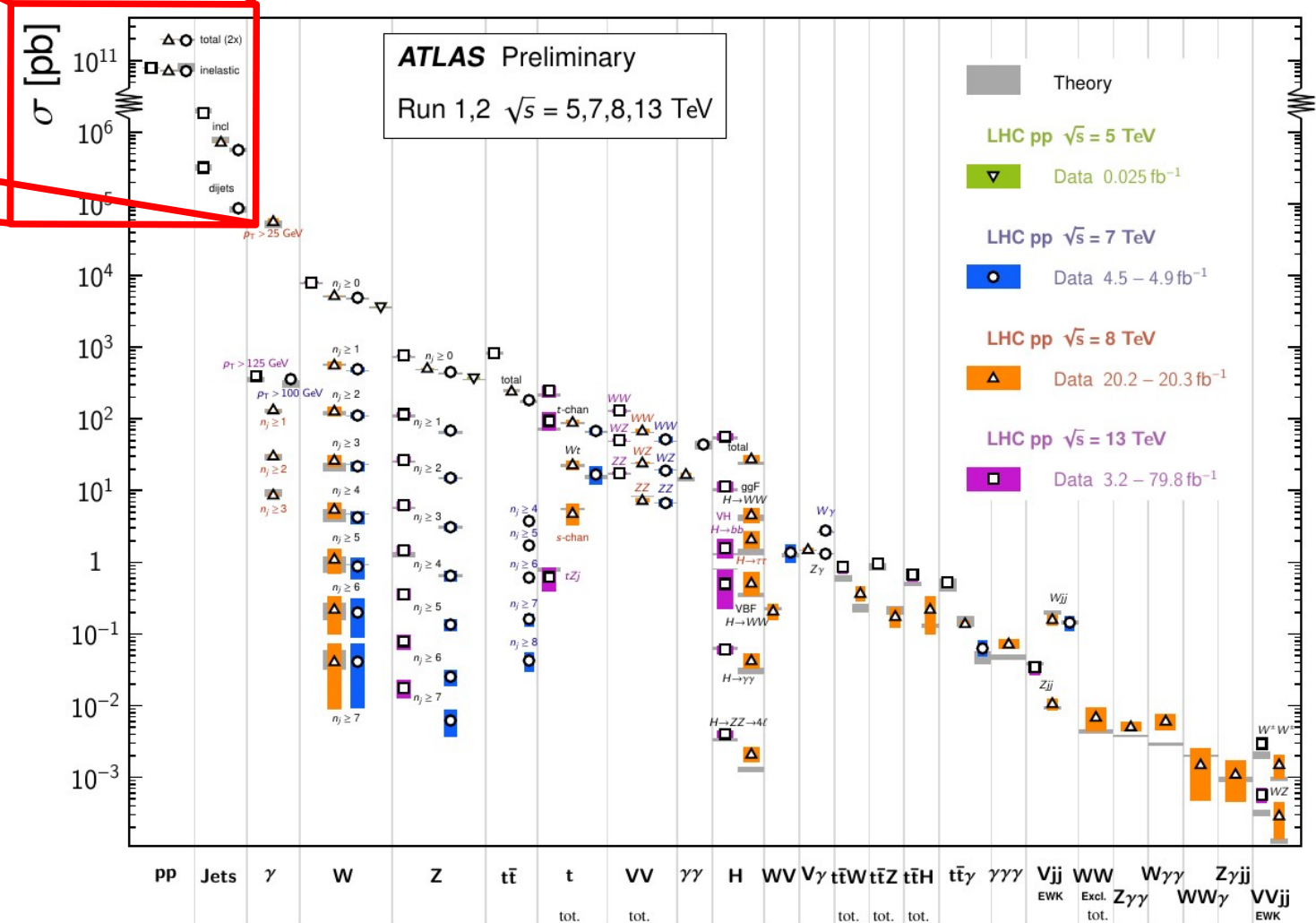


# Jets at the LHC



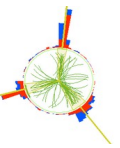
## Standard Model Production Cross Section Measurements

Status: November 2019





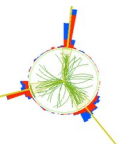
# *Jet cross sections $\sim \alpha_s^2$*



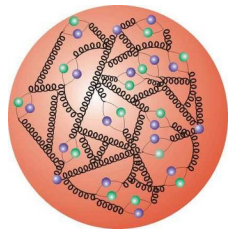
- **Determination of  $\alpha_s(M_Z)$  in single-parameter fit**
- **Test consistency of running of  $\alpha_s(Q)$**
- **Multi-parameter fit of  $\alpha_s(M_Z)$  & PDFs**



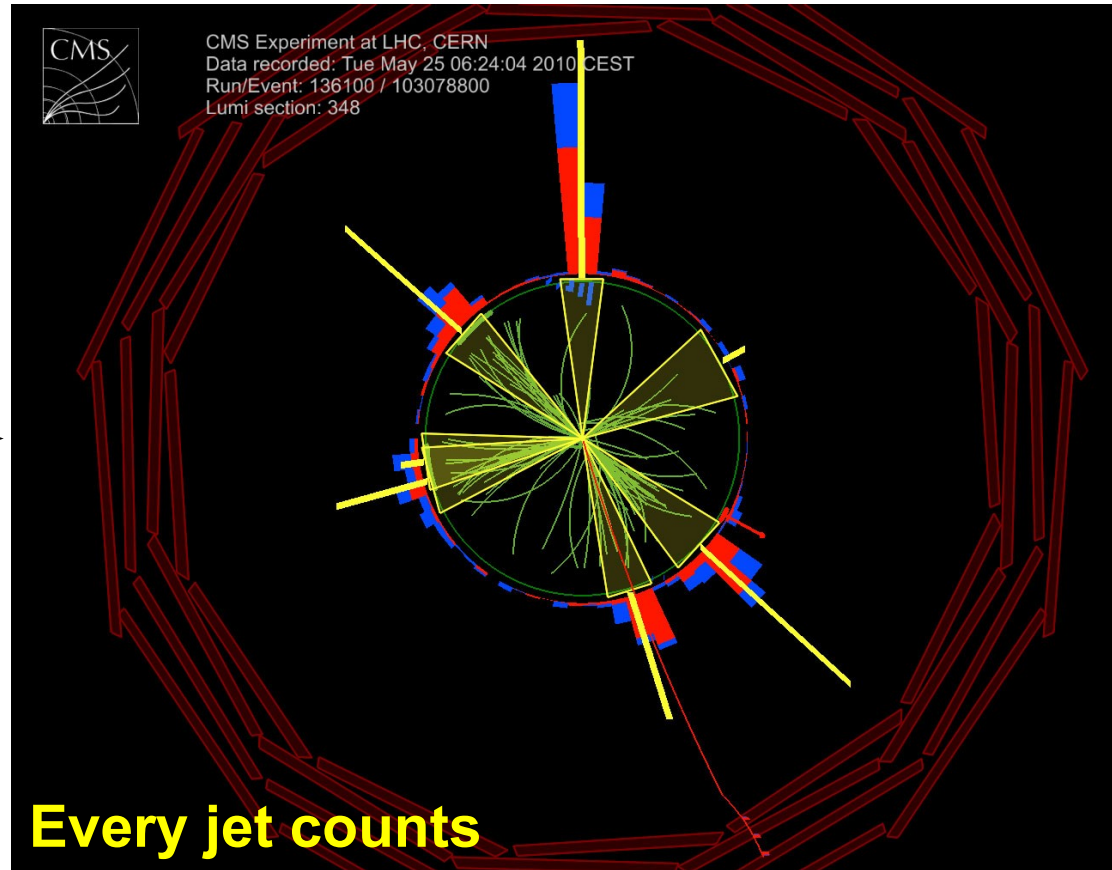
# All inclusive



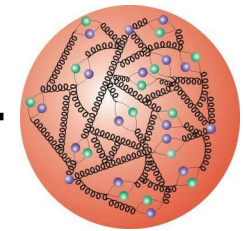
## Large transverse momenta



Proton



Every jet counts



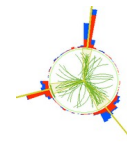
Proton

### Relevant ATLAS & CMS measurements:

**ATLAS:**  
 EPJC 73 (2013) 2509; JHEP 02 (2015) 153; JHEP 09 (2017) 020; JHEP 05 (2018) 195.  
**CMS:**  
 PRD 87 (2013) 112002; PRD 90 (2014) 072006; EPJC 75 (2015) 288;  
 EPJC 76 (2016) 265; EPJC 76 (2016) 451; JHEP 03 (2017) 156.



# Inclusive jets: cross section

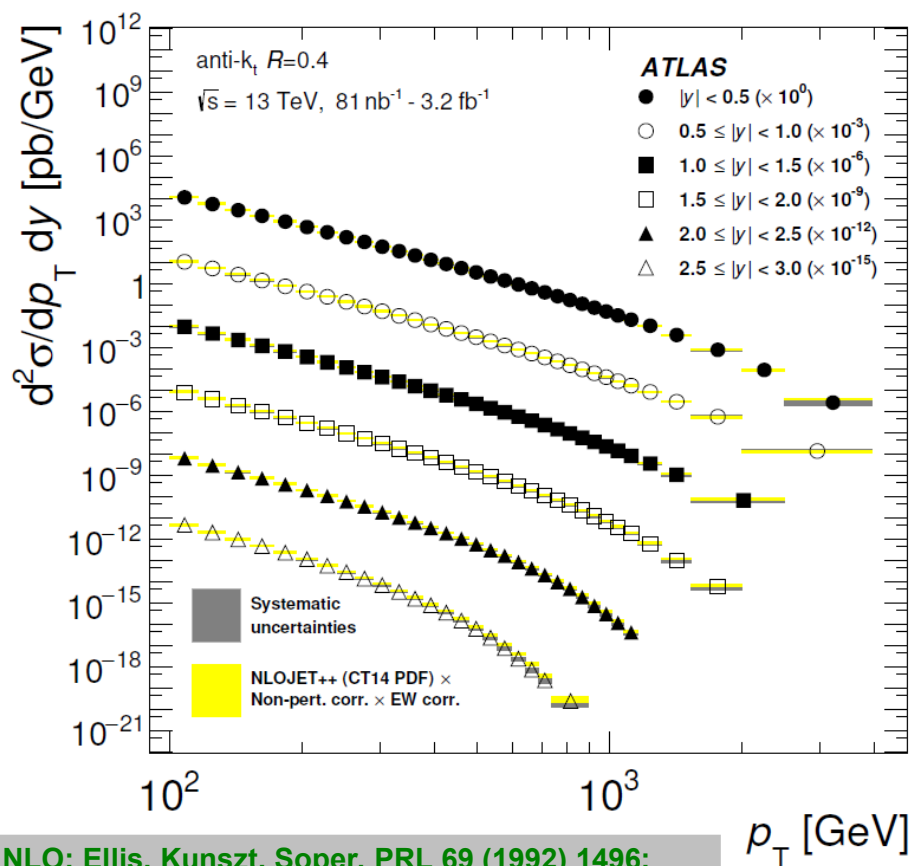


Overall agreement with predictions of **QCD** at **NLO** over many orders of magnitude in cross section and even beyond 2 TeV in jet  $p_T$  and for rapidities  $|y|$  up to 3 ~ 5 at  $\sqrt{s} = 2.76, 7, 8, \text{ and } 13 \text{ TeV}$ .

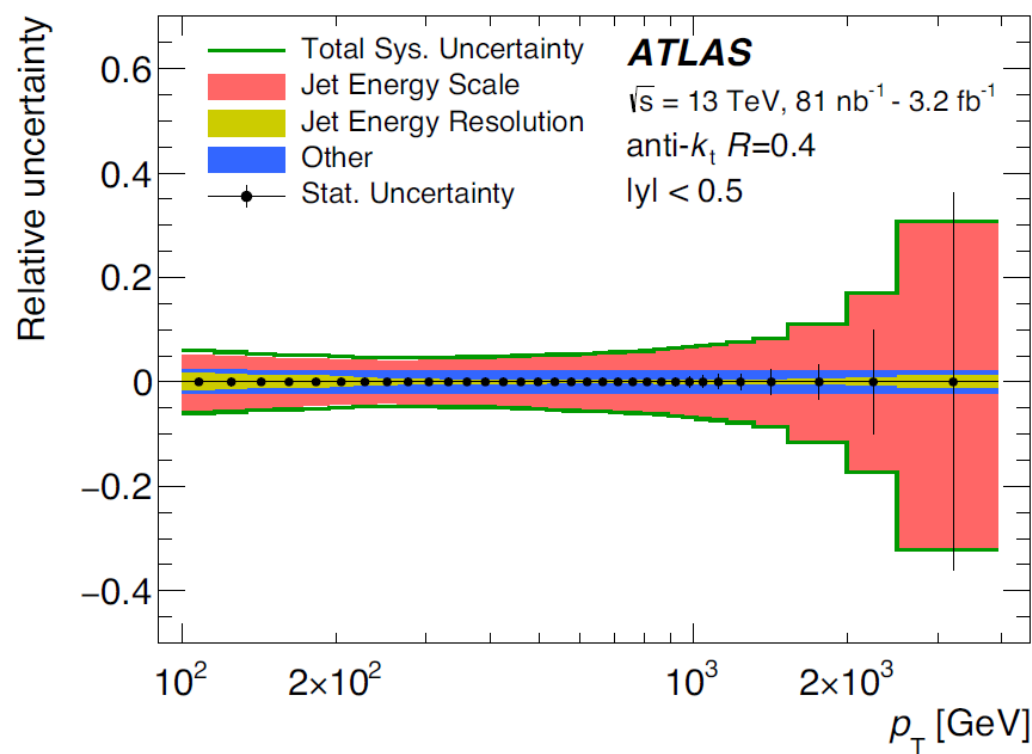
$$\frac{d^2\sigma}{dp_T dy} \propto \alpha_s^2$$

Here: anti- $k_T$ ,  $R=0.4$ , 13 TeV

Data vs. NLO pQCD x non-pert. x EW corrections



Exp. uncertainties for  $|y| < 0.5$

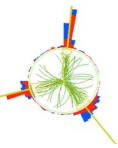


NLO: Ellis, Kunszt, Soper, PRL 69 (1992) 1496;  
 Giele, Glover, Kosower, NPB 403 (1993) 633;  
 Z. Nagy, PRD 68 (2003) 094002.





# Inclusive jets: $\alpha_s$

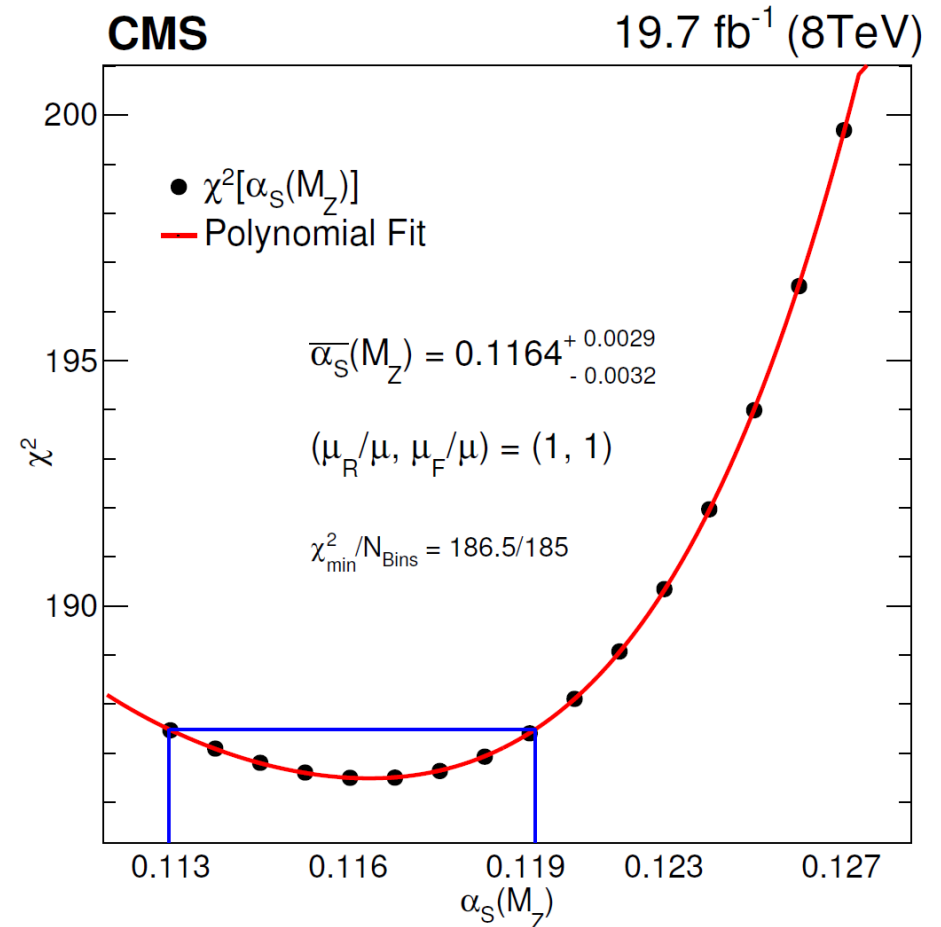
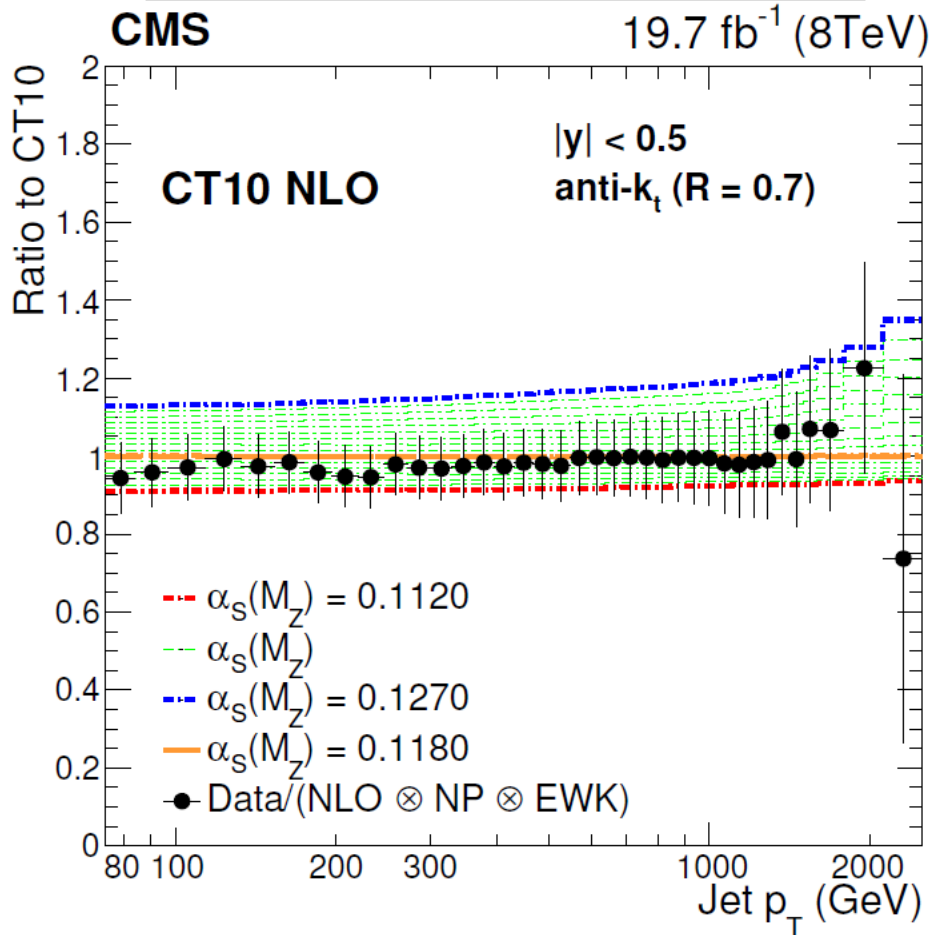


## Sensitivity to $\alpha_s(M_Z)$ at NLO

- CMS: anti- $k_t$   $R = 0.7$  at  $\sqrt{s} = 8$  TeV
- QCD scale choice:  $\mu_R = \mu_F = p_{T,\text{jet}}$

## $\chi^2$ fit of $\alpha_s(M_Z)$ for all jet $p_T$ and $|y|$ bins

- In fit: all exp. + PDF + NP uncertainties
- PDFs: CT10 NLO PDF sets for various  $\alpha_s(M_Z)$

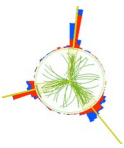


Jets @ NNLO not fully used yet in fits @ LHC → in progress

Results for ep: → Britzger et al., EPJC79 (2019) 845.

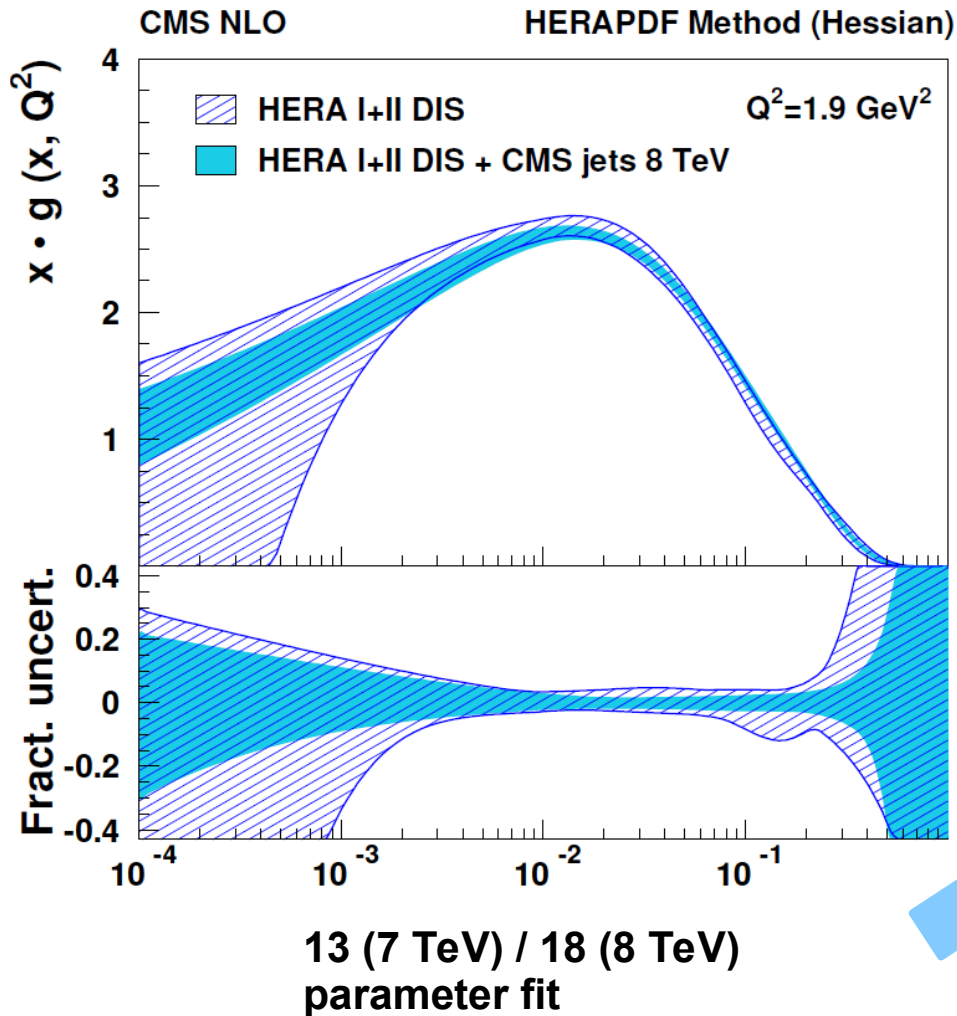


# Inclusive jets: $\alpha_s$ & PDFs



Simultaneous fit of  $\alpha_s$  & PDFs possible combining HERA DIS & CMS jet data using xFitter Tool

## Reduced uncertainties of gluon PDF



## CMS results for $\alpha_s(M_Z)$ at NLO

Orange shading: external PDF sets

Bluish shading: PDF fit incl. HERA data

$\sqrt{s}$ [TeV]	$\text{lum}$ [fb $^{-1}$ ]	$\alpha_s(M_Z)$	exp NP PDF	scale
7	5.0	0.1185	35	+53 -24
8	19.7	0.1164	+29 -33	+53 -28
7	5.0	0.1192	+23 -19	+24 -39
8	19.7	0.1185	+19 -26	+22 -18

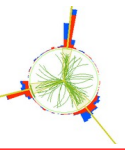
Question: How to deal with uncertainty of Missing higher orders (aka scale uncertainty) in PDF fits?

First progress  $\rightarrow$  e.g. NNPDF, EPJC79 (2019) 931.

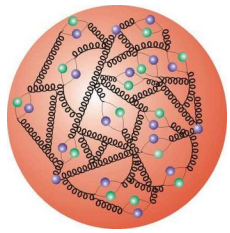
xFitter (HERAFitter): Alekhin et al., EPJC 75 (2015) 304.



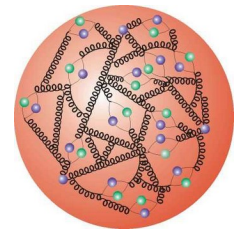
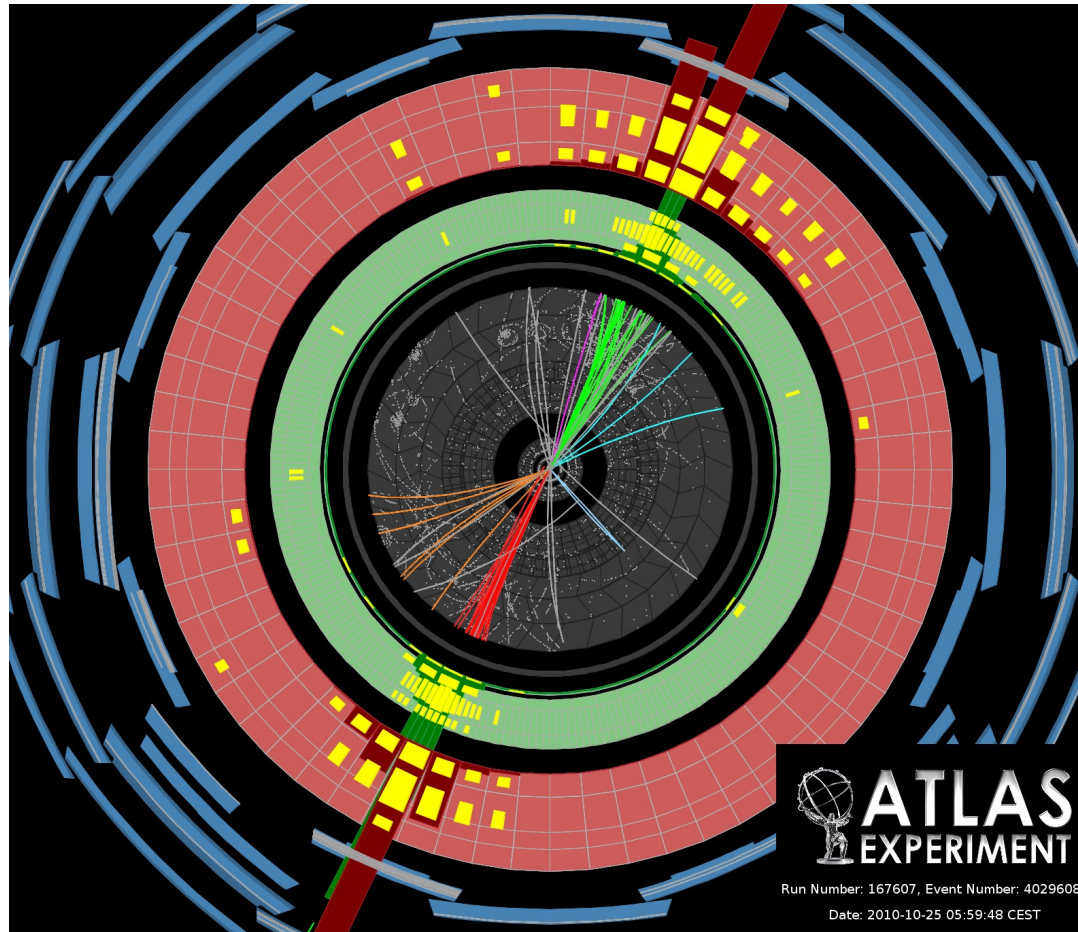
# Dijets



## Large masses



Proton



Proton

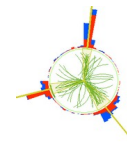


Relevant ATLAS & CMS measurements:

ATLAS:  
JHEP 05 (2014) 059; JHEP 05 (2018) 195.  
CMS:  
PRD 87 (2013) 112002; EPJC 77 (2017) 746.



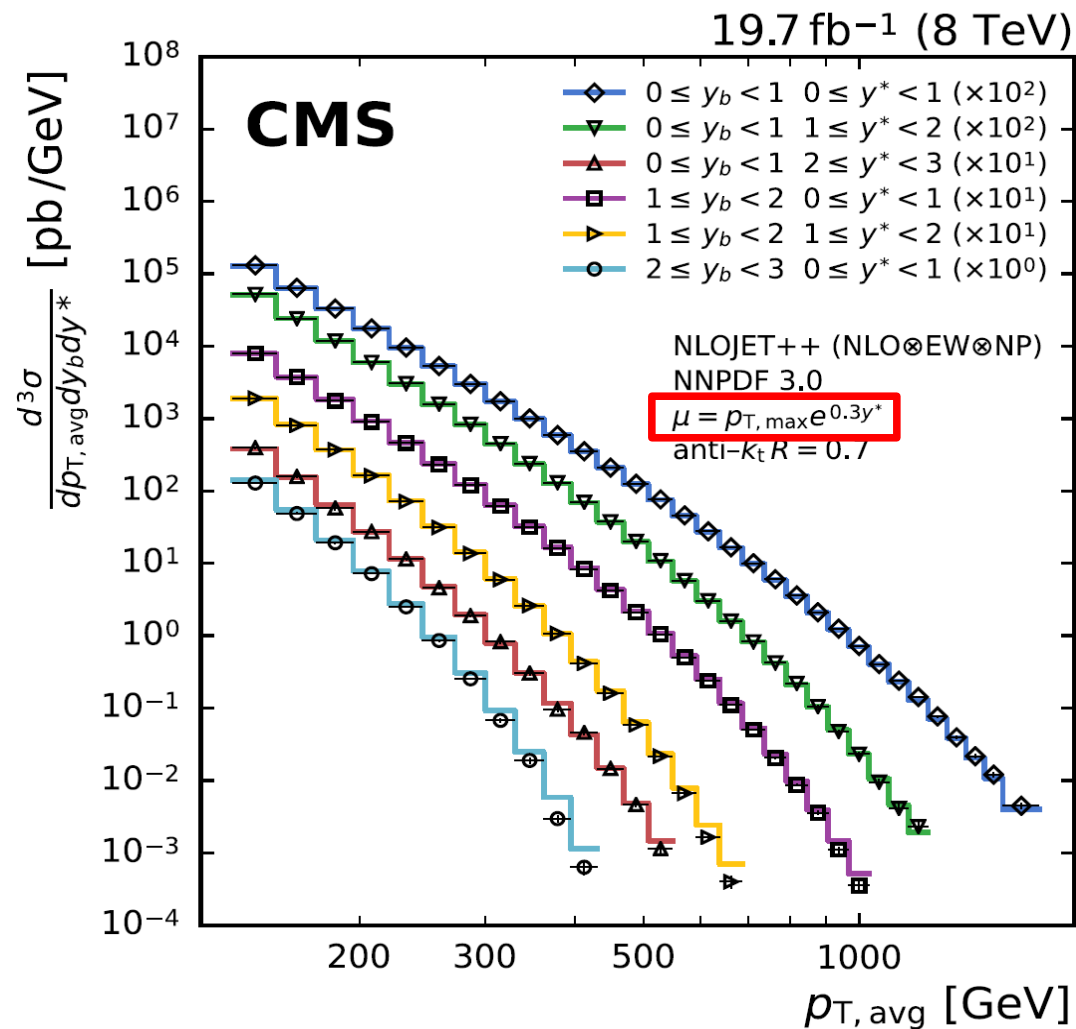
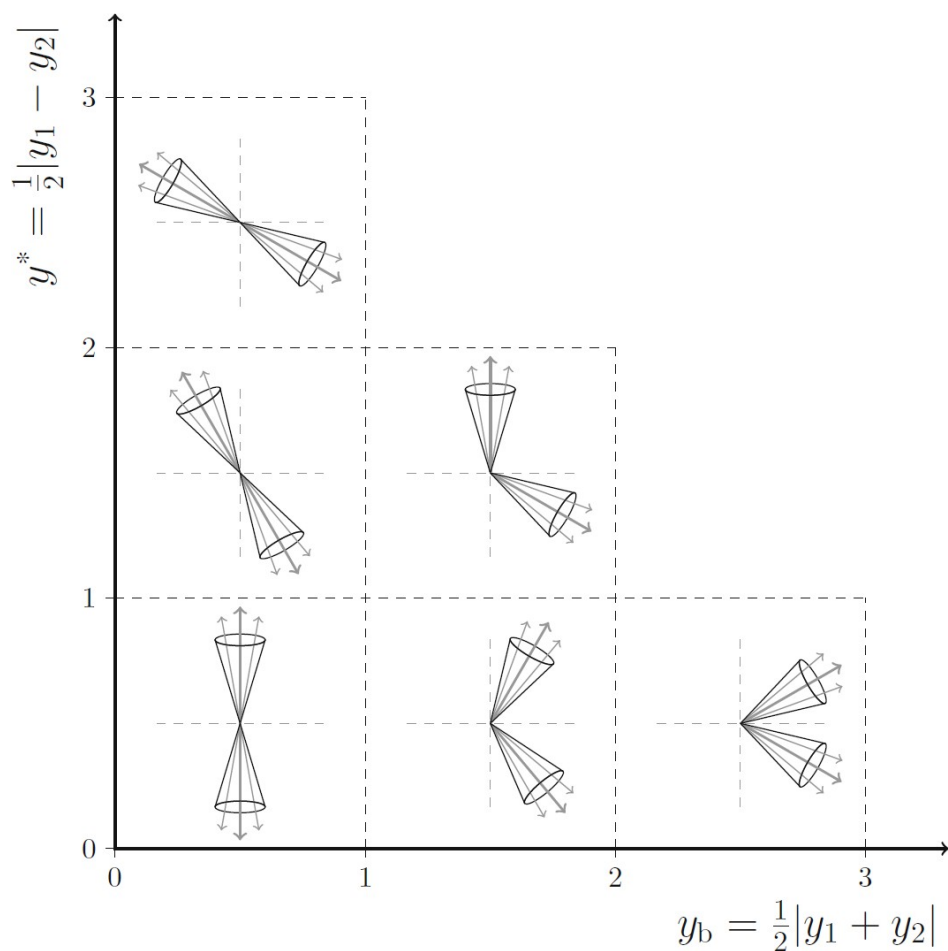
# Triple-differential dijets



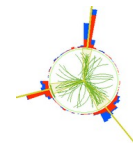
Most measurements done with respect to dijet mass and either max. rapidity  $|y|_{\max}$  (CMS) or rapidity separation  $y^*$  (ATLAS). One CMS result on  $\alpha_s(M_Z)$ :

$$\frac{d^3\sigma}{dp_{T,\text{avg}} dy_b dy^*} \propto \alpha_s^2$$

## Illustration of dijet event topologies



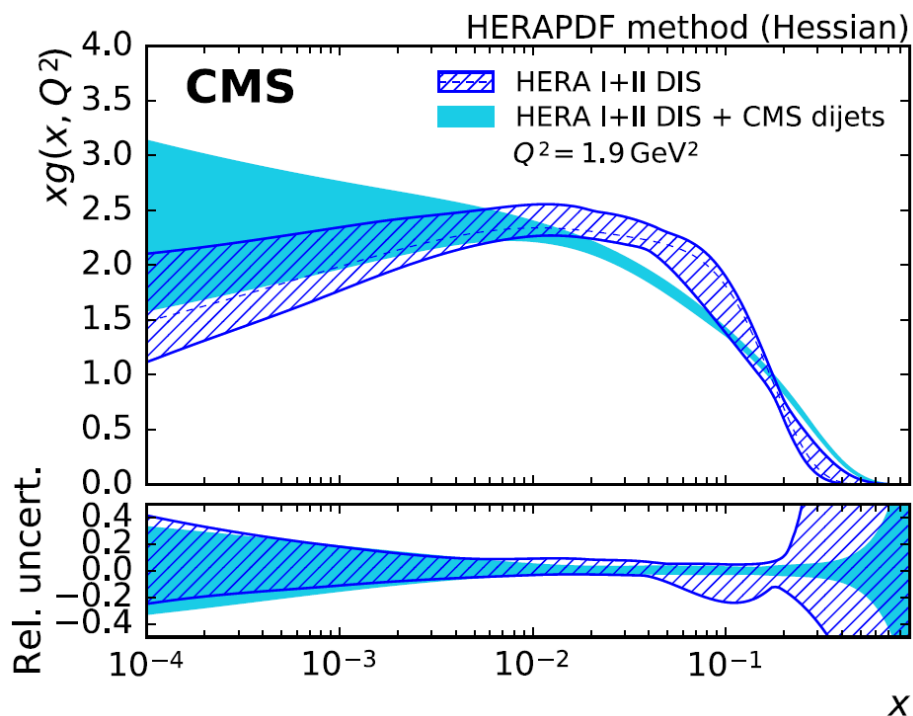
# Triple-differential dijets



Simultaneous fit of  $\alpha_s$  & PDFs combining  
HERA DIS & CMS dijet data using xFitter Tool

Data over NLO pQCD x non-pert. x EW corrections

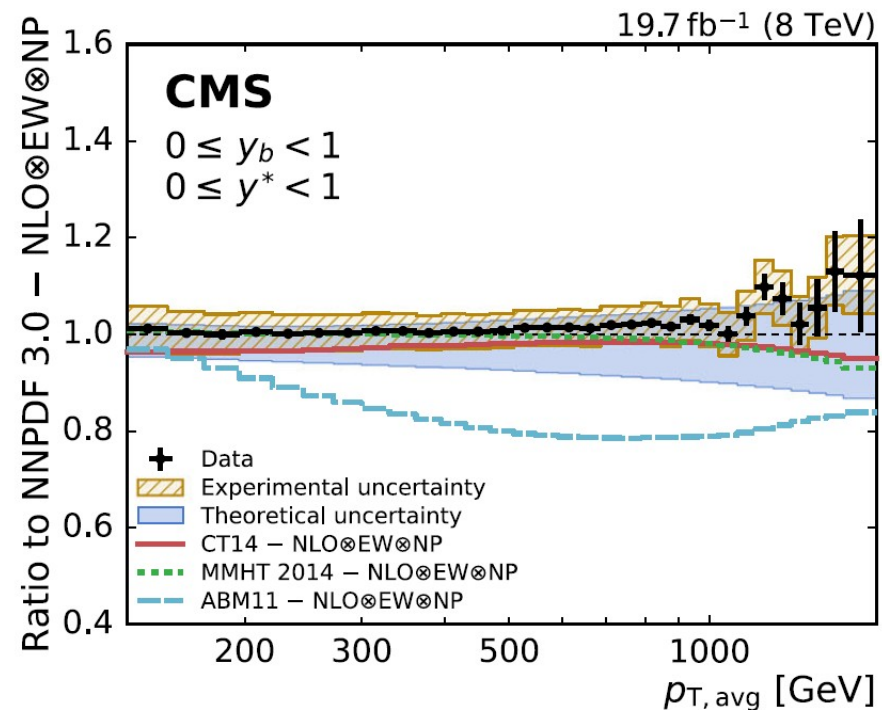
Reduced uncertainties of gluon PDF



16-parameter fit

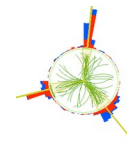


$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp NP PDF	scale
7	5.0	0.1185	35	+53 -24
8	19.7	0.1164	+29 -33	+53 -28
7	5.0	0.1192	+23 -19	+24 -39
8	19.7	0.1185	+19 -26	+22 -18
8	19.7	0.1199	+15 -16	+31 -19



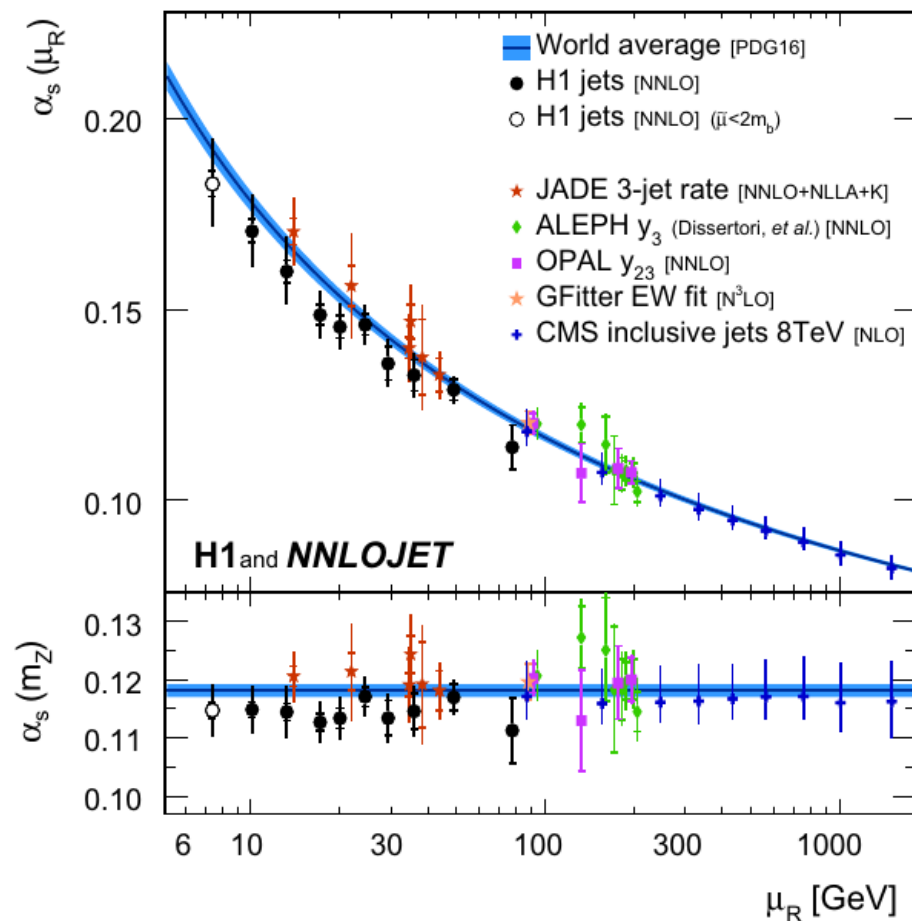
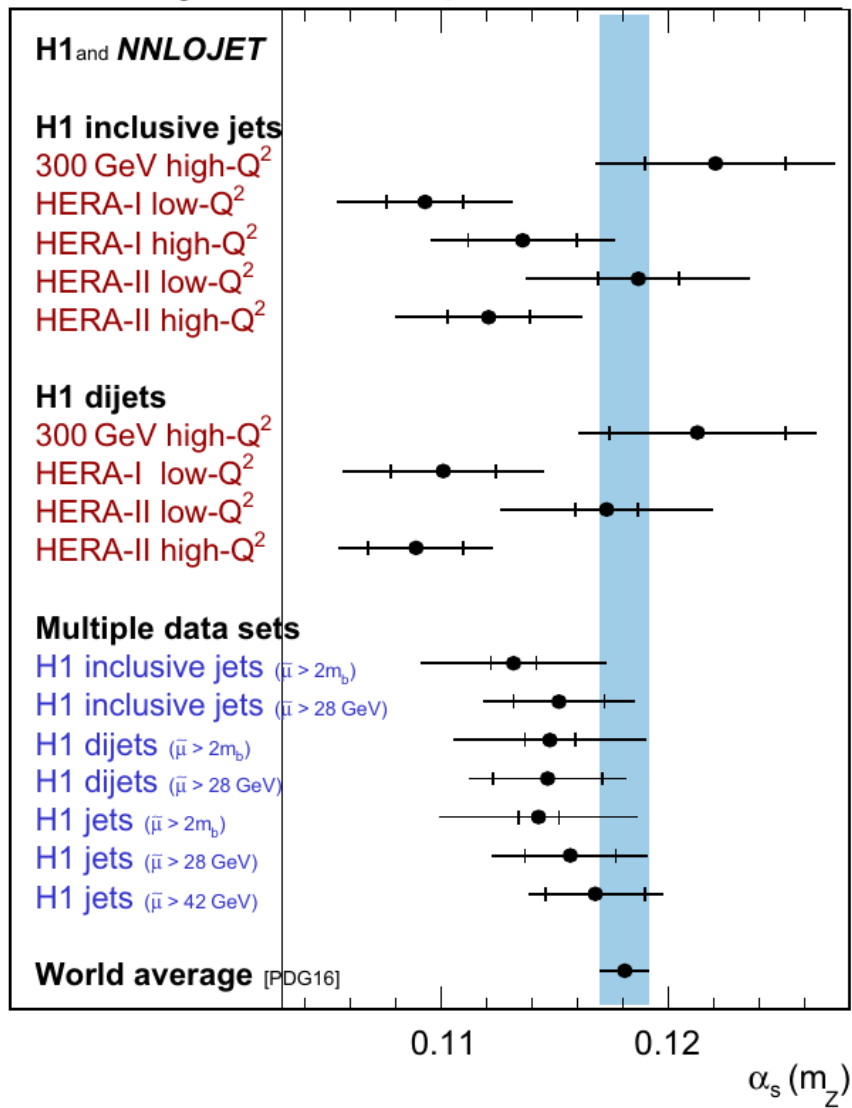


# Inclusive & Dijets at HERA



## NNLO

$\alpha_s$  results from H1 jet data in NNLO



$$\alpha_s(M_Z) = 0.1157^{+0.0035}_{-0.0035}$$

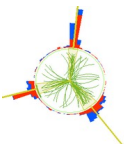
Fit  $\alpha_s$

$$\alpha_s(M_Z) = 0.1142^{+0.0028}_{-0.0028}$$

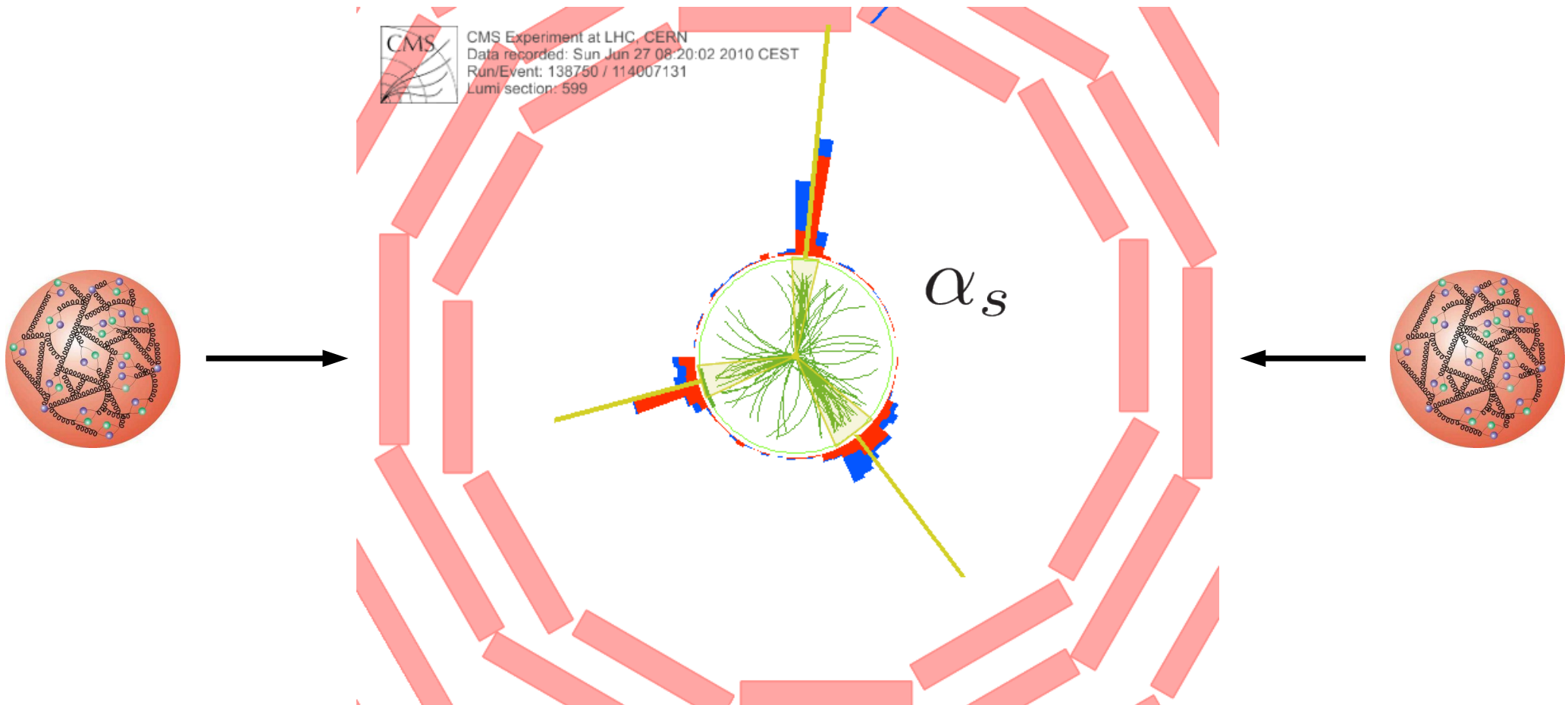
Fit PDF +  $\alpha_s$



# Multi-jets and $\alpha_s$



## Higher multiplicity

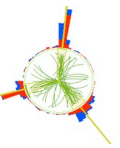


Relevant ATLAS & CMS measurements:

ATLAS:  
EPJC 75 (2014) 288.  
CMS:  
EPJC 73 (2013) 2604; EPJC 75 (2015) 186;  
PAS-SMP-16-008 (2017).



# Jet cross section ratios

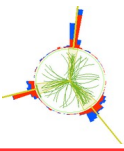


- **Determination of  $\alpha_s(M_Z)$  in single-parameter fit**
- **Test running of  $\alpha_s(Q)$  (reduced PDF dependence)**
- **Some reduction in sensitivity**
- **But cancellation of many systematic effects**
- **More scale choices**





# Sensitivity vs. systematic effects

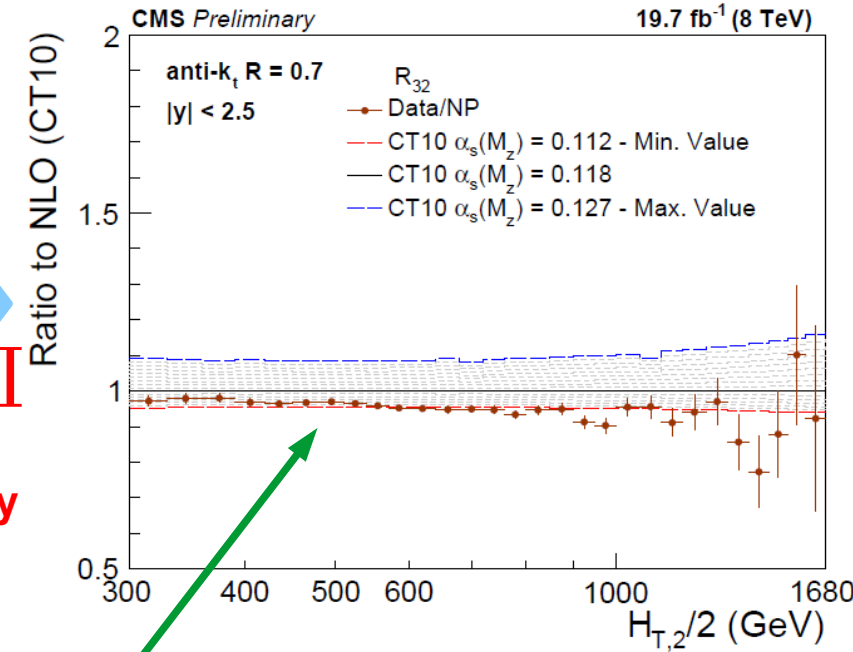
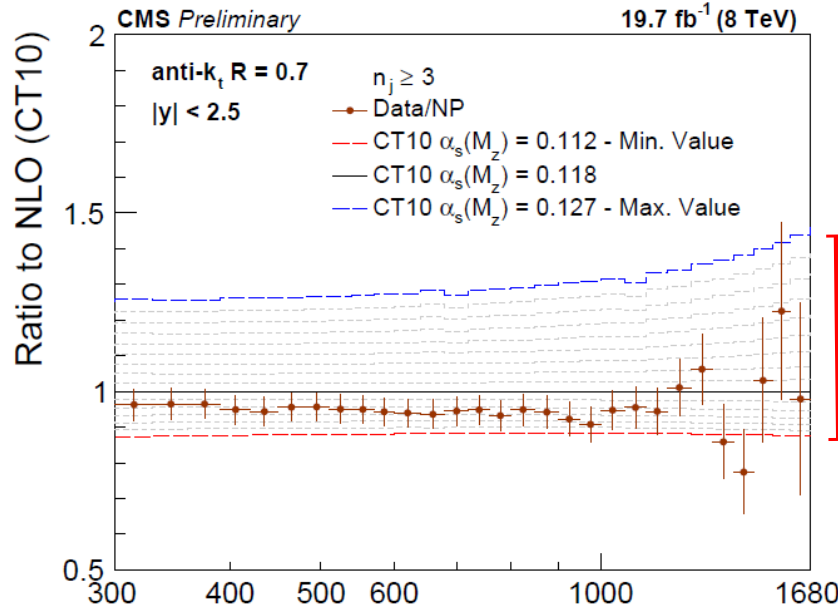


Inclusive 3-jet cross section

$$\sigma_{3j} \propto \alpha_s^3$$

Inclusive 3-jet to inclusive 2-jet cross section ratio

$$R_{3/2} \propto \alpha_s$$

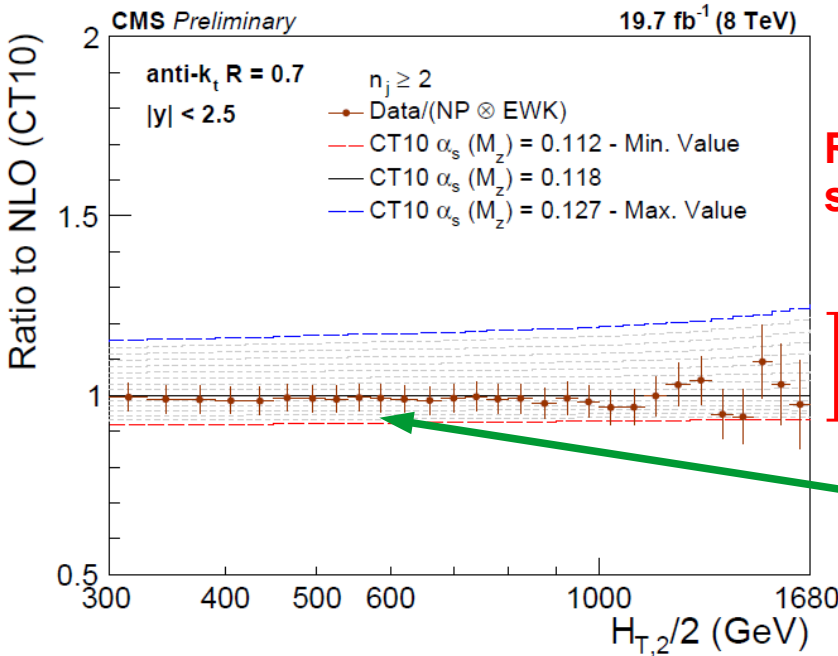


Inclusive 2-jet cross section

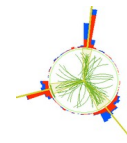
$$\sigma_{2j} \propto \alpha_s^2$$

Reduced sensitivity

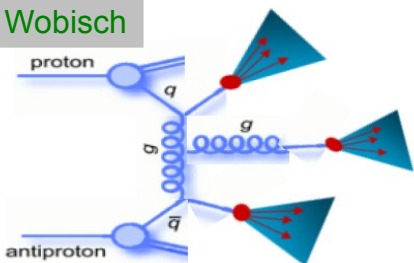
Much reduced systematic uncertainty



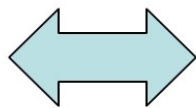
# 3- to 2-jet ratios



M. Wobisch



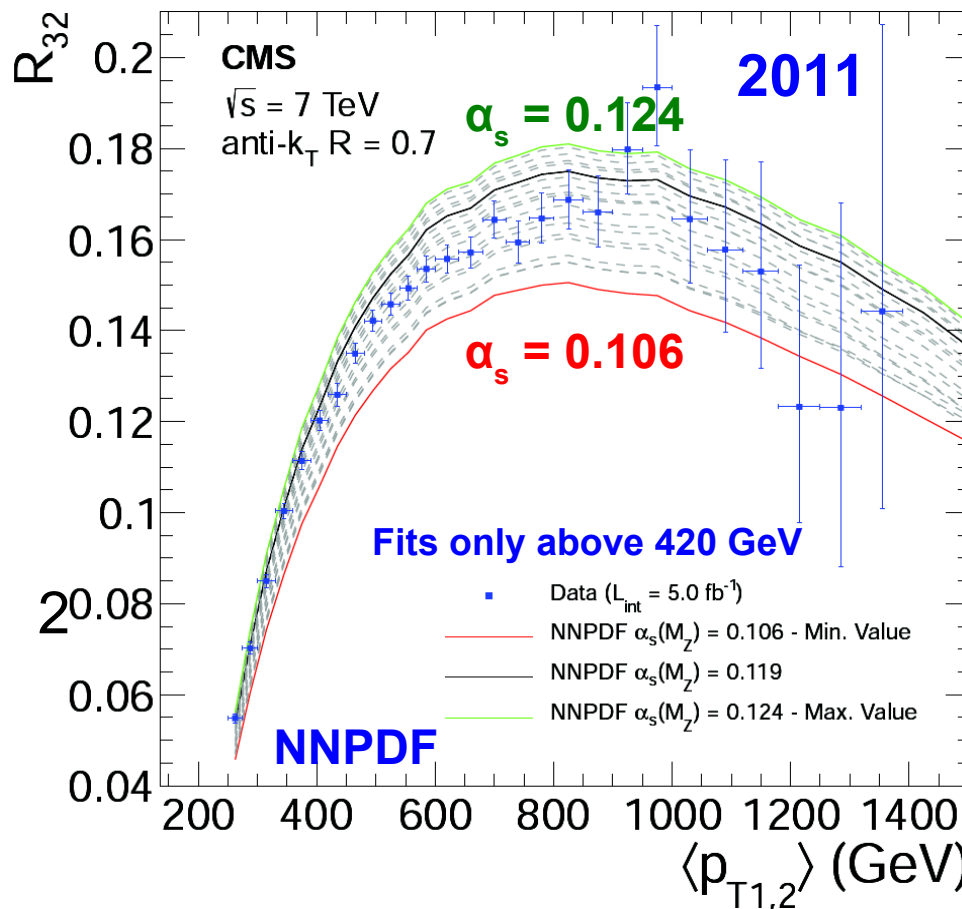
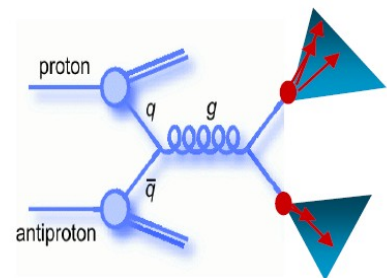
$R_{3/2}$



$\alpha_s$

$$\frac{\sigma_{3+jet}}{\sigma_{2+jet}} \propto \alpha_s^1$$

$$Q = \langle p_{T1,2} \rangle$$



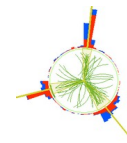
**CMS:  $R_{3/2}$**

- Ratio of inclusive 3- to inclusive 2-jet events
- anti-kt R=0.7
- Min. jet  $p_T$ : 150 GeV
- Max. rap.:  $|y| < 2.5$
- Data 2011 7 TeV, and 2012 8 TeV prel.



$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp NP PDF	scale
7	5.0	0.1148	23	50
8	19.7	0.1150	22	+50

# Running of $\alpha_s(Q)$



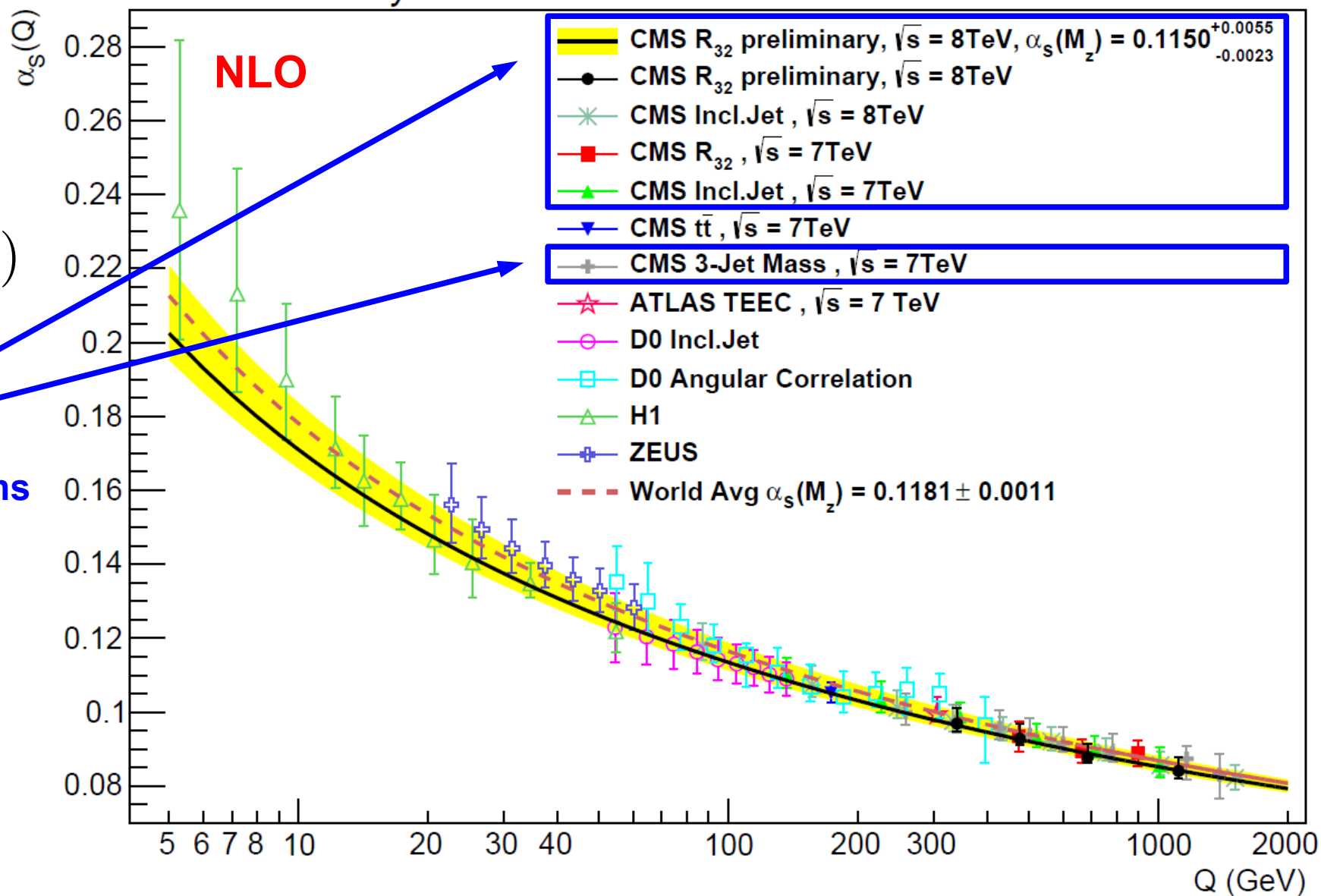
Perform fits in fixed intervals of the chosen scale  $Q$

$\alpha_s(Q)$

Jet cross sections and ratios

Needs an update for latest ATLAS, CMS, & H1 points ...

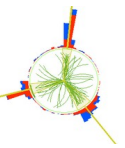
CMS Preliminary



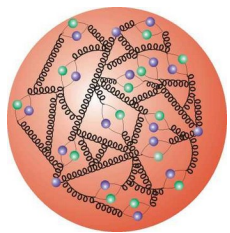
New range explored at LHC  $\longrightarrow$



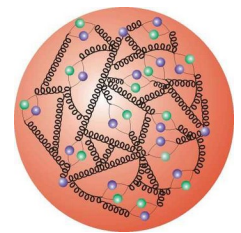
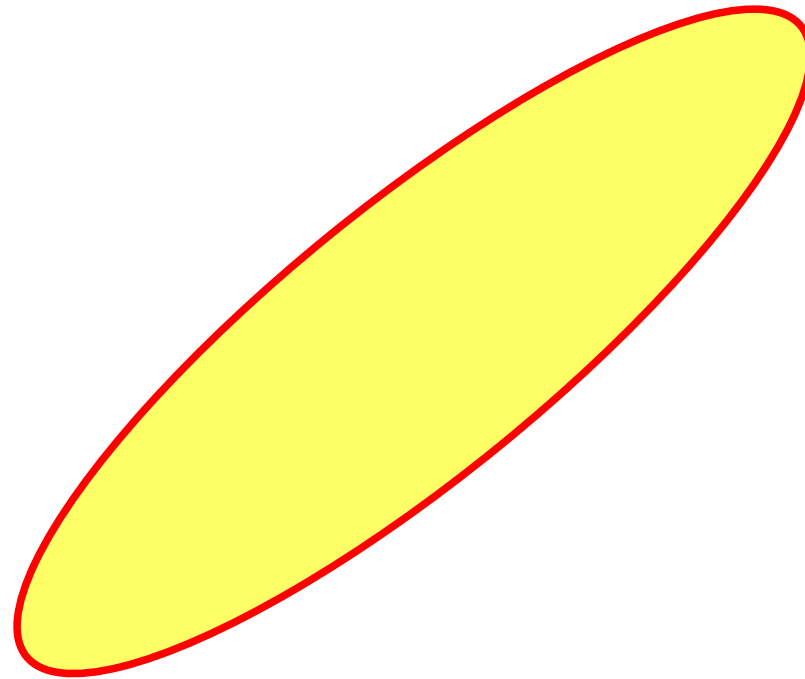
# Normalised distributions



## Event shapes



Proton



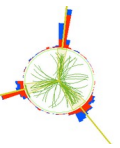
Proton

Relevant ATLAS & CMS measurements:

ATLAS:  
PLB 750 (2015) 427; EPJC 77 (2017) 872;  
PRD98 (2018) 092004.



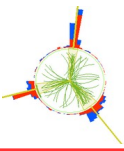
# Normalised distributions



Pros & cons similar as for cross section ratios ...

- Determination of  $\alpha_s(M_Z)$  in single-parameter fit
- Test running of  $\alpha_s(Q)$  (reduced PDF dependence)
- Some reduction in sensitivity
- But cancellation of many systematic effects
- More scale choices

# Transverse energy-energy correlation



$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} = \frac{1}{N} \sum_{A=1}^N \sum_{ij} \frac{E_{Ti}^A E_{Tj}^A}{\left(\sum_k E_{Tk}^A\right)^2} \delta(\cos \phi - \cos \phi_{ij})$$

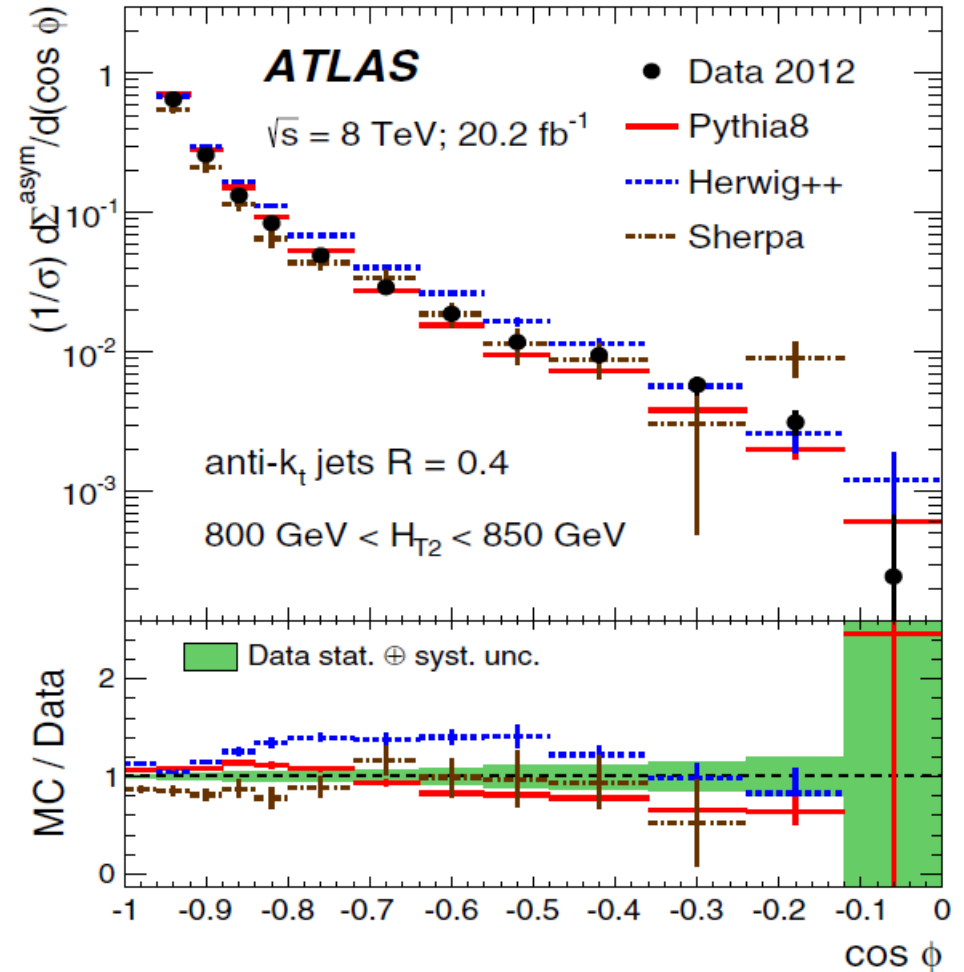
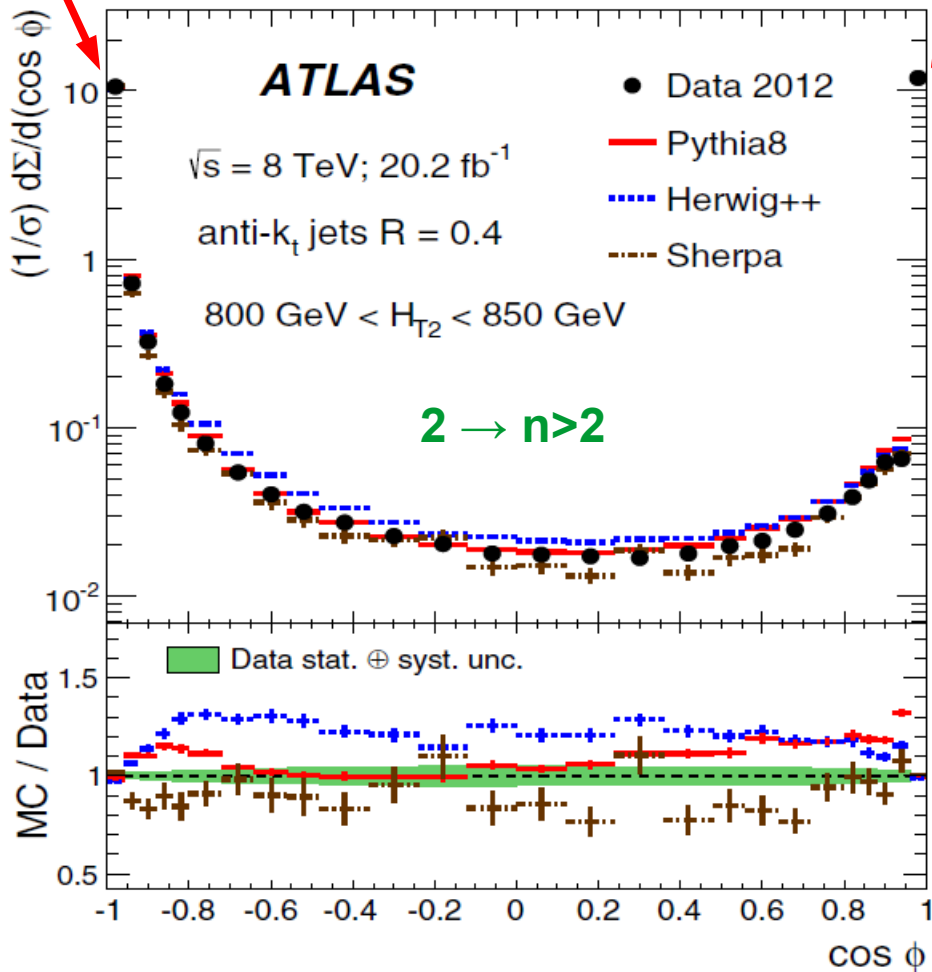
$$\frac{1}{\sigma} \frac{d\Sigma^{\text{asym}}}{d \cos \phi} = \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \Big|_{\phi} - \frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} \Big|_{\pi-\phi}$$

2 → 2

TEEC  $\propto \alpha_s$

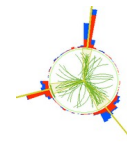
2 → 2

AATEEC  $\propto \alpha_s$





# (A) TEEC in bins of $Q = (p_{T1} + p_{T2})/2$



Theory:  
3-jet NLOJet++

Scale choice:

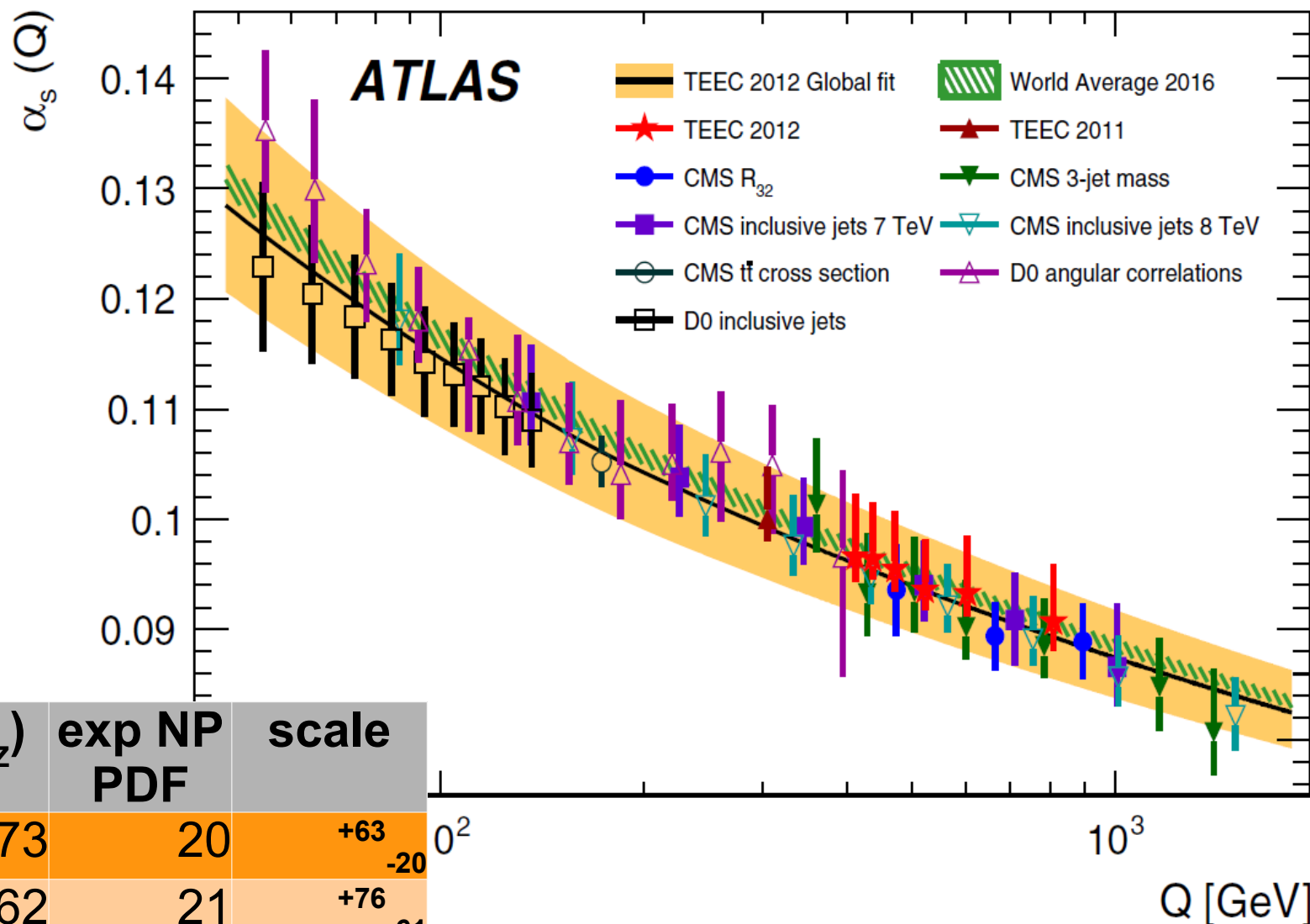
2011 7 TeV:

$$\mu_R = \mu_F = (p_{T1} + p_{T2})/2$$

2012 8 TeV:

$$\mu_R = (p_{T1} + p_{T2})/2$$

$$\mu_F = (p_{T1} + p_{T2})/4$$

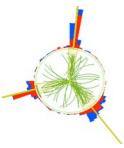


Orange: TEEC  
Blue: ATEEC

$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp NP PDF	scale
7	0.16	0.1173	20	+63 -20
8	20.2	0.1162	21	+76 -61
7	0.16	0.1195	24	+60 -15
8	20.2	0.1196	22	+61 -13



# Dijet azimuthal decorrelation

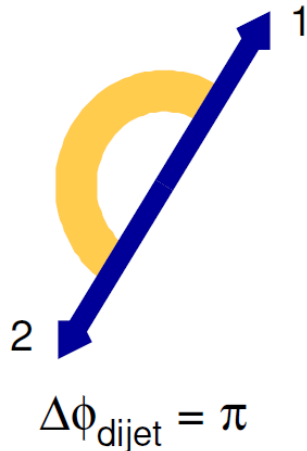


Determine  $\alpha_s(Q)$  from additional parton branchings separated in  $\Phi$  around the two leading jets. Binning in sum of scalar transverse momentum  $H_T$  and rapidity separation  $y^*$ .

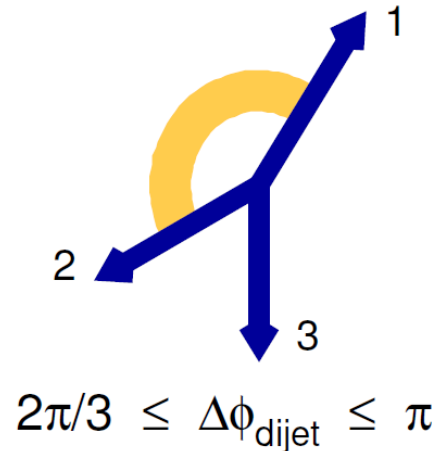
$$R_{\Delta\phi}(H_T, y^*; \Delta\phi_{\max}) = \frac{\frac{d^2\sigma_{\text{dijet}}(\Delta\phi_{\text{dijet}} < \Delta\phi_{\max})}{dH_T dy^*}}{\frac{d^2\sigma_{\text{dijet}}(\text{inclusive})}{dH_T dy^*}}$$

$$R_{\Delta\phi} \propto \alpha_s$$

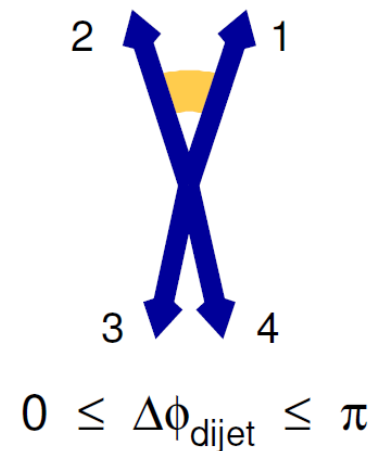
a)  $2 \rightarrow 2$



b)  $2 \rightarrow 3$



c)  $2 \rightarrow 4$



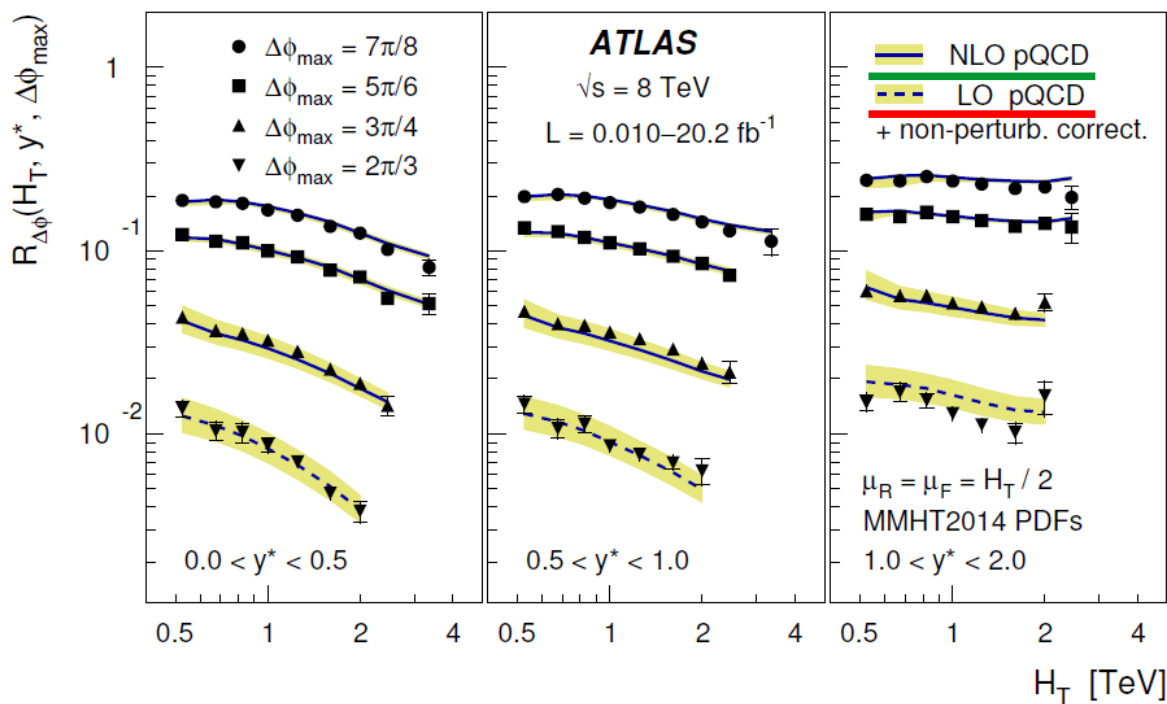
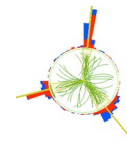
If  $\Delta\phi_{\max}$  in 3-jet region

Wobisch et al., JHEP 01 (2013) 172;  
KR, M. Wobisch, JHEP 12 (2015) 024.





# $R_{\Delta\phi}$ in bins of $Q = H_T/2$

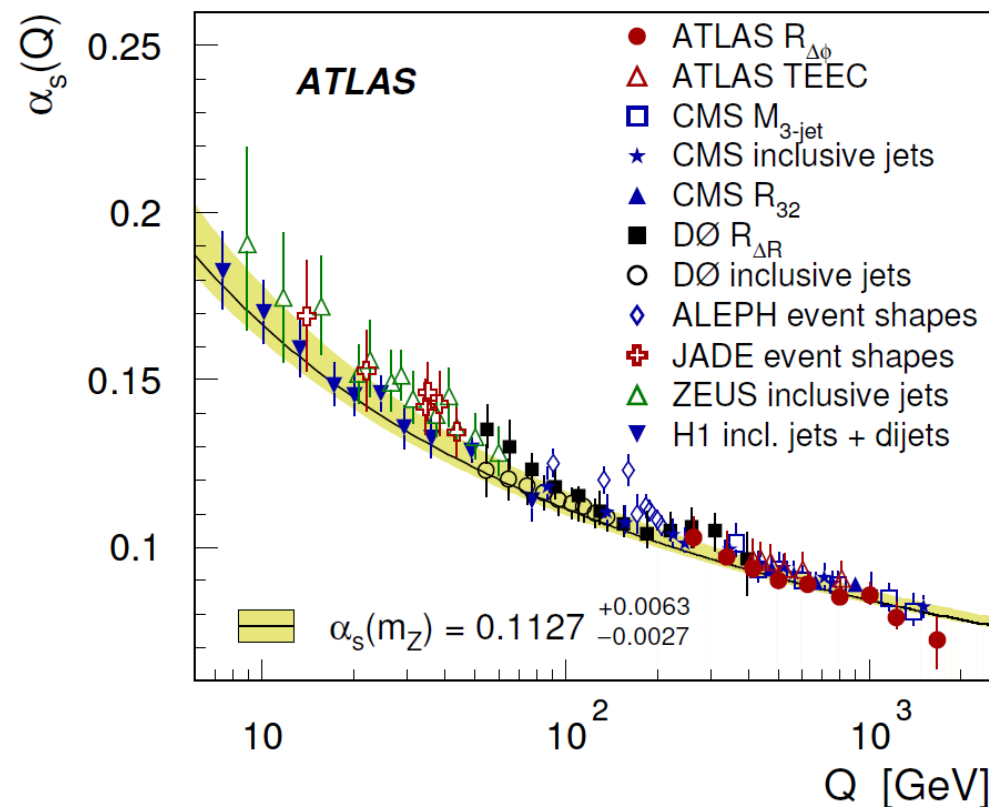


**Theory:**  
3-jet NLOJet++

**Scale choice:**  $\mu_R = \mu_F = H_T/2$

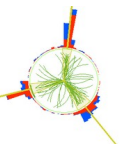
From more precise results with  $\Delta\phi_{\max} = 7\pi/8$  in the two  $y^*$  regions below 1.0:

$\sqrt{s}$ [TeV]	$\text{lum}$ [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp NP PDF	scale
8	20.2	0.1127	+36 -19	+52 -19



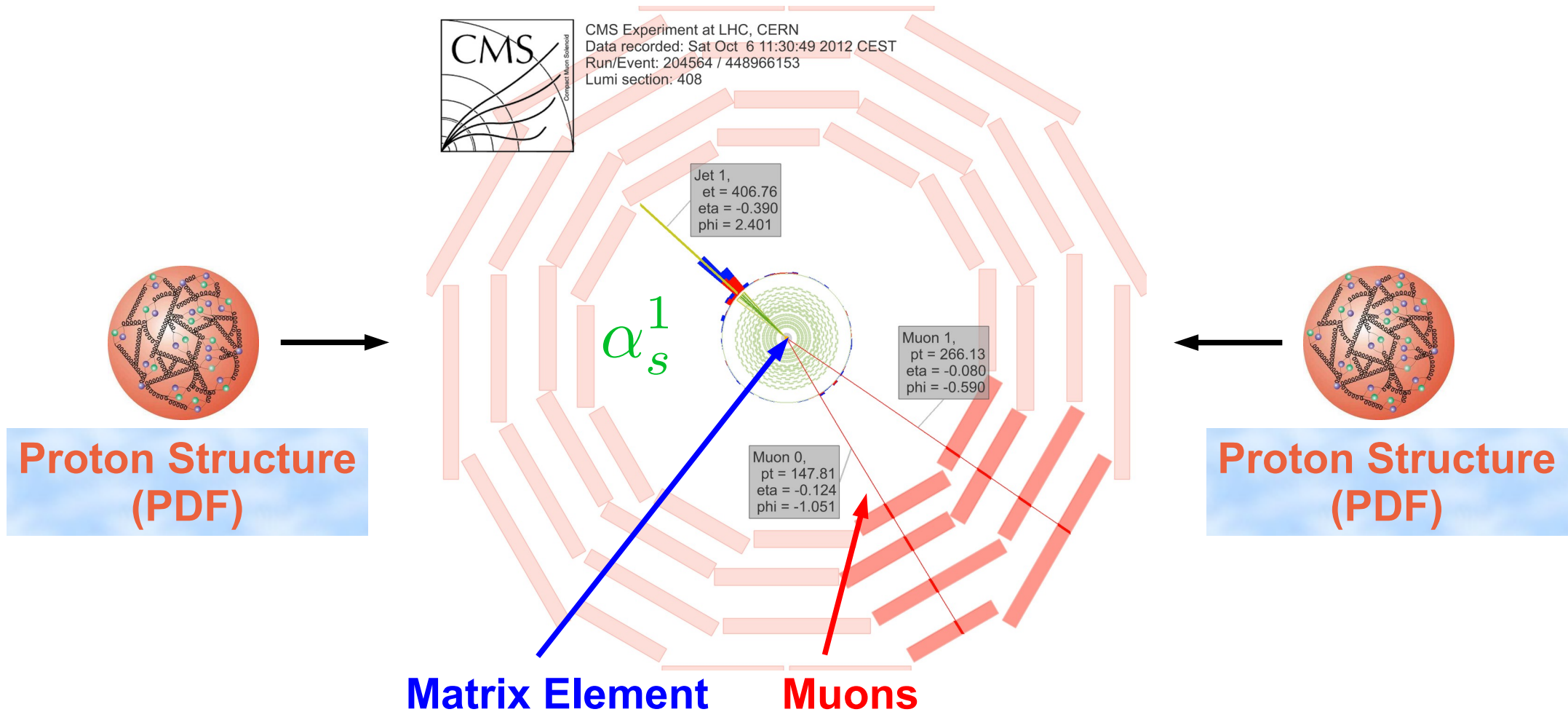


# W, Z, top at the LHC



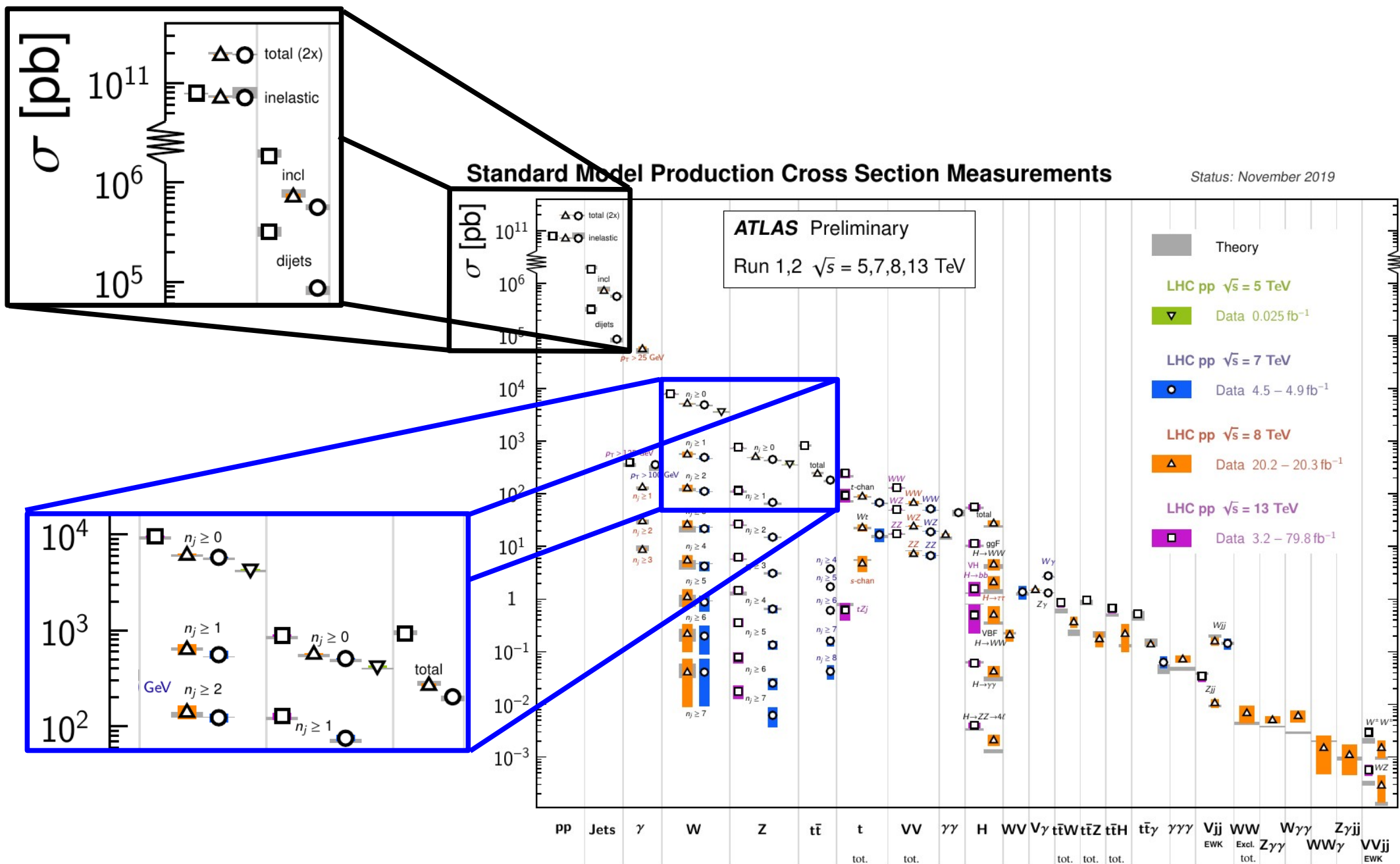
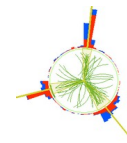
## High-precision lepton measurements:

- ➔ W, Z, top measurements provide high-precision cross sections
- ➔ Also learn about electroweak parameters, the top mass, and the proton structure



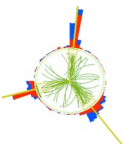


# W, Z, tT at the LHC





# *top-antitop production*



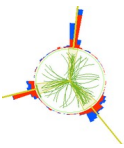
- Determination of  $\alpha_s(M_Z)$  correlated with  $m_{\text{top}}$  (and gluon like for jets)
- Differential cross sections ( $\rightarrow$  Backup)
- What top mass? Pole?  $MS_{\text{bar}}$ ?
- Top measurements already in PDF?
- Theory at NNLO or NNLO+NNLL

**Relevant CMS measurements:**

PLB 728, 496 (2013), JHEP 11, 067 (2012)  
[Erratum: PLB 738, 526 (2014)],  
EPJC 79 (2019) 368,  
arXiv:1904.05237.

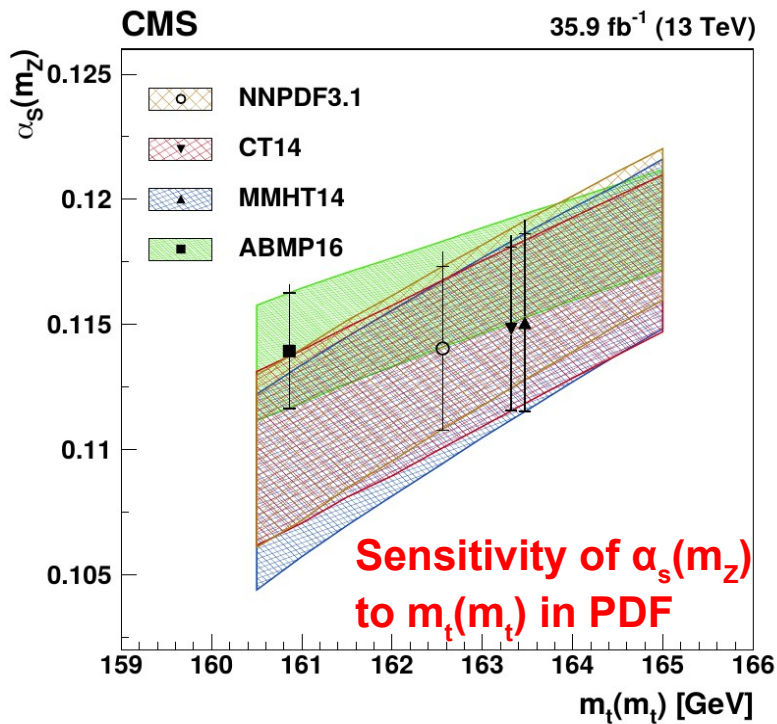


# Fits with $tt$ production cross section



Top-pair production is especially sensitive to: NNLO  
 $m_t$  and  $\alpha_s$  and  $g(x, \mu_f^2)$  as the main production process at LHC is from  $gg$   
 Using only the  $t\bar{t}$  cross section measurement (dilepton channel) combined fits are not possible.

Fix  $m_t$  (& PDF)  $\rightarrow$  constrain  $\alpha_s$  (or vice versa)



Analysis @ 13 TeV much improved:

- ➔ Obtain  $\sigma_{tt}$  in sim. fit from data with  $m_t^{MC}$  as nuisance parameter
- ➔ Running  $MS_{bar}$  mass  $m_t(m_t)$  as scale
- ➔ Conventional scale uncertainty
- ➔ Choose PDF and fix  $m_t(m_t)$  as given
- ➔ Determine  $\alpha_s(M_Z)$  from fit to  $\sigma_{tt}$
- ➔ Try various PDF sets

$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp $m_t$ PDF ...	scale
7	2.3	0.1151	+27 -26	+9 -8
13	35.9	<b>0.1139</b>	23	+14 -1

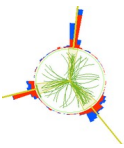
OLD: 7 TeV, NNLO + NNLL, NNPDF23  $\rightarrow$

NEW: 13 TeV, NNLO, ABMP16  $\rightarrow$

HATHOR, Aliev et al., CPC 182 (2011) 1034.



# Inclusive W,Z production



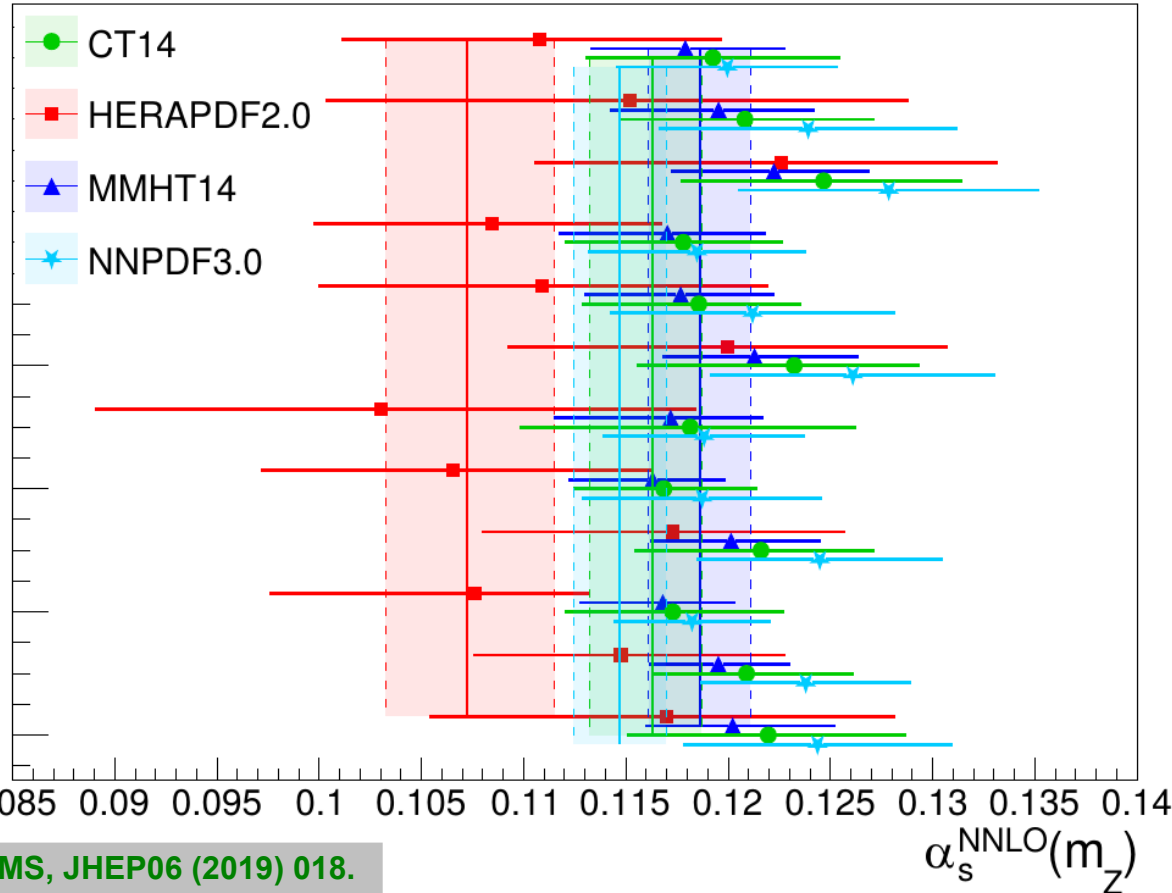
Recent result from combined fit for set of inclusive W and Z cross section measurements, e and  $\mu$  decay final states only.

$$\sigma_{\text{LO}} \propto \alpha_s^0$$

Results using NNLO pQCD for four PDF sets with CMS data.

CMS

38 pb<sup>-1</sup> (7 TeV) + 18.2 pb<sup>-1</sup> (8 TeV)



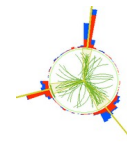
CMS, JHEP06 (2019) 018.

$$\alpha_s(M_Z) = 0.1186^{+0.0025}_{-0.0025}$$

MMHT14 only



# Inclusive W,Z production



Recent result from combined fit for set of inclusive W and Z cross section measurements, e and  $\mu$  decay final states only.

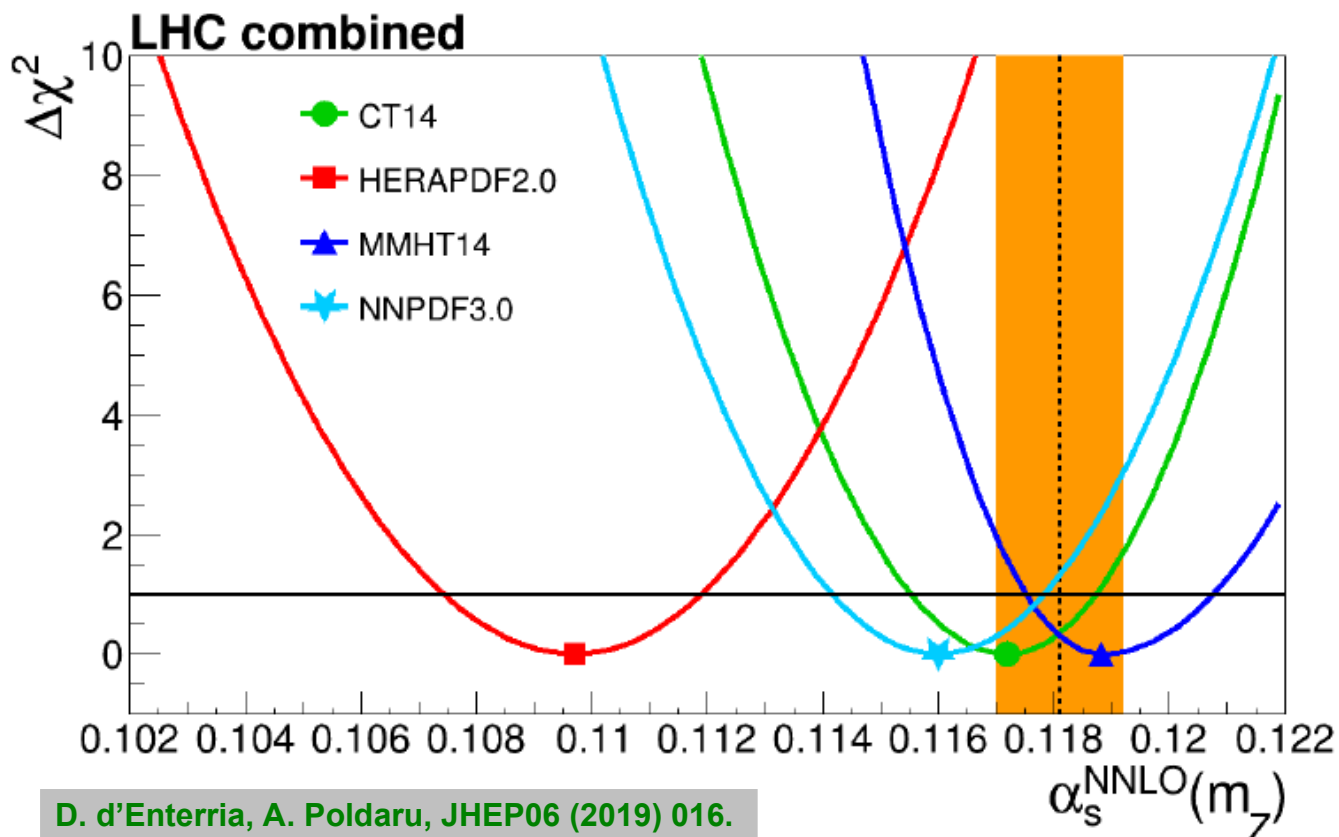
$$\sigma_{\text{LO}} \propto \alpha_s^0$$

Results using NNLO pQCD for four PDF sets with 28 LHC datasets:

ATLAS 7  
CMS 12  
LHCb 9

$$\alpha_s(M_Z) = 0.1188^{+0.0019}_{-0.0013}$$

MMHT14 only



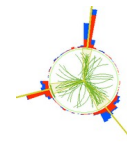
D. d'Enterria, A. Poldaru, JHEP06 (2019) 016.

CT14 & MMHT14 & NNPDF30

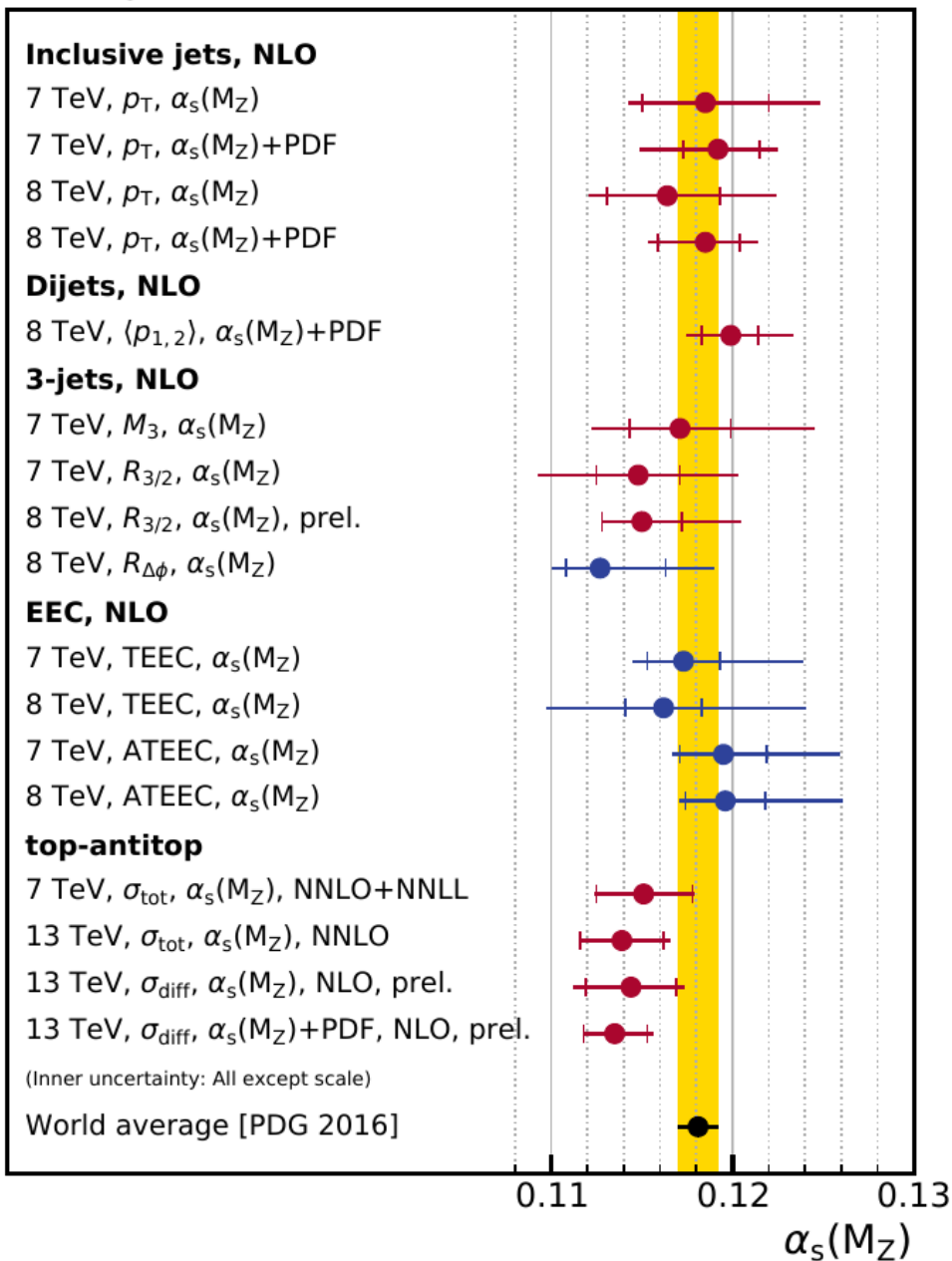
$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	total symm.
7,8,13	var.	0.1173	+17 -17



# Wrap up & concerns



$\alpha_s(M_Z)$  results from ATLAS and CMS

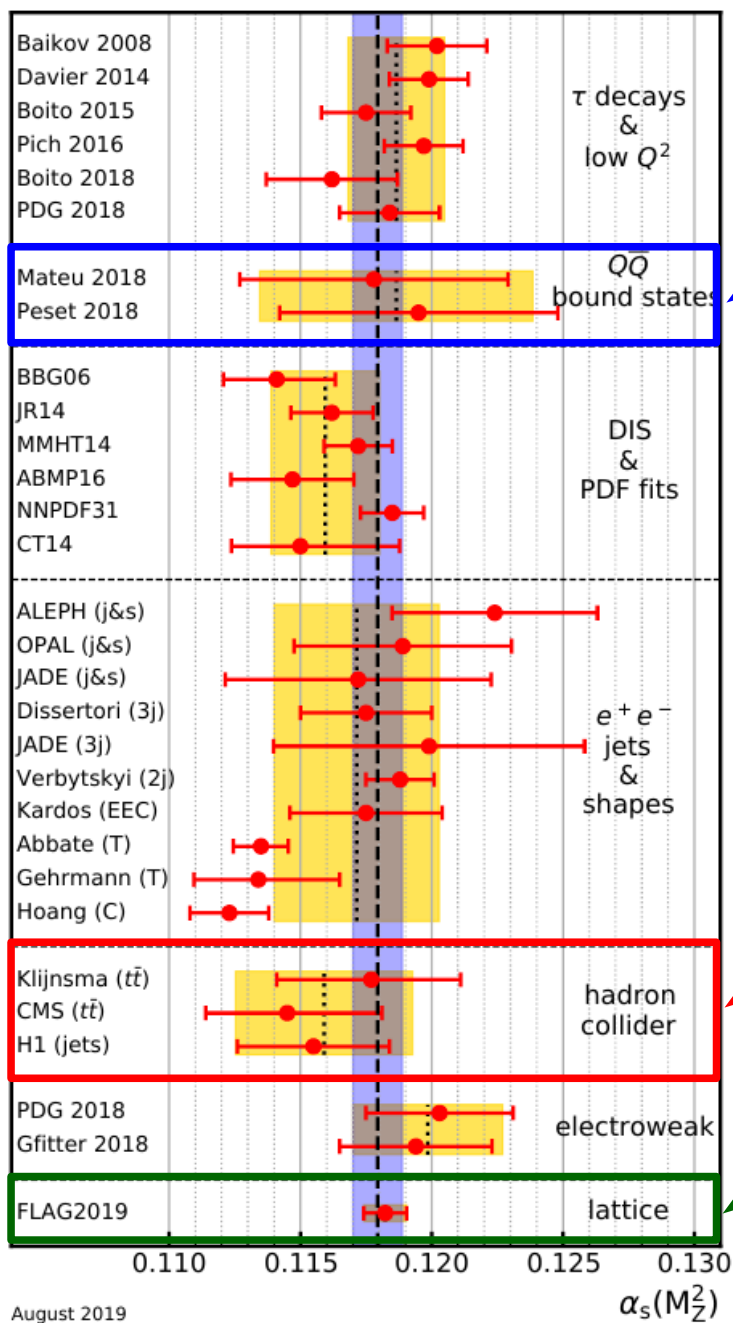
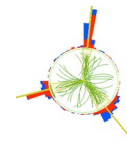


- Correlations to LHC data already in PDF fits
- Correlations between  $\alpha_s(M_Z)$ ,  $M_{top}$ ,  $g(x)$
- (Gu)estimation of nonperturbative effects:
  - Different event generators & tunes, different orders, different ...
  - Incoherent among ATLAS, CMS, Tevatron, ...
- Conventional scale variation by factors of  $1/2$ , 2 and  $1\sigma$  assumption
- Central scale choice ...!





# PDG Summary 2019

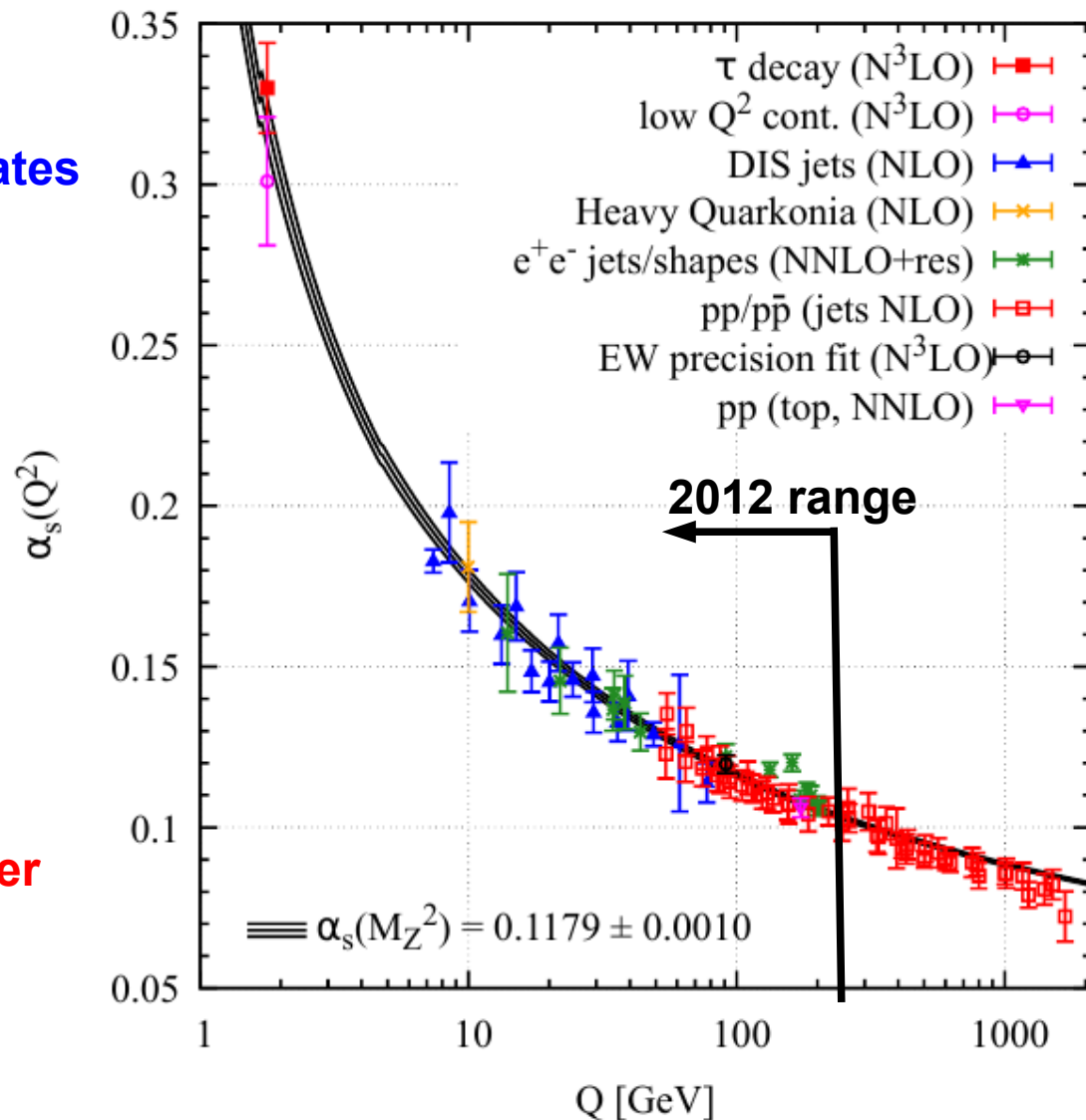


PDG2019

New: QQ bound states

New: hadron collider

Most precise: Lattice



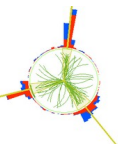
$$\frac{\Delta\alpha_s(M_Z)}{\alpha_s(M_Z)} = 0.8\%$$

PDG'92: 2.4%

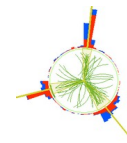
August 2019



# Summary & Outlook



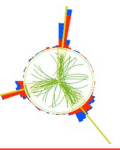
- LHC at 7 TeV and 8 TeV enables measurements up to scales of 2 TeV
- 13 TeV data yet to be fully evaluated
- Theory at NNLO QCD + electroweak corrections are a must!
- Typical uncertainties on  $\alpha_s(M_Z)$ :
  - ➔ Experimental:  $\sim 1 - 2 \%$
  - ➔ PDF:  $\sim 1 - 2 \%$
  - ➔ Scale:  $3 - 5 \%$   $\rightarrow 1 - 2\%$  at NNLO ?  
Central scale choice?
  - ➔ Nonpert. Effects:  $1 \%$  (really?)
- Beyond one experiment started ...
  - ➔ Combined fits of ATLAS & CMS (LHC) measurements
  - ➔ Combined fits of HERA, Tevatron & LHC measurements
- ➔ **CHALLENGE:  $\alpha_s(M_Z)$  at 1% or better from hadron colliders!**



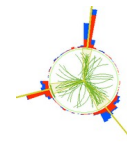
**Thank you for your attention!**



# *Backup Slides*

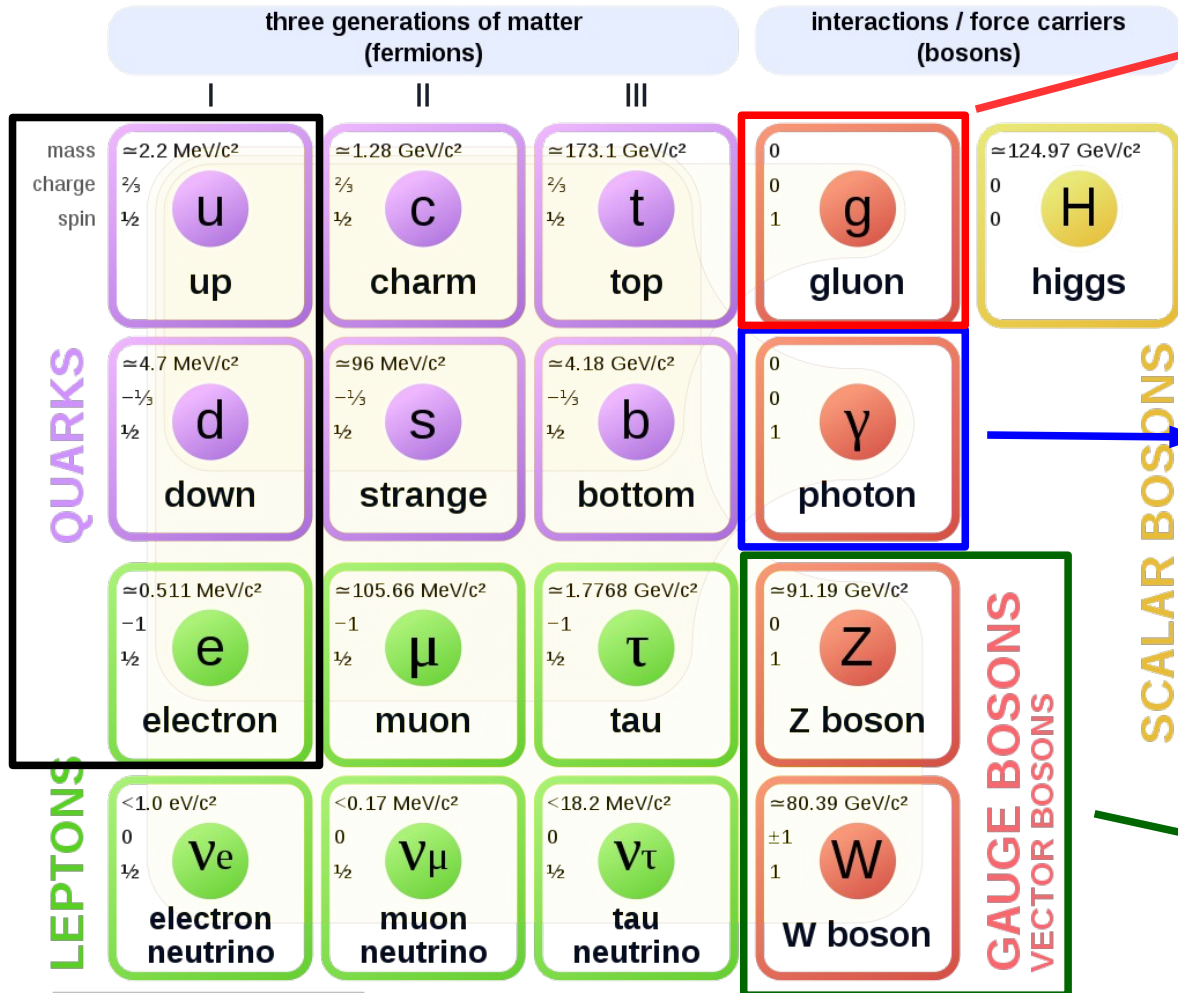


# Standard Model of Particle Physics



## Standard Model of Elementary Particles

Solid matter  
...



Cush, Wikipedia.

... and three fundamental interactions.  
(no gravity)

**Strong interaction**  
(nuclear forces, ...)

$$\alpha_s \approx 0.118$$

$$\Delta\alpha_s/\alpha_s = 8.5 \cdot 10^{-3}$$

**Electromagnetic interaction**  
(magnets, electricity, ...)

$$\alpha \approx 1/137$$

$$\Delta\alpha/\alpha = 0.15 \cdot 10^{-9}$$

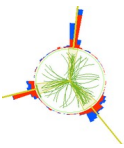
**Weak interaction**  
( $\beta$  decays, sun, ...)

$$G_F \approx 1.17 \cdot 10^{-5} / \text{GeV}^2$$

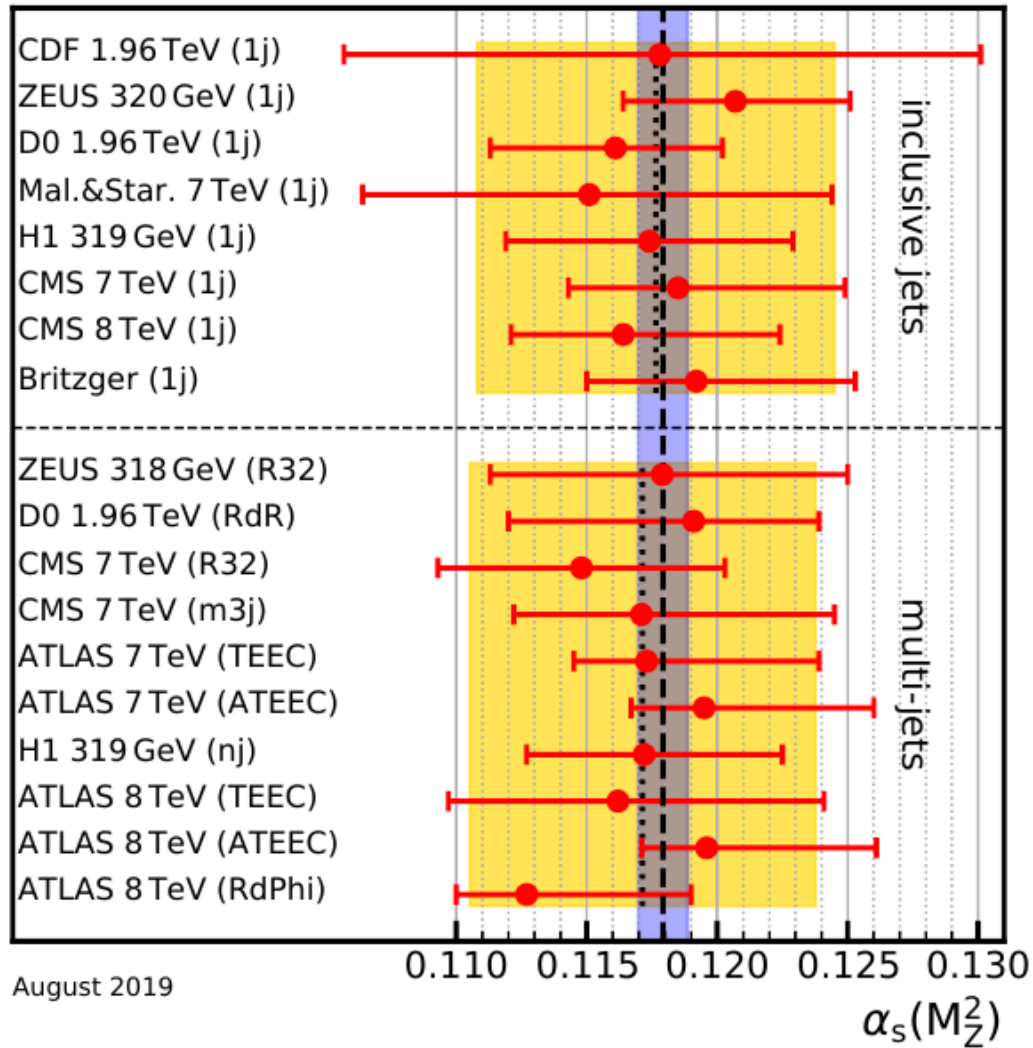
$$\Delta G_F/G_F = 0.51 \cdot 10^{-6}$$



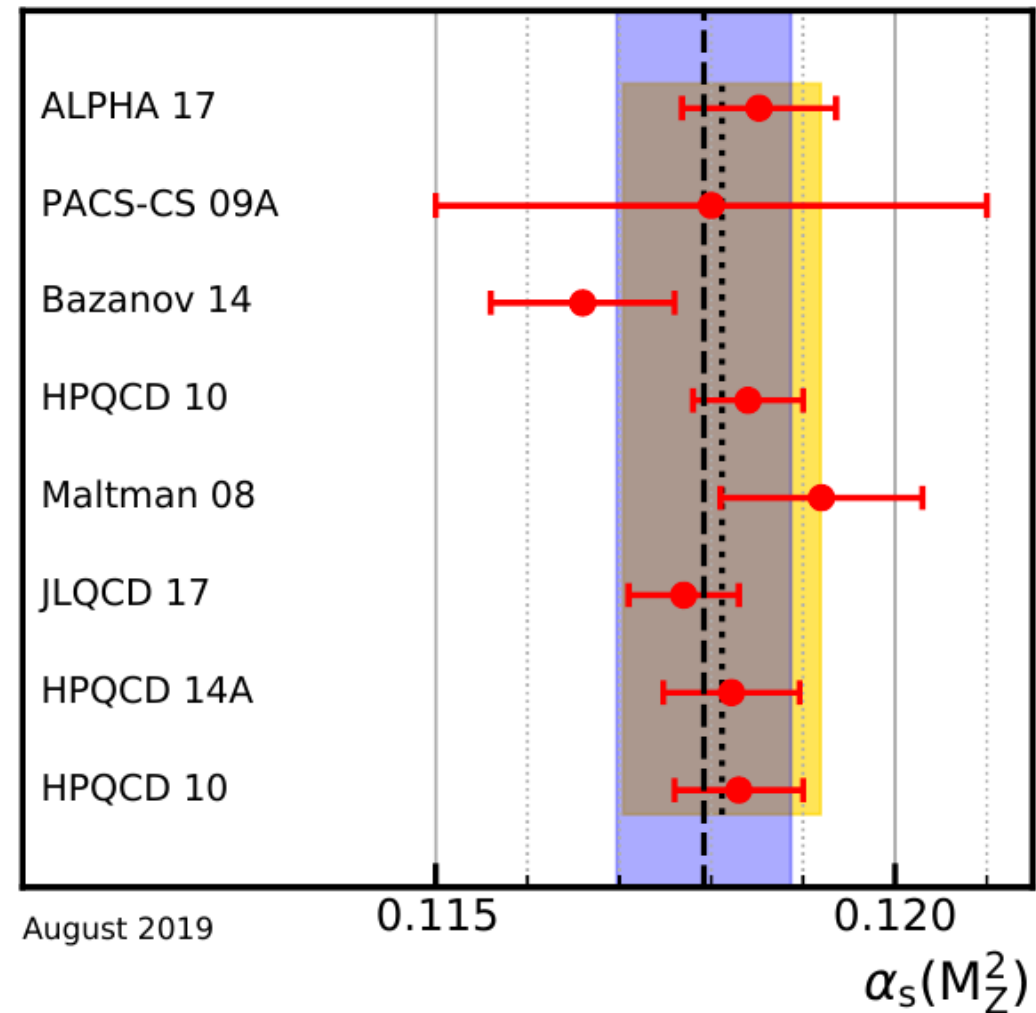
# PDG 2019 Comparison



## $\alpha_s$ at NLO from jet production

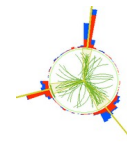


## $\alpha_s$ from lattice groups





# $\alpha_s$ at previous Snowmass



## Still at LHC:

Only jets probe running  $\alpha_s$  at highest scales

< 1% uncertainty at  $M_Z$  challenging ...

Need NNLO and improved PDFs (gluon) plus some experimental optimization

Method	Current relative precision	Future relative precision
<u><math>e^+e^-</math> evt shapes</u>	expt $\sim 1\%$ (LEP) thry $\sim 1-3\%$ (NNLO+up to N <sup>3</sup> LL, n.p. signif.) [27]	< 1% possible (ILC/TLEP) $\sim 1\%$ (control n.p. via $Q^2$ -dep.)
<u><math>e^+e^-</math> jet rates</u>	expt $\sim 2\%$ (LEP) thry $\sim 1\%$ (NNLO, n.p. moderate) [28]	< 1% possible (ILC/TLEP) $\sim 0.5\%$ (NLL missing)
<u>precision EW</u>	expt $\sim 3\%$ ( $R_Z$ , LEP) thry $\sim 0.5\%$ (N <sup>3</sup> LO, n.p. small) [9, 29]	0.1% (TLEP [10]), 0.5% (ILC [11]) $\sim 0.3\%$ (N <sup>4</sup> LO feasible, $\sim 10$ yrs)
$\tau$ decays	expt $\sim 0.5\%$ (LEP, B-factories) thry $\sim 2\%$ (N <sup>3</sup> LO, n.p. small) [8]	< 0.2% possible (ILC/TLEP) $\sim 1\%$ (N <sup>4</sup> LO feasible, $\sim 10$ yrs)
<u><math>ep</math> colliders</u>	$\sim 1-2\%$ (pdf fit dependent) [30, 31], (mostly theory, NNLO) [32, 33]	0.1% (LHeC + HERA [23]) $\sim 0.5\%$ (at least N <sup>3</sup> LO required)
<u>hadron colliders</u>	$\sim 4\%$ (Tev. jets), $\sim 3\%$ (LHC $t\bar{t}$ ) (NLO jets, NNLO $t\bar{t}$ , gluon uncert.) [17, 21, 34]	< 1% challenging (NNLO jets imminent [22])
<u>lattice</u>	$\sim 0.5\%$ (Wilson loops, correlators, ...) (limited by accuracy of pert. th.) [35-37]	$\sim 0.3\%$ ( $\sim 5$ yrs [38])

$\sim 1\%$

< 1%

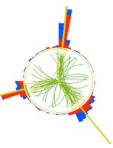
< 1%

$\sim 1\%$

< 0.5%



# Perspectives & educated guesses



## Experiment:

- ➔ Done: Observables  $\sigma \sim \alpha_s^2, \alpha_s^3$ ;  $R_{3/2} \sim \alpha_s$ ; 7 TeV; full phase space
- ➔ Mostly done, 8 TeV data: Some reduction in experimental uncertainty
- ➔ Partially done, 13 TeV: Final precision?
- ➔ Best JEC phase space: Further reduction by some permille?
- ➔ Other observables: Ratios  $(n+m) / n$  jets (incl.  $\gamma, W, Z$ ),  
Normalized cross sections (A)TEEC,  $R_{\Delta\phi}$ ,  $R_{\Delta R}$  ( $\rightarrow$  D0)

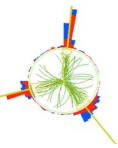
## Theory:

- ➔ Scales: NNLO important  $\rightarrow$  reduction by 2 – 3 percent!?
- ➔ PDFs: Much improved after LHC I, also HERA 2 data available
  - ➔ Better known gluon (**Attention circularity jets  $\rightarrow g(x)$  & jets  $\rightarrow \alpha_s$** )
  - ➔ Fits combining observables at various  $\sqrt{s}$  to disentangle  $g(x)$ ,  $M_t$ ,  $\alpha_s$
- ➔ NNLO ratios?
- ➔ NP effects?





# Scale choices



- Inclusive jets**

$$\mu_0 = p_{T,1}, \quad p_{T,\text{jet}}, \quad \hat{H}_T?$$

- Dijets**

$$\mu_0 = p_{T,1}, \quad p_{T,1} \cdot \exp(0.3y^*)?$$
$$\mu_0 = (p_{T,1} + p_{T,2}) / 2, \quad m_{jj}/2?$$

- 3-jets**

$$\mu_0 = p_{T,3}, \quad (p_{T,1} + p_{T,2}) / 2, \quad m_{jjj}/2?$$

- Ratios**

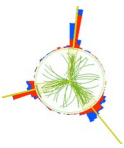
- Shapes**

- V+jets**

$$\mu_0 = \sqrt{M_Z^2 + p_{TZ}^2} + H_{T,\text{jet}}?$$



# Inclusive jets: theory corrections



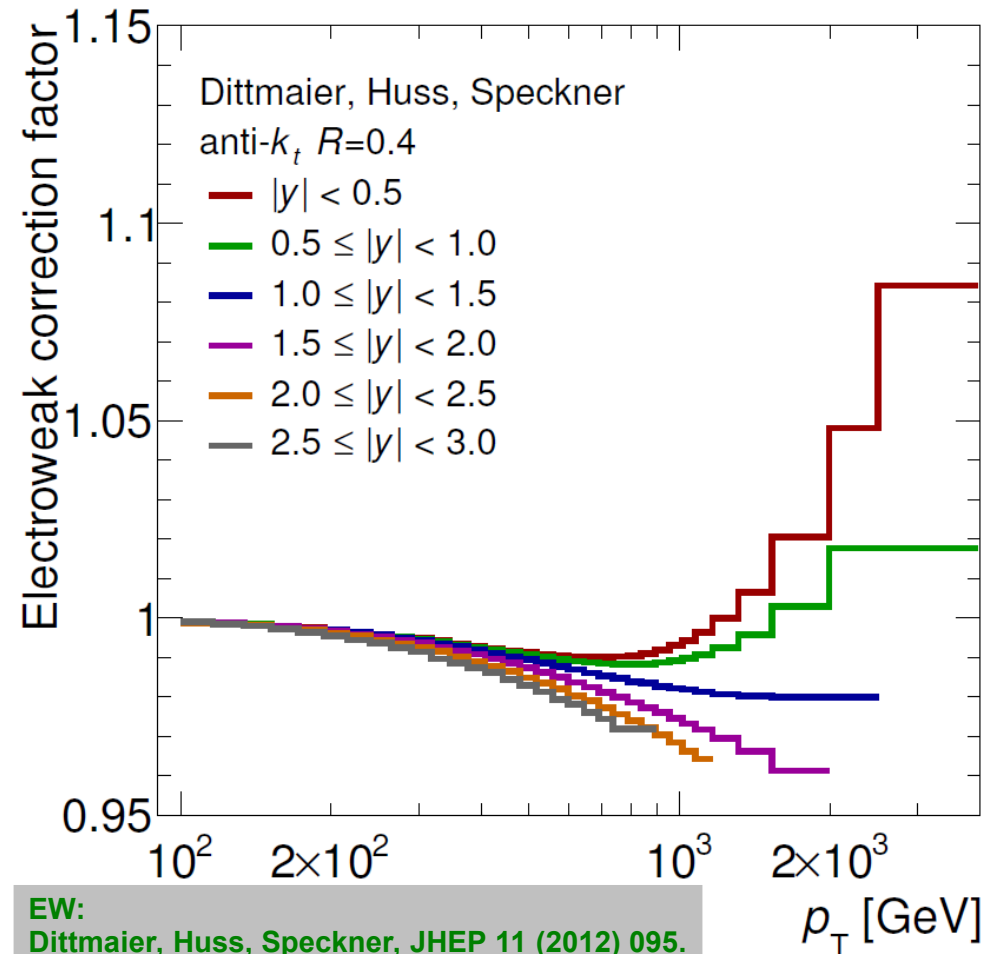
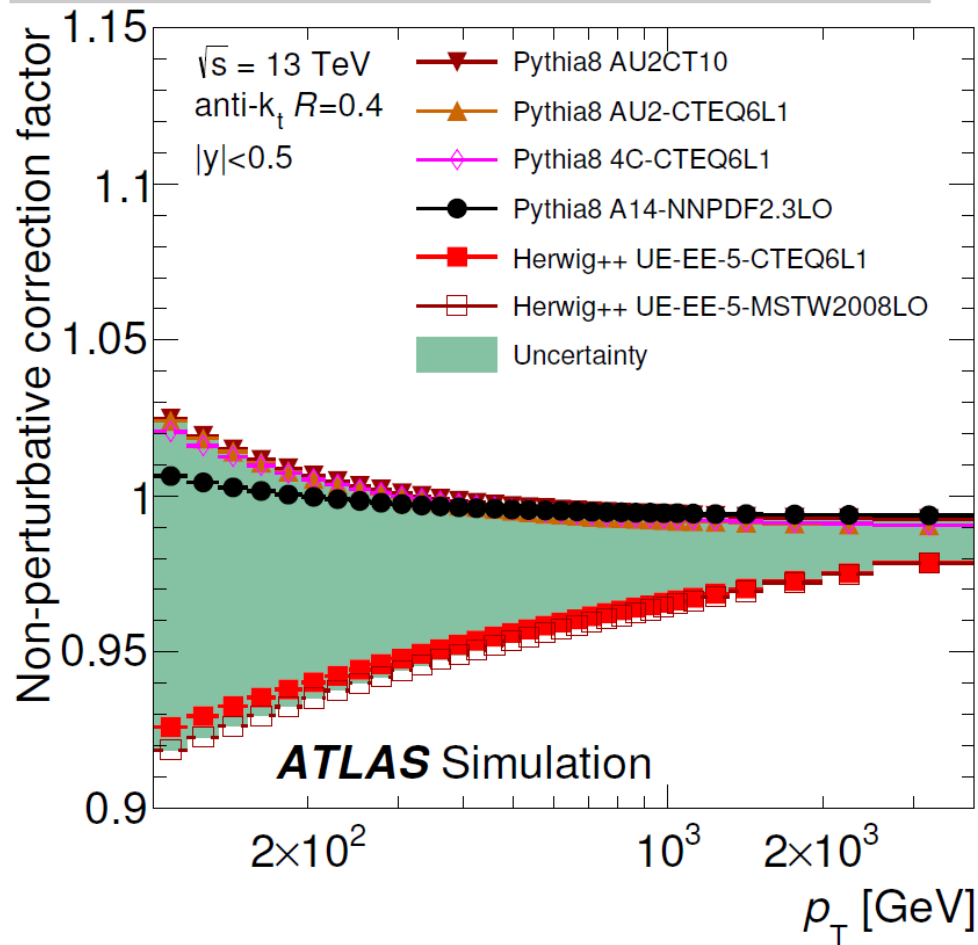
anti-kt, R=0.4, 13 TeV,  $|y| < 0.5$

## Nonperturbative correction factors:

- estimated from tuned MC event generators
- **uncertainty of 5 – 15% at  $p_T = 100$  GeV**
- strongly dependent on jet size R
- less important at high  $p_T$

## Electroweak correction factors:

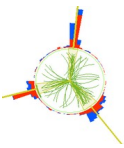
- calculated perturbatively
- uncertainty small
- strongly dependent on jet rapidity y
- very important at high  $p_T$



EW:  
 Dittmaier, Huss, Speckner, JHEP 11 (2012) 095.  
 Frederix et al., JHEP 04 (2017) 076.



# Inclusive jets: theory corrections



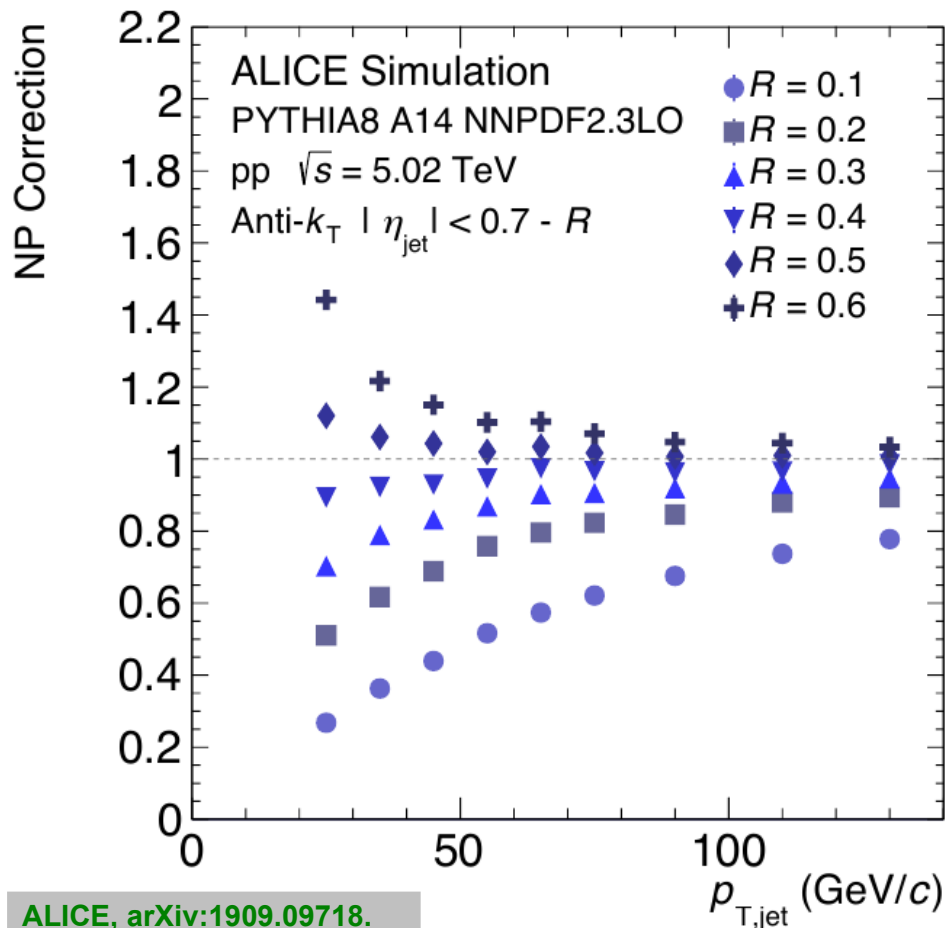
anti-kt, R=0.4, 13 TeV,  $|y| < 0.5$

## Nonperturbative correction factors:

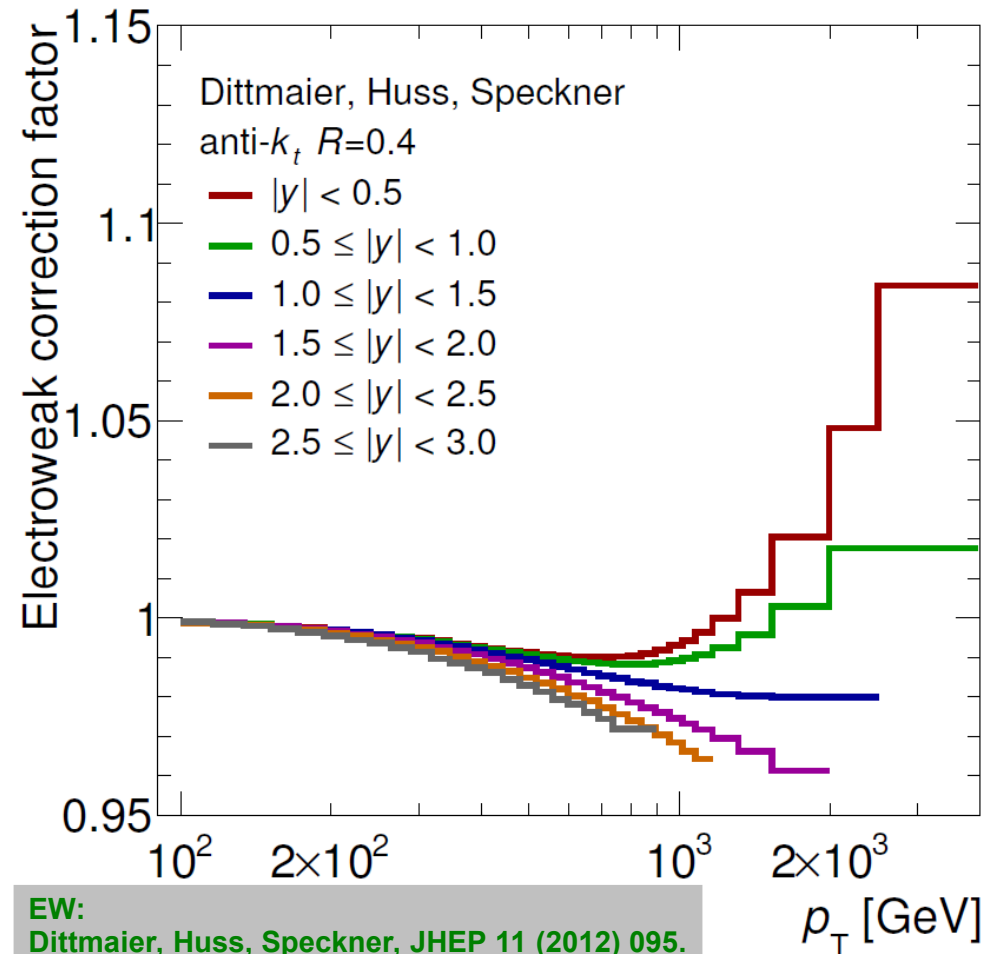
- estimated from tuned MC event generators
- uncertainty of 5 – 15% at  $p_T = 100$  GeV
- **strongly dependent on jet size R**
- less important at high  $p_T$

## Electroweak correction factors:

- calculated perturbatively
- uncertainty small
- **strongly dependent on jet rapidity y**
- very important at high  $p_T$



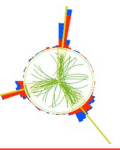
ALICE, arXiv:1909.09718.  
See also CMS, SMP-19-003.



EW:  
Dittmaier, Huss, Speckner, JHEP 11 (2012) 095.  
Frederix et al., JHEP 04 (2017) 076.

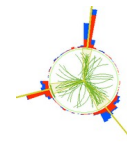


# Cross sections $\sim \alpha_s^3$



- As compared to  $\alpha_s^2$ :
  - ➔ Higher sensitivity
  - ➔ Smaller statistical precision
  - ➔ Smaller dynamical range
  - ➔ More scale choices
  - ➔ Theory at NNLO not available

# 3-jet mass

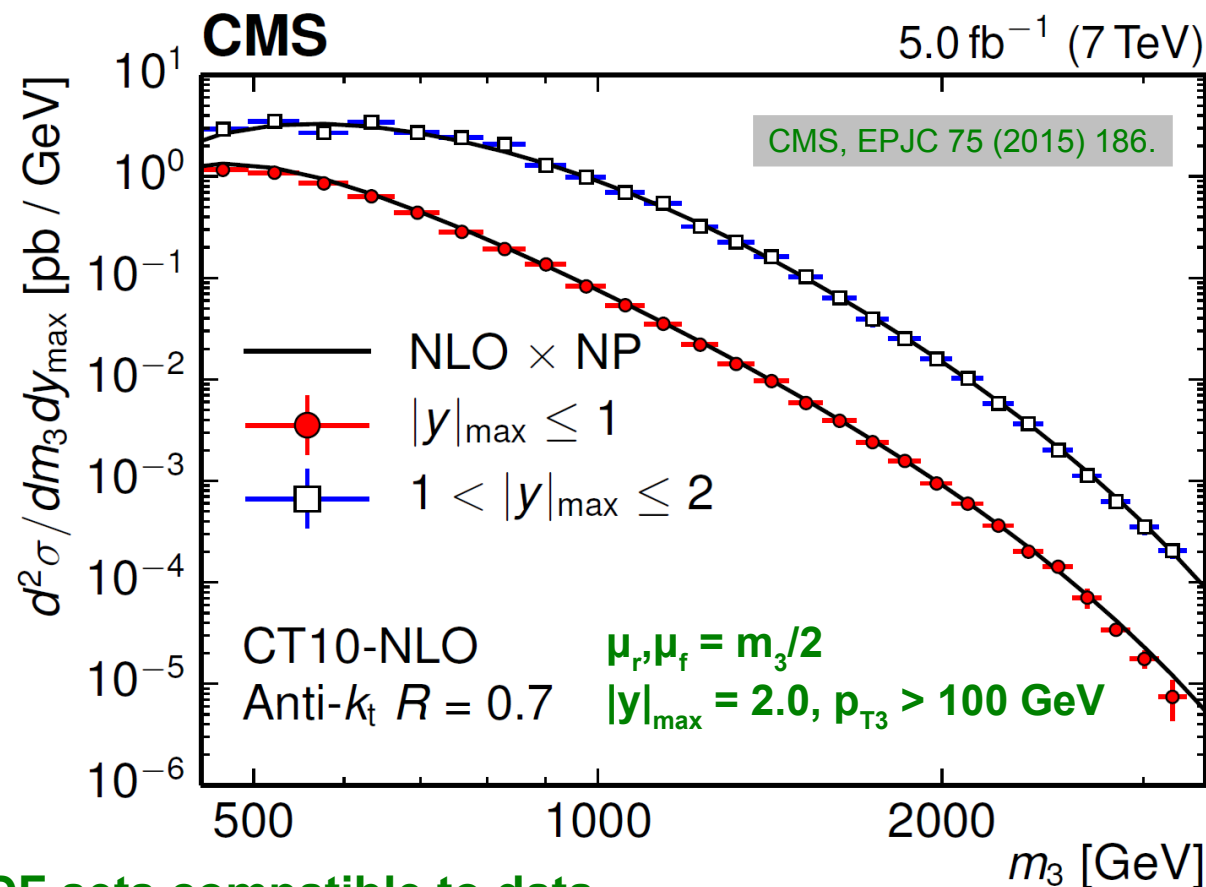
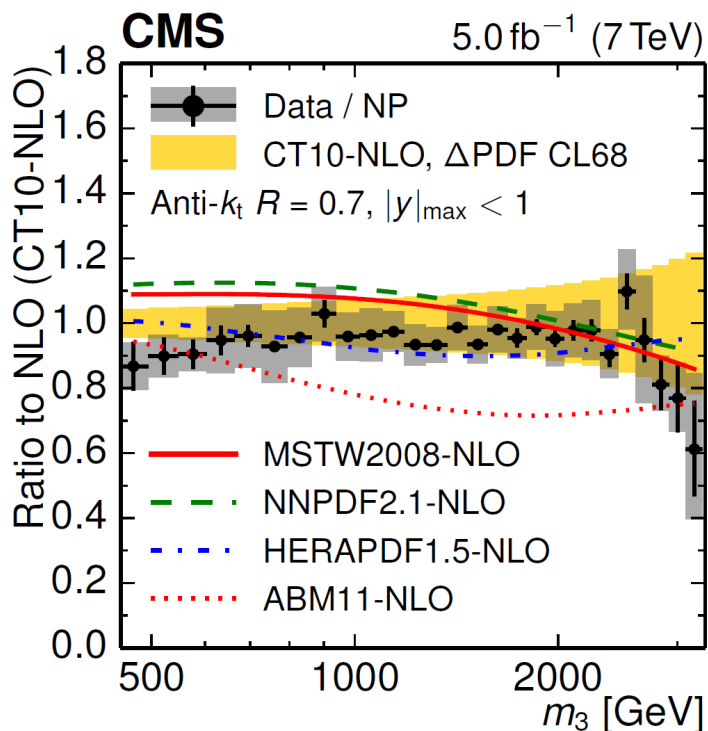


Sensitive to  $\alpha_s$  beyond 2→2 process

NLO with 3-4 partons (NLOJet++)

Sensitive to PDFs

Involves additional "scale"  $p_{T,3}$



Most PDF sets compatible to data

Extraction of  $\alpha_s(M_Z)$ :  $\rightarrow \alpha_s$

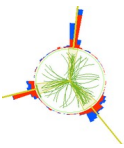
$$Q = m_3/2$$

$$\frac{d\sigma_{3jet}}{dm_{3jet}} \propto \alpha_s^3$$

$\sqrt{s}$ [TeV]	lum [fb <sup>-1</sup> ]	$\alpha_s(M_Z)$	exp NP PDF	scale
7	5.0	0.1171	28	+69 -40



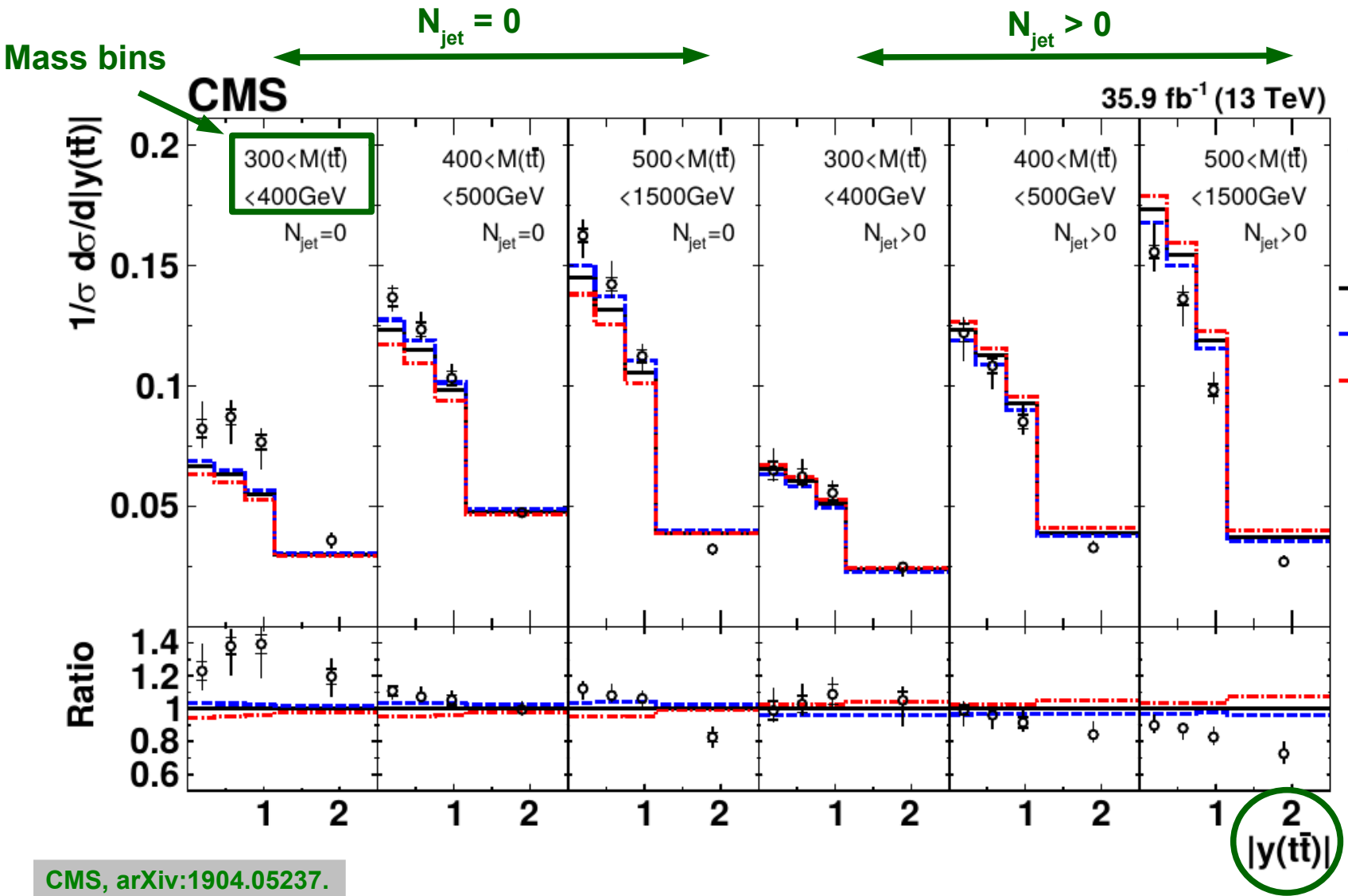
# Sensitivity of differential cross section



## Binning in $y(t\bar{t})$ , $M(t\bar{t})$ , and jet multiplicity $N_{jet}$

NLO

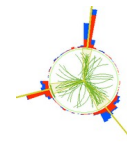
Normalised



CMS, arXiv:1904.05237.

### Initial description of data at NLO with CT14 PDFs for 3 values of $\alpha_s(M_Z)$

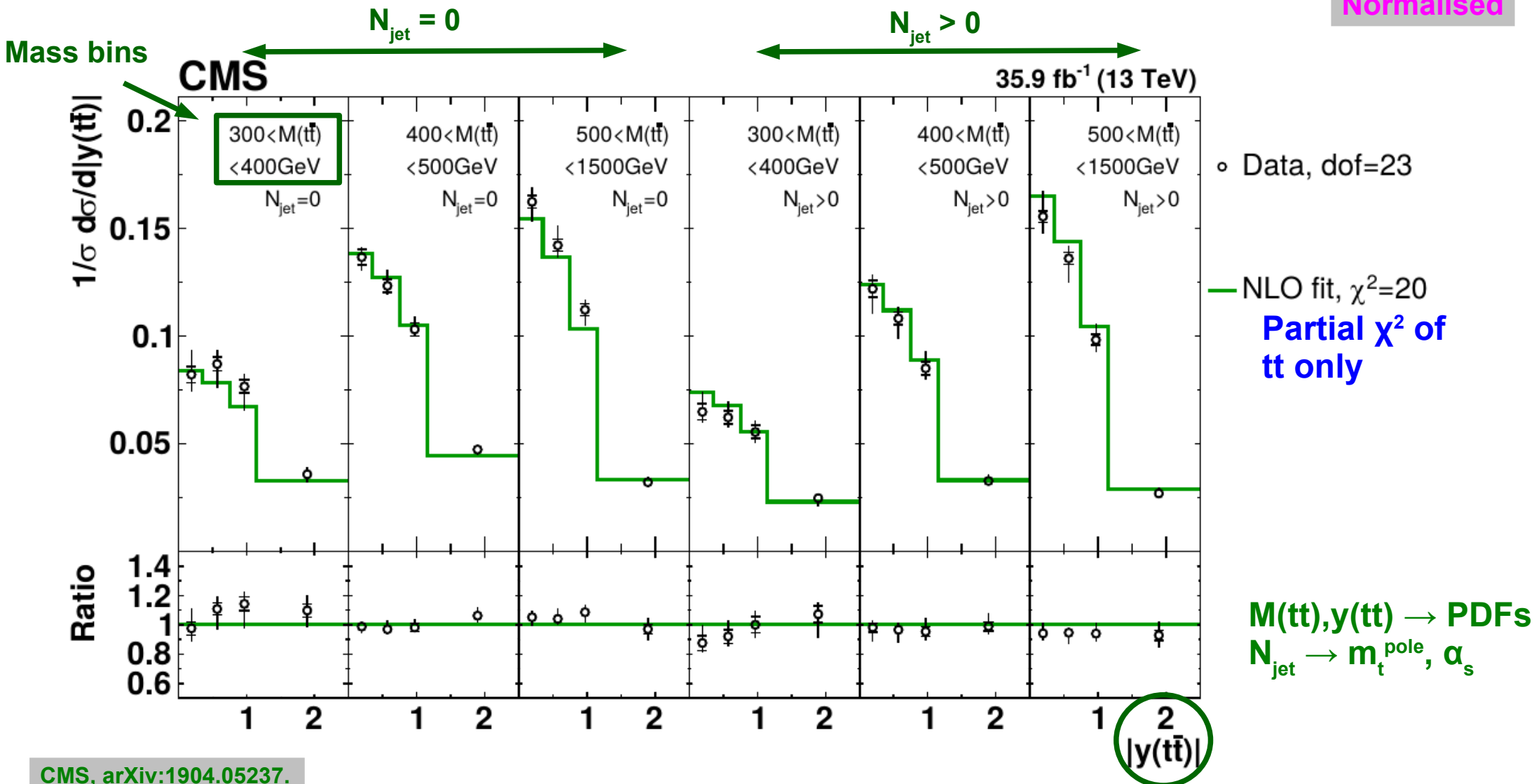
# Fits using $t\bar{t}$ differential distributions



Binning in  $y(t\bar{t})$ ,  $M(t\bar{t})$ , and jet multiplicity  $N_{jet}$

NLO

Normalised

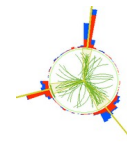


CMS, arXiv:1904.05237.

Description of data after fit of  $\alpha_s(M_Z)$ ,  $m_t^{\text{pole}}$ , PDFs to HERA +  $t\bar{t}$  data



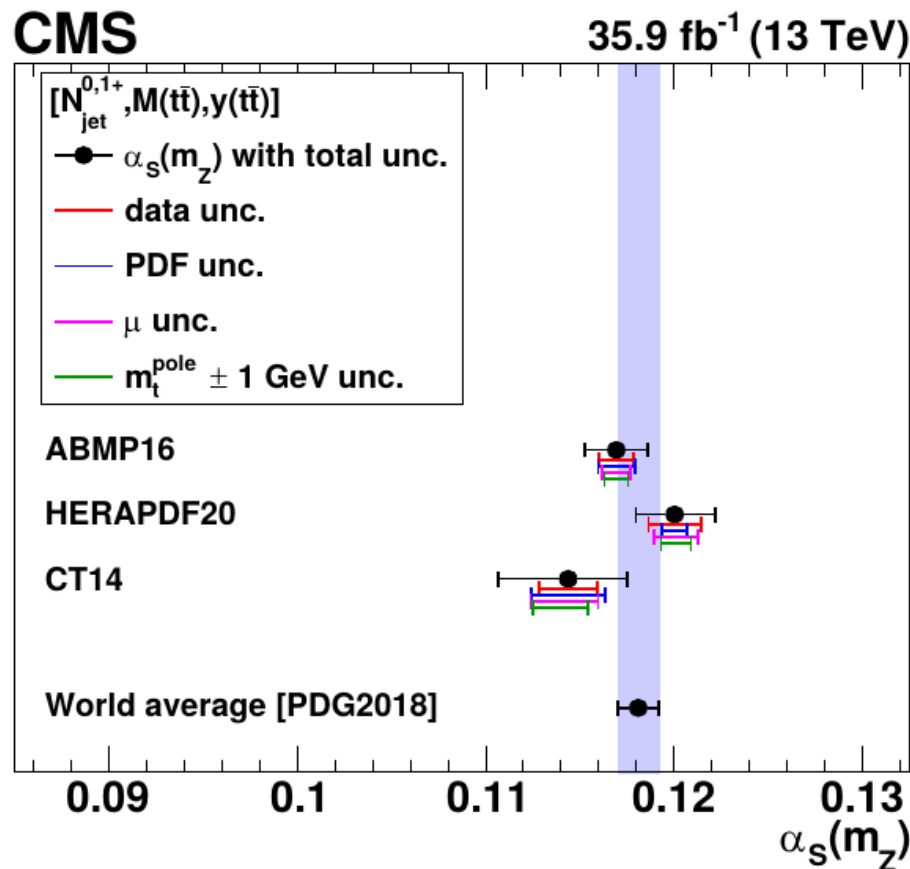
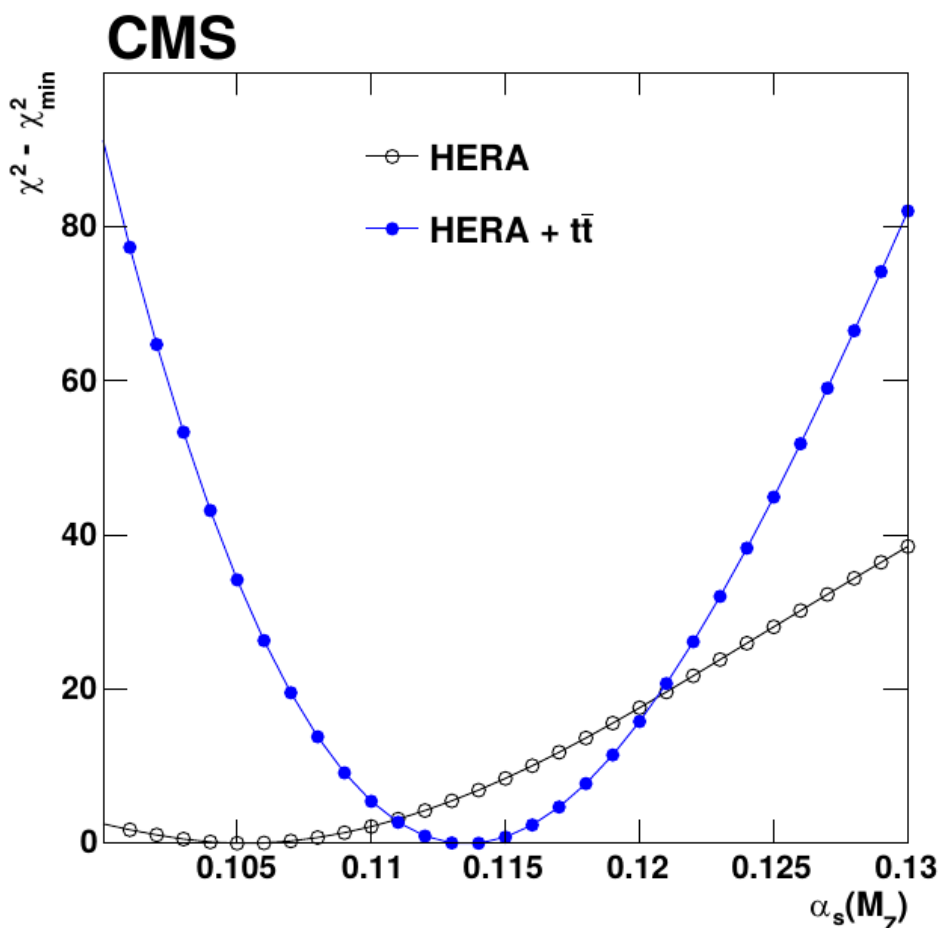
# Fits using $t\bar{t}$ differential distributions



NLO

Comparison of  $\chi^2$  for  $\alpha_s(M_Z)$  with HERA only and with additional  $t\bar{t}$  data

Cross check  $\alpha_s(M_Z)$  fit @ NLO with external PDFs ABMP16, HERAPDF20, and CT14

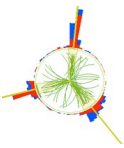


CMS, arXiv:1904.05237.





# Combining LHC & Tevatron $t\bar{t}$ data



- fitting procedure similar to CMS; **more conservative scale dependence treatment**
- combines results using NNLO or NNLO+NNLL for theory prediction
- updated and complemented set of  $t\bar{t}$  cross section measurements from LHC
- includes Tevatron results
- consideration of correlations among measurements
- combine results only from PDF sets without  $t\bar{t}$  data (CT14nnlo, NNPDF30\_nolhc)

## Datasets:

	$\sigma_{t\bar{t}}$ (pb)	Statistical unc. (%)	Systematic unc. (%)	Luminosity unc. (%)	$E_{\text{beam}}$ unc. (%)	Exp. $m_t$ unc. (%)
ATLAS (7 TeV) [16]	182.5	1.7	2.3	2.0	0.3	-0.2 +0.2
ATLAS (8 TeV) [16]	242.4	0.7	2.3	2.1	0.3	-0.2 +0.2
ATLAS (13 TeV) [17]	816.3	1.0	3.3	2.3	0.2	-0.3 +0.3
CMS (7 TeV) [13]	173.4	1.2	2.5	2.2	0.3	-0.2 +0.2
CMS (8 TeV) [13]	244.1	0.6	2.4	2.6	0.3	-0.4 +0.4
CMS (13 TeV) [14]	809.8	1.1	4.7	2.3	0.2	-0.8 +0.8
Tevatron (1.96 TeV) [18]	7.52	2.7	3.9	2.8	0.0	-1.1 +1.4

Bethke et al., NPPP 282-284 (2017) 139.