

From Lagrangian to Observable

Roger Wolf

13. Mai 2014

INSTITUTE OF EXPERIMENTAL PARTICLE PHYSICS (IEKP) – PHYSICS FACULTY



KIT – University of the State of Baden-Wuerttemberg and National Research Center of the Helmholtz Association

www.kit.edu

Recap from Last Time



 $V(\phi)$

• Introduced new field ϕ as SU(2) doublet in the theory:

$$\mathcal{L}^{SU(2)\times U(1)} = \mathcal{L}^{\text{kin}} + \mathcal{L}^{CC} + \mathcal{L}^{NC} + \mathcal{L}^{\text{gauge}} + \mathcal{L}^{\text{Higgs}}$$
$$\mathcal{L}^{\text{Higgs}} = \partial_{\mu}\phi^{+}\partial^{\mu}\phi - V(\phi)$$
$$V(\phi) = -\mu^{2}\phi^{+}\phi + \lambda \left(\phi^{+}\phi\right)^{2}$$

- Coupled ϕ to SU(2) gauge fields (via covariant derivate).
- Developed ϕ in its energy ground state and obtained massive gauge bosons, massive Higgs boson and massive fermions via coupling to ϕ :
 - Higgs boson obtains mass via *Goldstone* potential.
 - Gauge bosons obtain mass via gauge invariance requirement (→ covariant derivative).
 - Fermions obtain mass via "naïve" Yukawa coupling to ϕ .



- Wrap up: milestones in the formulation of the SM (including masses)?
- How does the Lagrangian density link to actual observables? How do we get from the paper work to something that is measurable?
- Review Feynman rules. What is a propagator? Does a Feynman graph have a time direction?
- What can we know already about the Higgs boson (mass) from within the theory.

Schedule for Today

Boundaries on the Higgs boson mass within the SM

3

2

From Lagrangian to observable (on trees and loops).

Milestones in the formulation of the SM & discussion







• Combine ν and e_L into a SU(2) doublet, which behaves like a vector in weak isospin space. Enforce local gauge invariance for \mathcal{L} . The e_R component of the electron behaves like a SU(2) singlet.

$$\psi_L = \begin{pmatrix} \nu \\ e \end{pmatrix}_L^{e_R} D_\mu = (\partial_\mu + igW_\mu)$$

 $\vartheta(\vec{x},t)$

- Description of weak interactions.
- Gauge bosons W_{μ}^{a} .
- To also obtain a description of the electromagnetic force additionally local gauge invariance is enforced for the U(1) symmetry on the doublet as a whole and on the singlet. $\psi(\vec{x},t) = g' = B_{\mu} = g' \psi(\vec{x'},t')$

Description of electromagnetic interactions ($W^a_\mu \& B_\mu$).

 $\vartheta(\vec{x'},t')$



• To achieve that the coupling to the ν is governed only by a single physical field, the fields W^3_{μ} and B_{μ} are rotated by the Weinberg angle θ_W .

 $\begin{pmatrix} Z_{\mu} \\ A_{\mu} \end{pmatrix} = \begin{pmatrix} \cos \theta_W & -\sin \theta_W \\ \sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} W_{\mu}^3 \\ B_{\mu} \end{pmatrix}$ $\sin \theta_W = \frac{g'}{\sqrt{g^2 + g'^2}} \quad \cos \theta_W = \frac{g}{\sqrt{g^2 + g'^2}}$

• Obtain physical fields $(Z_{\mu} \& A_{\mu})$.

Step 3: Higgs Mechanism



• To obtain mass terms for the massive gauge bosons introduce a new field ϕ with a potential that leads to spontaneous symmetry breaking for this field. The gauge fields are coupled to ϕ via the covariant derivative $D_{\mu}\phi$.

- Masses for gauge bosons (m_Z & m_W).
- Massive Higgs boson *H*.
- Couplings of gauge bosons to $H \propto m_{W/Z}^2 H.$



• To obtain mass terms for fermions couple the fermion fields to ϕ via *Yukawa* couplings.

• Couplings of fermions $\propto m_f H$.

SM Full Lagrangian



$$\begin{split} L^{\rm SM} &= L_{\rm kin}^{\rm Lepton} + L_{\rm IA}^{CC} + L_{\rm IA}^{NC} + L_{\rm kin}^{\rm Gauge} + L_{kin}^{\rm Higgs} + L_{V(\phi)}^{\rm Higgs} + L_{\rm Yukawa}^{\rm Higgs} \\ L_{\rm kin}^{\rm Lepton} &= i \overline{e} \gamma^{\mu} \partial_{\mu} e + i \overline{\nu} \gamma^{\mu} \partial_{\mu} \nu \\ L_{\rm IA}^{\rm CC} &= -\frac{e}{\sqrt{2 \sin \theta_W}} \left[W_{\mu}^{+} \overline{\nu} \gamma_{\mu} e_L + W_{\mu}^{-} \overline{e}_L \gamma_{\mu} \nu \right] \\ L_{\rm IA}^{NC} &= -\frac{e}{2 \sin \theta_W \cos \theta_W} Z_{\mu} \left[(\overline{\nu} \gamma_{\mu} \nu) + (\overline{e}_L \gamma_{\mu} e_L) \right] - e \left[A_{\mu} + \tan \theta_W Z_{\mu} \right] (\overline{e} \gamma_{\mu} e) \\ L_{\rm Kin}^{\rm Gauge} &= -\frac{1}{2} Tr \left(W_{\mu\nu}^{a} W^{a\mu\nu} \right) - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} \Big| \begin{array}{c} B_{\mu} \to A_{\mu} \\ W_{\mu}^{3} \to Z_{\mu} \end{array} \\ L_{kin}^{\rm Higgs} &= \frac{1}{2} \partial_{\mu} H \partial^{\mu} H + \left(1 + \sqrt{\frac{\lambda}{\mu^{2}}} H \right)^{2} m_{W}^{2} W_{\mu}^{+} W^{\mu-} + \left(1 + \sqrt{\frac{\lambda}{\mu^{2}}} H \right)^{2} m_{Z}^{2} Z_{\mu} Z^{\mu} \\ L_{V(\phi)}^{\rm Higgs} &= -\frac{\mu^{4}}{4\lambda} + \frac{\mu^{2}}{2} H^{2} + \mu \sqrt{\lambda} H^{3} + \frac{\lambda}{4} H^{4} \\ L_{\rm Yukawa}^{\rm Higgs} &= - \left(1 + \sqrt{\frac{\lambda}{\mu^{2}}} H \right) m_{e}^{2} \overline{e} e \end{split}$$

Questions???



• Is there any further questions or need for discussion on your side that we can address in the scope of this lecture?



Lagrangian Density \rightarrow Observable







 \mathcal{L}



- Review the QM model of scattering wave.
- Turning the Dirac equation from a differential equation into an integral equation (→ Green's functions).
- Iterative solution of the integral equation with the help of perturbation theory.
- Finding the solution for A_{μ} when the target particle is moving (\rightarrow photon propagator).
- 1st oder full solution and the Feynman rules.

QM Model of Particle Scattering



• Consider incoming collimated beam of projectile particles on target particle:



QM Model of Particle Scattering



• Consider incoming collimated beam of projectile particles on target particle:



Solution for $\psi_{ m scat}$



• In the case of fermion scattering the scattering wave ψ_{scat} is obtained as a solution of the *Dirac* equation for an interacting field:

$$(i\gamma^{\mu}\partial_{\mu}-m)\psi_{
m scat}=-eA_{\mu}\psi_{
m scat}$$
 (+)

• The inhomogeneous *Dirac* equation is analytically not solvable.

Solution for $\psi_{ m scat}$ (*Green's* Function)



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• The inhomogeneous *Dirac* equation is analytically not solvable. A formal solution can be obtained by the *Green's* Function K(x - x'):

$$(i\gamma^{\mu}\partial_{\mu} - m) K(x - x') = \delta^4(x - x')$$

$$\psi_{\rm scat}(x) = -e \int K(x - x') \gamma^{\mu} A_{\mu}(x') \psi_{\rm scat}(x') d^4 x'$$

$$(i\gamma^{\mu}\partial_{\mu} - m)\psi_{\text{scat}}(x) = -e\int \underbrace{(i\gamma^{\mu}\partial_{\mu} - m)K(x - x')\gamma^{\mu}A_{\mu}(x')\psi_{\text{scat}}(x')d^{4}x'}_{\delta^{4}(x - x')}$$
$$= -eA_{\mu}(x)\psi(x)$$

Solution for ψ_{scat} (*Green's* Function)



• In the case of fermion scattering the scattering wave ψ_{scat} is obtained as a solution of the *Dirac* equation for an interacting field:

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 $\left|\psi_{\mathrm{scat}}(x) = -e\int K(x-x')\gamma^{\mu}A_{\mu}(x')\psi_{\mathrm{scat}}(x')\mathrm{d}^{4}x'
ight|$

NB: this is not a solution to (+), since ψ_{scat} appears on the left- and on the righthand side of the equation. But it turns the differential equation into an integral equation.



• The best way to find the *Green's* function is to use the *Fourier* transform:

 $K(x - x') = (2\pi)^{-4} \int \tilde{K}(p) e^{-ip(x - x')} d^4p$ (Fourier transform)

• Applying the *Dirac* equation to the *Fourier* transform of K(x - x') turns the derivative into a product operator:

$$\underbrace{(i\gamma^{\mu}\partial_{\mu} - m)K(x - x')}_{\parallel} = (2\pi)^{-4} \int \underbrace{(\gamma^{\mu}p_{\mu} - m)\tilde{K}(p)e^{-ip(x - x')}d^{4}p}_{\parallel} \\ = (2\pi)^{-4} \int \underbrace{\mathbb{I}_{4}}_{\parallel} e^{-ip(x - x')}d^{4}p$$



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• From the uniqueness of the *Fourier* transformation the solution for $\tilde{K}(p)$ follows:

$$(\gamma^{\mu}p_{\mu} - m) \tilde{K}(p) = \mathbb{I}_{4}$$
$$(\gamma^{\mu}p_{\mu} + m) \cdot (\gamma^{\mu}p_{\mu} - m) \tilde{K}(p) = (\gamma^{\mu}p_{\mu} + m) \cdot \mathbb{I}_{4}$$



$$(\gamma^{\mu}p_{\mu}+m)\cdot(\gamma^{\mu}p_{\mu}-m)\,\tilde{K}(p)=(\gamma^{\mu}p_{\mu}+m)\cdot\mathbb{I}_{4}$$



$$(\gamma^{\mu}p_{\mu}+m)\cdot(\gamma^{\mu}p_{\mu}-m)\,\tilde{K}(p)=(\gamma^{\mu}p_{\mu}+m)\cdot\mathbb{I}_{4}$$

- The Fermion propagator is a 4×4 matrix, which acts in the Spinor room.
- It is only defined for virtual electrons since $p^2 m^2 = E^2 \vec{p}^2 m^2 \neq 0$.



$$(\gamma^{\mu}p_{\mu}+m)\cdot(\gamma^{\mu}p_{\mu}-m)\,\tilde{K}(p)=(\gamma^{\mu}p_{\mu}+m)\cdot\mathbb{I}_{4}$$

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- The *Green's* function can be obtained from $\tilde{K}(p)$ by:

$$K(x - x') = (2\pi)^{-4} \int d^3 \vec{p} \, e^{i\vec{p}(\vec{x} - \vec{x'})} \int_{-\infty}^{+\infty} dp_0 \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$



$$(\gamma^{\mu}p_{\mu}+m)\cdot(\gamma^{\mu}p_{\mu}-m)\,\tilde{K}(p)=(\gamma^{\mu}p_{\mu}+m)\cdot\mathbb{I}_{4}$$

- The Fermion propagator is a 4×4 matrix, which acts in the Spinor room.
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- K(x x') has two poles in the integration plane (at $p_0 = \pm E$).
- The integral can be solved with the methods of *function theory*.

The Fermion Propagator (Time Integration t > t')

• Choose path *C* in complex plain to circumvent poles and at the same time imply proper time evolution:

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \, \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$

For t > t' (e^{-ip₀(t-t')} → 0 for Im(p₀) ≪ 0):
 → close contour in lower plane & calculate integral from residual of enclosed pole.

$$\oint_{\mathcal{C}} dp_0 \frac{1}{p_0 - E} \cdot \frac{(\gamma^{\mu} p_{\mu} + m)}{p_0 + E} e^{-ip_0(t - t')} = -2\pi i \cdot f(p_0)|_{p_0 = E}$$
pole at:

$$p_0 = +E$$
residuum: $f(p_0)$
Sign due to sense of integration.

$$p_{0} = -E$$

$$p_{0} = -E$$

$$p_{0} = +E$$

$$Re(p_{0})$$

$$t > t'$$

$$C: R \to \infty$$



The Fermion Propagator (Time Integration
$$t > t'$$
)

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \, \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$

$$p_{0} = -E$$

$$p_{0} = +E$$

$$Re(p_{0})$$

$$t > t'$$

$$C: R \to \infty$$

$$\oint_{\mathcal{C}} \mathrm{d}p_0 \frac{1}{p_0 - E} \cdot \frac{(\gamma^{\mu} p_{\mu} + m)}{p_0 + E} e^{-ip_0(t - t')} = -2\pi i \cdot f(p_0)|_{p_0 = E}$$
$$K(x - x') = -i(2\pi)^3 \int \mathrm{d}^3 \vec{p} \, \frac{+\gamma^0 E - \vec{\gamma} \vec{p} + m}{2E} \cdot e^{-iE(t - t') + i\vec{p}(\vec{x} - \vec{x'})}$$





The Fermion Propagator (Time Integration t < t')

 Choose path C in complex plain to circumvent poles and at the same time imply proper time evolution:

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \, \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$

For t < t' (e^{+ip₀(t-t')} → 0 for Im(p₀) ≫ 0):
 → close contour in upper plane & calculate integral from residual of enclosed pole.

$$\oint_{\mathcal{C}} dp_0 \frac{1}{p_0 + E} \cdot \frac{(\gamma^{\mu} p_{\mu} + m)}{p_0 - E} e^{-ip_0(t - t')} = +2\pi i \cdot f(p_0)|_{p_0 = E}$$
pole at:

$$p_0 = -E$$
residuum: $f(p_0)$
Sign due to sense of integration.





$$\oint_{\mathcal{C}} \mathrm{d}p_0 \frac{1}{p_0 + E} \cdot \frac{(\gamma^{\mu} p_{\mu} + m)}{p_0 - E} e^{-ip_0(t - t')} = +2\pi i \cdot f(p_0)|_{p_0 = E}$$
$$K(x - x') = -i(2\pi)^3 \int \mathrm{d}^3 \vec{p} \, \frac{-\gamma^0 E - \vec{\gamma} \vec{p} + m}{2E} \cdot e^{+iE(t - t') + i\vec{p}(\vec{x} - \vec{x'})}$$

• Choose path ${\mathcal C}$ in complex plain to

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} e^{-ip_0(t - t')}$$

$$C: R \to \infty$$

$$p_0 = -E$$

$$p_0 = -E$$

$$p_0 = +E$$

$$Re(p_0)$$

The Fermion Propagator (Time Integration
$$t < t'$$
)



The Fermion Propagator (Nota Bene)



 Choose path C in complex plain to circumvent poles and at the same time imply proper time evolution:

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \, \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$



• The bending of the integration path can be circumvented by shifting the poles by ϵ .

$$\left[p_0 + \left(E - \frac{i\epsilon}{2E}\right)\right] \cdot \left[p_0 - \left(E - \frac{i\epsilon}{2E}\right)\right] = p_0^2 - \left(\vec{p}^2 + m^2\right) + i\epsilon$$
$$= p^2 - m^2 + i\epsilon$$



The Fermion Propagator (Nota Bene)



 Choose path C in complex plain to circumvent poles and at the same time imply proper time evolution:

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$$= p^2 - m^2 + i\epsilon$$
$$(+E, -\frac{\epsilon}{2E})$$

The Fermion Propagator (Nota Bene)



 Choose path C in complex plain to circumvent poles and at the same time imply proper time evolution:

$$\int_{-\infty}^{+\infty} \mathrm{d}p_0 \, \frac{(\gamma^{\mu} p_{\mu} + m)}{(p_0 - E)(p_0 + E)} \, e^{-ip_0(t - t')}$$



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$$= p^2 - m^2 + i\epsilon$$
$$\tilde{K}(p) = \frac{(\gamma^\mu p_\mu + m)}{p^2 - m^2 + i\epsilon} \quad \epsilon > 0$$

• Fermion Propagator:

$$\tilde{K}(p) = \frac{(\gamma^{\mu} p_{\mu} + m)}{p^2 - m^2 + i\epsilon} \qquad \epsilon > 0$$

• *Green's* function (for t > t'):

$$K(x - x') = -i(2\pi)^3 \int d^3 \vec{p} \, \frac{+\gamma^0 E - \vec{\gamma} \vec{p} + m}{2E} \cdot e^{-iE(t - t') + i\vec{p}(\vec{x} - \vec{x'})}$$

$$\phi(t, \vec{x}) = \begin{cases} i \int d^3 \vec{x}' K(x - x') \gamma^0 \phi(t', \vec{x}') & \text{for} \quad t > t' \\ 0 & \text{for} \quad t < t' \end{cases}$$

particle w/ pos. energy traveling forward in time.

$$\overline{\phi}(t, \vec{x}) = \begin{cases} 0 & \text{for } t > t' \\ i \int d^3 \vec{x}' \overline{\phi}(t', \vec{x}') \gamma^0 K(x - x') & \text{for } t < t' \end{cases}$$

particle w/ pos. energy traveling backward in time.



• Check the highlighted equation.

• Fermion Propagator:

$$\tilde{K}(p) = \frac{(\gamma^{\mu}p_{\mu} + m)}{p^2 - m^2 + i\epsilon} \qquad \epsilon > 0$$

• *Green's* function (for t < t'):

$$K(x - x') = -i(2\pi)^3 \int d^3 \vec{p} \, \frac{-\gamma^0 E - \vec{\gamma} \vec{p} + m}{2E} \cdot e^{+iE(t - t') + i\vec{p}(\vec{x} - \vec{x'})}$$

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particle w/ neg. energy traveling forward in time.

$$\overline{\phi}(t, \vec{x}) = \begin{cases} i \int \mathrm{d}^3 \vec{x}' \overline{\phi}(t', \vec{x}') \gamma^0 K(x - x') & \text{for} \quad t > t' \\ 0 & \text{for} \quad t < t' \end{cases}$$

particle w/ neg. energy traveling backward in time.

Solution for $\psi_{ m scat}$ (Perturbative Series)



• The integral equation can be solved perturbatively:

 $\psi_{\text{scat}}(x) = -e \int K(x - x') \gamma^{\mu} A_{\mu}(x') \psi_{\text{scat}}(x') d^4x'$

• 0th order perturbation theory:

 $\psi^{(0)}(x_f) = \phi_i(x_f)$

(solution of the homogeneous *Dirac* equation)

Solution for $\psi_{ m scat}$ (Perturbative Series)



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 $\psi_{\text{scat}}(x) = -e \int K(x - x') \gamma^{\mu} A_{\mu}(x') \psi_{\text{scat}}(x') d^4x'$

• 0th order perturbation theory:

 $\psi^{(0)}(x_f) = \phi_i(x_f)$

• 1st order perturbation theory:

$$\psi^{(1)}(x_f) = \psi^{(0)}(x_f) -e \int K(x_f - x') \gamma^{\mu} A_{\mu}(x') \psi^{(0)}(x') d^4 x'$$
Solution for $\psi_{ m scat}$ (Perturbative Series)



• The integral equation can be solved perturbatively:

 $\psi_{\text{scat}}(x) = -e \int K(x - x') \gamma^{\mu} A_{\mu}(x') \psi_{\text{scat}}(x') d^{4}x'$

• 0th order perturbation theory:

 $\psi^{(0)}(x_f) = \phi_i(x_f)$

• 1st order perturbation theory:

$$\psi^{(1)}(x_f) = \psi^{(0)}(x_f) -e \int K(x_f - x') \gamma^{\mu} A_{\mu}(x') \psi^{(0)}(x') d^4 x'$$

• 2nd order perturbation theory:

$$\psi^{(2)}(x_f) = \psi^{(0)}(x_f)$$

- $e \int K(x_f - x') \gamma^{\mu} A_{\mu}(x') \psi^{(0)}(x') d^4 x'$
- $e^2 \int \int K(x_f - x'') \gamma^{\mu} A_{\mu}(x'') K(x'' - x') \gamma^{\mu} A_{\mu}(x') \psi^{(0)}(x') d^4 x' d^4 x''$



• The integral equation can be solved perturbatively:

 $\psi_{\text{scat}}(x) = -e \int K(x - x') \gamma^{\mu} A_{\mu}(x') \psi_{\text{scat}}(x') d^4x'$

- 0th order perturbation theory: $\psi^{(0)}(x_f) = \phi_i(x_f)$
- 1st order perturbation theory:

This procedure is justified since e (in natural units) is small wrt. to 1:

$$\alpha = \frac{e^2}{4\pi\hbar c} \quad \hbar = c = 1 \quad \blacktriangleright \quad \alpha = \frac{e^2}{4\pi} \approx \frac{1}{137}$$

$$\psi^{(1)}(x_f) = \psi^{(0)}(x_f) -e \int K(x_f - x') \gamma^{\mu} A_{\mu}(x') \psi^{(0)}(x') d^4x'$$

• 2nd order perturbation theory:

$$\psi^{(2)}(x_f) = \psi^{(0)}(x_f)$$

- $e \int K(x_f - x')\gamma^{\mu}A_{\mu}(x')\psi^{(0)}(x')d^4x'$
- $e^2 \int \int K(x_f - x'')\gamma^{\mu}A_{\mu}(x'')K(x'' - x')\gamma^{\mu}A_{\mu}(x')\psi^{(0)}(x')d^4x'd^4x''$

The Matrix Element \mathcal{S}_{fi}



• S_{fi} is obtained from the projection of the scattering wave ψ_{scat} on ϕ_f :

$$S_{fi} = \int d^3 \vec{x}_f \phi_f^{\dagger}(x_f) \psi_{\text{scat}}(x_f) = \int d^3 \vec{x}_f \phi_f^{\dagger}(x_f) S \phi_i(x_f)$$
$$= \delta_{fi} + S_{fi}^{(1)} + S_{fi}^{(2)} + \dots$$

• 1st order perturbation theory:

$$S_{fi}^{(1)} = -e \int d^4x' \int d^3x_f \phi_f^{\dagger}(x_f) K(x_f - x') \gamma^{\mu} A_{\mu}(x') \phi_i(x')$$

$$\equiv -i \overline{\phi}_f(x')$$

$$S_{fi}^{(1)} = i \cdot e \int d^4x' \overline{\phi}_f(x') \gamma^{\mu} A_{\mu}(x') \phi_i(x')$$

corresponds to the
IA term in \mathcal{L} .

The Matrix Element \mathcal{S}_{fi}



• S_{fi} is obtained from the projection of the scattering wave ψ_{scat} on ϕ_f :

$$\mathcal{S}_{fi} = \int \mathrm{d}^3 \vec{x}_f \phi_f^{\dagger}(x_f) \psi_{\mathrm{scat}}(x_f) = \int \mathrm{d}^3 \vec{x}_f \phi_f^{\dagger}(x_f) \mathcal{S} \phi_i(x_f)$$
$$= \delta_{fi} + \mathcal{S}_{fi}^{(1)} + \mathcal{S}_{fi}^{(2)} + \dots$$

• 1st order perturbation theory:

$$S_{fi}^{(1)} = -e \int d^4x' \int d^3x_f \phi_f^{\dagger}(x_f) K(x_f - x') \gamma^{\mu} A_{\mu}(x') \phi_i(x')$$

$$\equiv -i \overline{\phi}_f(x')$$

$$S_{fi}^{(1)} = i \cdot e \int d^4x' \overline{\phi}_f(x') \gamma^{\mu} A_{\mu}(x') \phi_i(x')$$

$$\text{ corresponds to the lA term in } \mathcal{L}.$$

The Matrix Element \mathcal{S}_{fi}



• S_{fi} is obtained from the projection of the scattering wave ψ_{scat} on ϕ_f :

$$S_{fi} = \int d^3 \vec{x}_f \phi_f^{\dagger}(x_f) \psi_{\text{scat}}(x_f) = \int d^3 \vec{x}_f \phi_f^{\dagger}(x_f) S \phi_i(x_f)$$
$$= \delta_{fi} + S_{fi}^{(1)} + S_{fi}^{(2)} + \dots$$

• 1st order perturbation theory:

$$S_{fi}^{(1)} = -e \int d^4x' \int d^3x_f \phi_f^{\dagger}(x_f) K(x_f - x') \gamma^{\mu} A_{\mu}(x') \phi_i(x')$$

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$$S_{fi}^{(1)} = i \cdot e \int d^4x' \overline$$



- Since the target particle is back scattered by the projectile, A_{μ} also evolves.
- This happens according to the inhomogeneous wave equation of the photon field (in *Lorentz* gauge $\partial_{\mu}A^{\mu} = 0$):

 $\Box A^{\mu} = e J^{\mu}$

• Ansatz via Green's function ...:

 $\Box D^{\mu\nu}(x - x') = g^{\mu\nu} \delta^4(x - x') \qquad A^{\mu}(x) = e \int d^4 x' D^{\mu\nu}(x - x') J_{\nu}(x')$ $\Box A^{\mu}(x) = e \int d^4 x' \Box D^{\mu\nu}(x - x') J_{\nu}(x') = e J^{\mu}(x)$



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• ... and Fourier transform:

$$D^{\mu\nu}(x-x') = (2\pi)^{-4} \int d^4q \tilde{D}^{\mu\nu}(q) e^{-iq(x-x')}$$
$$\Box D^{\mu\nu}(x-x') = (2\pi)^{-4} \int d^4q (-q^2) \tilde{D}^{\mu\nu}(q) e^{-iq(x-x')} \stackrel{!}{=} g^{\mu\nu} \delta^4(x-x')$$



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• ... and *Fourier* transform:

 $D^{\mu\nu}(x-x') = (2\pi)^{-4} \int d^4q \tilde{D}^{\mu\nu}(q) e^{-iq(x-x')}$ $\tilde{D}^{\mu\nu}(q) = \frac{-g^{\mu\nu}}{q^2+i\epsilon} \quad (\epsilon > 0) \quad \text{(Photon propagator)}$



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$$eJ^{\mu}(x) = e \cdot \overline{\psi}_f(x)\gamma^{\mu}\psi_i(x) = e \cdot \overline{u}(p_4)\gamma^{\mu}u(p_2)e^{i(p_4-p_2)x}$$

$$\psi_i(x) = u(p_2)e^{-ip_2x}$$
 $\psi_f(x) = u(p_4)e^{-ip_4x}$

• Introduce current and photon propagator into A_{μ} :

$$A^{\mu}(x) = e \cdot \int d^4x' \int \frac{d^4q}{(2\pi)^4} \cdot \frac{-g^{\mu\nu}}{q^2 + i\epsilon} e^{i(p_4 - p_2 + q)x'} e^{-iqx} \overline{u}(p_4) \gamma^{\nu} u(p_2)$$

$$= e \cdot \int \mathrm{d}^4 q \frac{-g^{\mu\nu}}{q^2 + i\epsilon} \delta^4 (p_4 - p_2 + q) e^{-iqx} \overline{u}(p_4) \gamma^{\nu} u(p_2)$$





 $u(p_4)$

 $u(p_2)$

target

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$$= e \cdot \int d^4 q \frac{-g^{\mu\nu}}{q^2 + i\epsilon} \delta^4(p_4 - p_2 + q) e^{-iqx} \overline{u}(p_4) \gamma^{\nu} u(p_2)$$

• Introduce A_{μ} and projectile Spinors into S_{fi} :

$$\phi_i(x) = u(p_1)e^{-ip_1x} \quad \phi_f(x) = u(p_3)e^{-ip_3x}$$



projectile















Feynman Rules (QED)



- *Feynman* diagrams are a way to represent the elements of the matrix element.
- The translation follows the *Feynman* rules:

Legs:	$u(p)$ $(\overline{u}(p))$	 Incoming (outgoing) lepton.
	$\epsilon_{\mu}(k)~~(\epsilon^{*}_{\mu}(k))$	 Incoming (outgoing) photon.
Vertexes:	$i(+a)$ $(2-)^4$ $\delta^4(m-m-a)$	
•	$-i(\pm e)\cdot(2\pi)^{-}\cdot o^{-}(p_f-p_i-q)$	 Lepton-photon vertex.
Propagators		
• • • •	$\frac{i(\gamma^{\mu}p_{\mu}+m)}{p^2-m^2+i\epsilon}$	 Incoming (outgoing) lepton.
••	$\frac{-ig^{\mu\nu}}{q^2+i\epsilon}$	 Incoming (outgoing) lepton.

• Four-momenta of all virtual particles have to be integrated out.



- *Feynman* diagrams are a way to represent the elements of the matrix element.
- A Feynman diagram:
 - is not a sketch, it is a mathematical representation!
 - is drawn in momentum space.
 - does not have a time direction. Only time information is introduced by choice of initial and final state by reader (e.g. t-channel vs s-channel processes).

Higher Order



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- Scattering amplitude S_{fi} is only known in perturbation theory.
- Works the better the smaller the perturbation is (= the coupling const.).
 - QED: $\alpha_{\rm em} \approx \frac{1}{137}$
 - QFD: $\alpha_{\rm w} = \alpha_{\rm em} / \sin^2(\theta_W) \approx 4 \cdot \alpha_{\rm em}$ $\theta_W = 28.74^{\circ}$
 - QCD: $\alpha_s(m_Z) \approx 0.12$
- If perturbation theory works well, the first contribution of the scattering amplitude is already sufficient to describe the main features of the process.
- This contribution is of order " α ". It is often called *Tree Level*, *Born Level* or *Leading Order* (LO) scattering amplitude.
- Any higher order of the scattering amplitude in perturbation theory appears at higher orders of " α ".



- We have only discussed contribution to S_{fi}, which are of order α¹ in QED.
 (e.g. LO ee → ee scattering).
- Diagrams which contribute to order α^2 would look like this:





(loops in propagators or legs)



(loops in vertexes)



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- LO term for a $2 \rightarrow 4$ process.
- NLO contrib. for the $2 \rightarrow 2$ process.
- Open phase spaces.



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(loops in propagators or legs)

 Modify (effective) masses of particles ("running masses").

Loops:



(loops in vertexes)



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 (e.g. LO ee → ee scattering).
- Diagrams which contribute to order α^2 would look like this:

Additional legs:



- LO term for a $2 \rightarrow 4$ process.
- NLO contrib. for the $2 \rightarrow 2$ process.
- Open phase spaces.



(loops in propagators or legs)

 Modify (effective) masses of particles ("running masses"). Loops:



(loops in vertexes)

 Modify (effective) couplings of particles ("running couplings").

Examples for "Running Constants"







- Running of the constants can be predicted and indeed are observed.
- But they need to be measured at least in one point.
- One usually gives the value at a reference scale (e.g. m_Z).

Effect of Higher Order Corrections



- Change over all normalization of cross sections (e.g. via change of coupling, but also by kinematic opening of phase space large effect)
- Change kinematic distributions (e.g. harder or softer transverse momentum spectrum of particles)
- In QED effects are usually "small" (correction to LO is already at O(1%) level).
 In QCD effects are usually "large" (O(10%)). Therefore reliable QCD predictions almost always require (N)NLO.
- Higher orders can be mixed (e.g. $O(\alpha \alpha_s^2)$).
- In concrete calculations the number of contributing diagrams quickly explodes for higher order calculations, which makes these calculations very difficult.

Boundaries on the Higgs Mass within the SM







• Like the couplings α_{em} , α_w and α_s also the self-coupling λ in the Higgs potential is subject to higher order corrections:

$$\mathcal{L}_{V(\phi)}^{\text{Higgs}} = -\frac{\mu^4}{4\lambda} + \frac{\mu^2}{2}H^2 + \mu\sqrt{\lambda}H^3 + \frac{\lambda}{4}H^4 \quad \text{(Higgs potential)}$$

$$\frac{d\lambda}{d \log Q^2} = \frac{1}{16\pi^2} \left[12\lambda^2 + 6\lambda f_t^2 - 3f_t^4 - \frac{3}{2}\lambda \left(3\alpha_{em}^2 + \alpha_w^2 \right) + \dots \right]$$

Higgs top quark (Renormalization group equation at 1-loop accuracy)

• Since the Higgs boson couples proportional to the mass the high energy behavior of λ will be dominated by the heaviest object in the loop.



• First case: large Higgs mass ($m_H \gg Q^2$)



- For $Q^2 \ll v^2 = 246 \,\text{GeV}$ we get $\log (Q^2/v^2) \ll 0$ and $\lambda(Q^2) \to 0$.
- For increasing $Q^2 \lambda(Q^2)$ will run into a pole and become non-perturbative!



• First case: large Higgs mass ($m_H \gg Q^2$)



• From this (*Landau*) pole an upper bound can be derived on $m_H = \mu$, depending on up to which scale the theory should remain perturbative.

Intrinsic Bounds on m_H



• The upper bound on m_H due to the Landau pole is called *triviality bound*:

 $m_H \left(Q(\text{Landau}) = 10^{-3} \,\text{GeV} \right) \le 800 \,\text{GeV}$ $m_H \left(Q(\text{Landau}) = 10^{16} \,\text{GeV} \right) \le 170 \,\text{GeV}$

(Triviality bound)



• Second case: small Higgs mass ($m_H \ll m_t$)



• With $\lambda(v^2) = \mu^2/v^2$ and increasing $Q^2 \lambda(Q^2)$ will turn negative and the Higgs potential will no longer be bound from below. The vacuum turns instable.

Intrinsic Bounds on m_H



• The upper bound on m_H due to the Landau pole is called *triviality bound*:

 $m_H \left(Q(\text{Landau}) = 10^{-3} \,\text{GeV} \right) \le 800 \,\text{GeV}$

 $m_H \left(Q(\text{Landau}) = 10^{16} \,\text{GeV} \right) \le 170 \,\text{GeV}$

(Triviality bound)

• The lower bound on m_H is called *stability bound*:

```
m_H \left( Q(\text{Landau}) = 10^{-3} \,\text{GeV} \right) \ge 20 \,\text{GeV}
m_H \left( Q(\text{Landau}) = 10^{16} \,\text{GeV} \right) \ge 90 \,\text{GeV}
```

(Stability bound)

• Calculate the boundaries from the equations that have been given.









- The amplitude of scattering processes can be obtained from a QM model via perturbation theory.
- We have derived the propagators as formal solutions of the equations of motion for the photon and for the electron.
- We have contracted the propagators and the fermion *spinors* into the matrix element to obtain its final form.
- We have reviewed the *Feynman* rules to translate the matrix element into a pictorial form and discussed the effect of higher order corrections.
- Finally we have seen how higher order corrections within the model give boundaries on the mass of the Higgs boson already within the model from requirements on its applicability.



- Next week Günter Quast will take over for the next two lectures/weeks.
- You will discuss the way from observable to measurement:
 - Rate measurements and measurements of particle properties.
 - Monte Carlo methods for event simulation.
 - Parton showers and hadronization, detector simulation.
- The week after you will discuss basic experimental measurement techniques:
 - Data acquisition, triggers.
 - Event selections, object calibration, reconstruction efficiencies, acceptances.
 - Determination of background processes.

