

Properties of the Higgs Boson

Joram Berger, Roger Wolf
2 July 2015

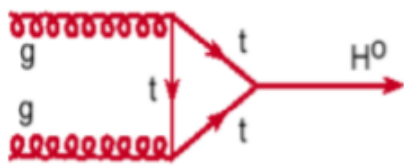
INSTITUTE OF EXPERIMENTAL PARTICLE PHYSICS (IEKP) – PHYSICS FACULTY



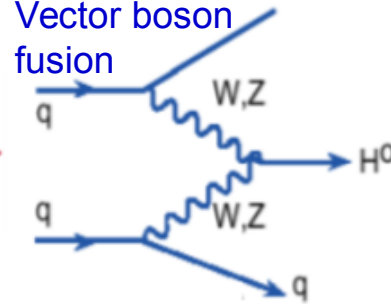
Higgs Boson Production & Decay

If m_H is given all properties of the (SM) Higgs boson are known:

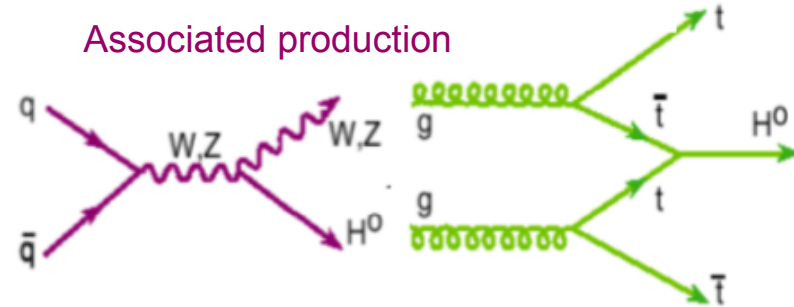
Gluon fusion



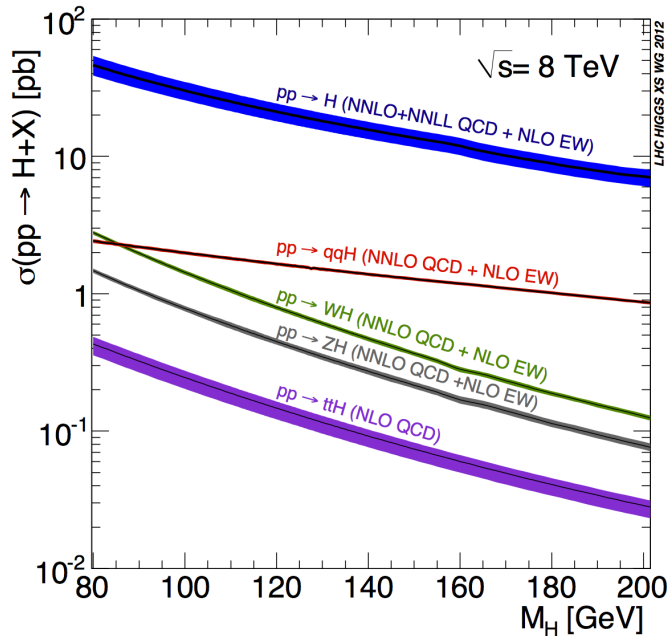
Vector boson fusion



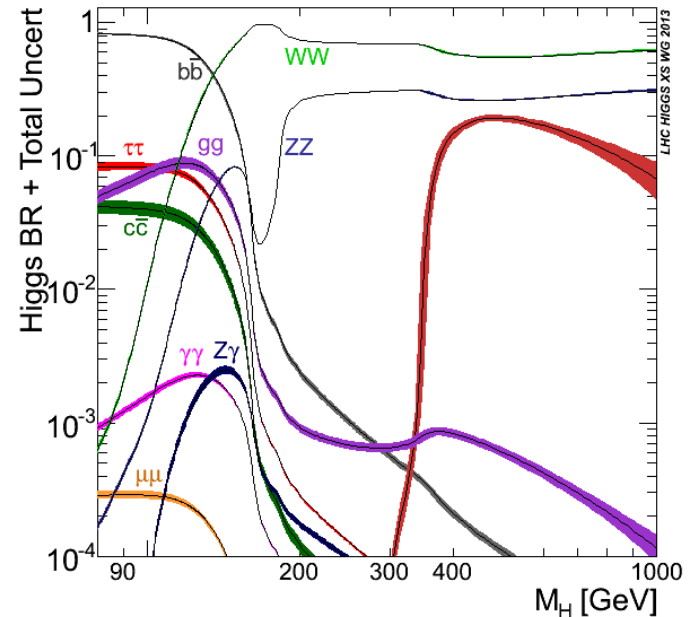
Associated production



Production (in proton proton collisions)

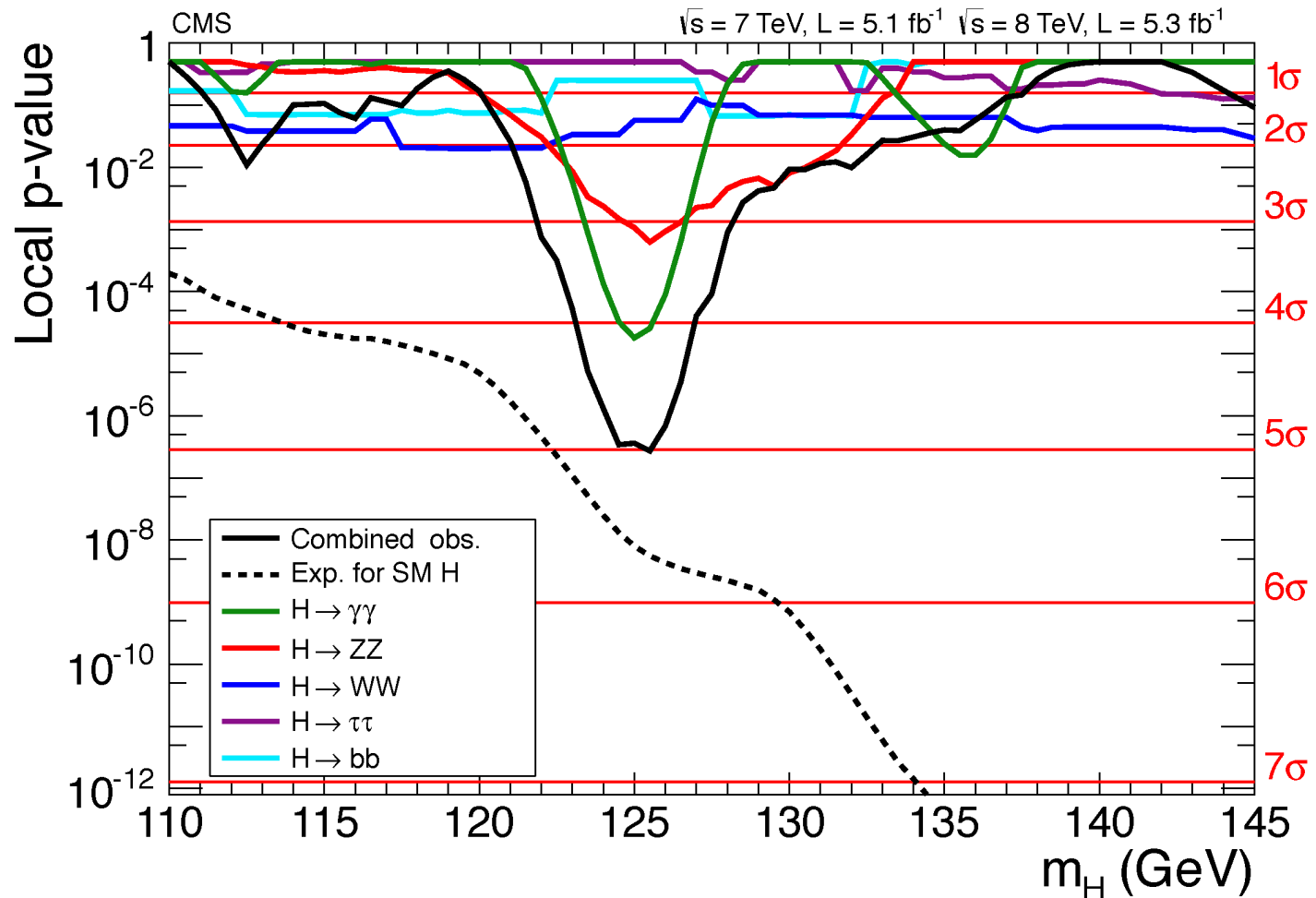


Decay



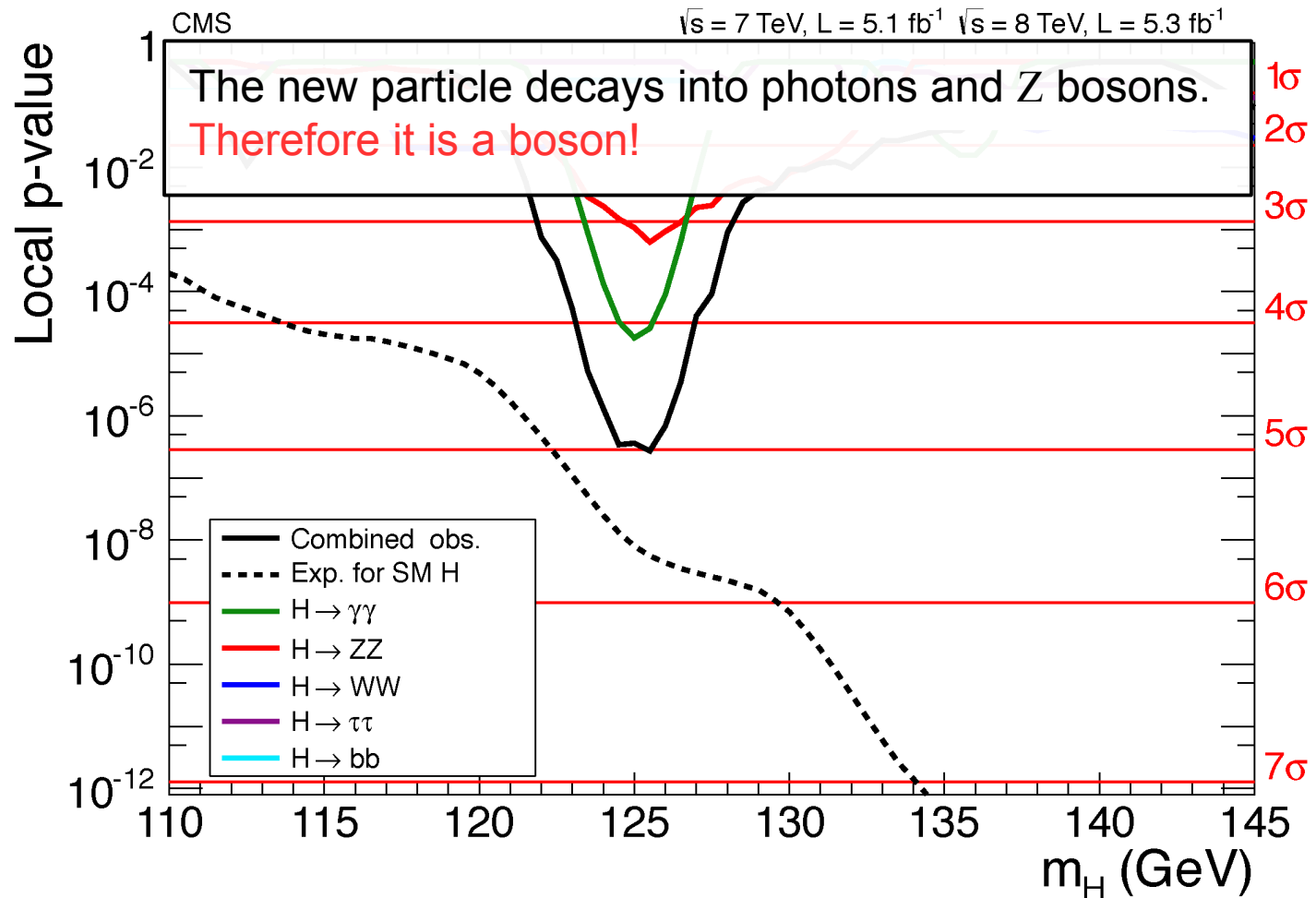
Reminder: Discovery on 4th July 2012

- Scratching magic 5σ boundary.
- Discovery driven by $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ$ (high resolution channels).
- Broad moderate excesses for $H \rightarrow WW$ and $H \rightarrow bb$.
- No signal seen in $H \rightarrow \tau\tau$.



Reminder: Discovery on 4th July 2012

- Scratching magic 5σ boundary.
- Discovery driven by $H \rightarrow \gamma\gamma$ and $H \rightarrow ZZ$ (high resolution channels).
- Broad moderate excesses for $H \rightarrow WW$ and $H \rightarrow bb$.
- No signal seen in $H \rightarrow \tau\tau$.





- Mass
- Decay Width
- Signal Strength
- Couplings
- Spin and CP

Analyzed Datasets

- Status: Summer 2015.
- Final states:

$$H \rightarrow \gamma\gamma \quad H \rightarrow bb$$

$$H \rightarrow ZZ \quad H \rightarrow \tau\tau$$

$$H \rightarrow WW$$

- Production modes:

$$gg \rightarrow H \quad qq \rightarrow VH$$

$$qq \rightarrow qqH \quad gg \rightarrow ttH$$

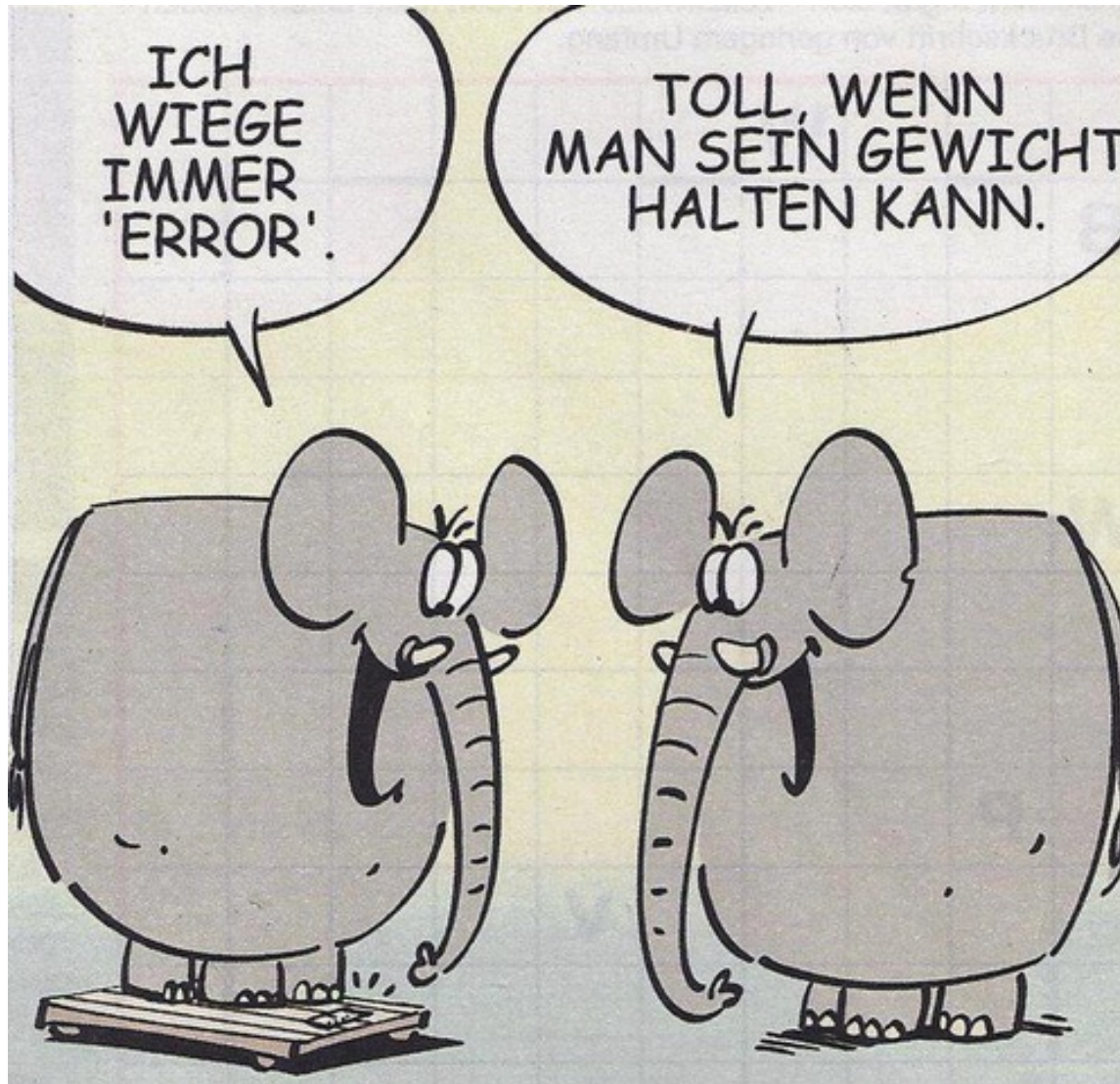
- 207 event categories.
- 2519 nuisance parameters.
- ~20 MB binary file of statistic model,
- ~50 MB human readable *txt* file.

Decay tag and production tag	Expected signal composition	$\sigma_{\text{sig}}/m_{\text{H}}$	Luminosity (fb^{-1})		
			7TeV	8TeV	
H $\rightarrow \gamma\gamma$ [20], Section 2.1			5.1	19.7	
$\gamma\gamma$	Untagged	76-93% ggH	0.8-2.1%	4	5
	2-jet VBF	50-80% VBF	1.0-1.3%	2	3
	Leptonic VH	$\approx 95\%$ VH (WH/ZH ≈ 5)	1.3%	2	2
	E_T^{miss} VH	70-80% VH (WH/ZH ≈ 1)	1.3%	1	1
	2-jet VH	$\approx 65\%$ VH (WH/ZH ≈ 5)	1.0-1.3%	1	1
	Leptonic $t\bar{t}H$	$\approx 95\%$ $t\bar{t}H$	1.1%	1 [†]	1
Multi-jet $t\bar{t}H$	$>90\%$ $t\bar{t}H$	1.1%	1 [†]	1	
H $\rightarrow ZZ^{(*)} \rightarrow 4\ell$ [18], Section 2.2			5.1	19.7	
4 μ , 2e2 μ , 4e	2-jet	42% VBF + VH	1.3, 1.8, 2.2% [‡]	3	3
	Other	$\approx 90\%$ ggH		3	3
H $\rightarrow WW^{(*)} \rightarrow \ell\nu\ell\nu$ [17], Section 2.3			4.9	19.4	
ee + $\mu\mu$, e μ	0-jet	96-98% ggH	e μ 16% [‡]	2	2
	1-jet	82-84% ggH	e μ 17% [‡]	2	2
	2-jet VBF	78-86% VBF		2	2
	2-jet VH	31-40% VH		2	2
3 ℓ 3 ν WH $\ell\ell + \ell'\nu\bar{\nu}$ ZH	SF-SS, SF-OS	$\approx 100\%$ WH, up to 20% $\tau\tau$		2	2
	eee, ee μ , $\mu\mu\mu$, $\mu\mu e$	$\approx 100\%$ ZH		4	4
H $\rightarrow \tau\tau$ [19], Section 2.4			4.9	19.7	
e τ_h , $\mu\tau_h$	0-jet	$\approx 98\%$ ggH	11-14%	4	4
	1-jet	70-80% ggH	12-16%	5	5
	2-jet VBF	75-83% VBF	13-16%	2	4
$\tau_h\tau_h$	1-jet	67-70% ggH	10-12%	-	2
	2-jet VBF	80% VBF	11%	-	1
e μ	0-jet	$\approx 98\%$ ggH, 23-30% WW	16-20%	2	2
	1-jet	75-80% ggH, 31-38% WW	18-19%	2	2
	2-jet VBF	79-94% VBF, 37-45% WW	14-19%	1	2
ee, $\mu\mu$	0-jet	88-98% ggH		4	4
	1-jet	74-78% ggH, $\approx 17\%$ WW [*]		4	4
	2-jet CJV	$\approx 50\%$ VBF, $\approx 45\%$ ggH, 17-24% WW [*]		2	2
$\ell\ell + LL'$ ZH $\ell + \tau_h\tau_h$ WH $\ell + \ell'\tau_h$ WH	LL' = $\tau_h\tau_h, \ell\tau_h, e\mu$	$\approx 15\%$ (70%) WW for LL' = $\ell\tau_h$ (e μ)		8	8
		$\approx 96\%$ VH, ZH/WH ≈ 0.1		2	2
		ZH/WH $\approx 5\%$, 9-11% WW		2	4
VH with H $\rightarrow bb$ [16], Section 2.5			5.1	18.9	
W($\ell\nu$)bb W($\tau_h\nu$)bb	$p_T(V)$ bins	$\approx 100\%$ VH, 96-98% WH		4	6
		93% WH	$\approx 10\%$	-	1
Z($\ell\ell$)bb Z($\nu\nu$)bb	$p_T(V)$ bins	$\approx 100\%$ ZH		4	4
	$p_T(V)$ bins	$\approx 100\%$ VH, 62-76% ZH		2	3
$t\bar{t}H$ with H \rightarrow hadrons [14, 28], Section 2.6			5.0	19.3	
H $\rightarrow bb$	$t\bar{t}$ lepton+jets	$\approx 90\%$ bb but $\approx 24\%$ WW in $\geq 6j + 2b$		7	7
	$t\bar{t}$ dilepton	45-85% bb, 8-35% WW, 4-14% $\tau\tau$		2	3
	$t\bar{t}$ lepton+jets	68-80% $\tau\tau$, 13-22% WW, 5-13% bb		-	6
$t\bar{t}H$ with H \rightarrow leptons [29], Section 2.6			-	19.6	
2 ℓ -SS		WW/ $\tau\tau$ ≈ 3		-	6
3 ℓ		WW/ $\tau\tau$ ≈ 3		-	2
4 ℓ		WW : $\tau\tau$: ZZ $\approx 3 : 2 : 1$		-	1

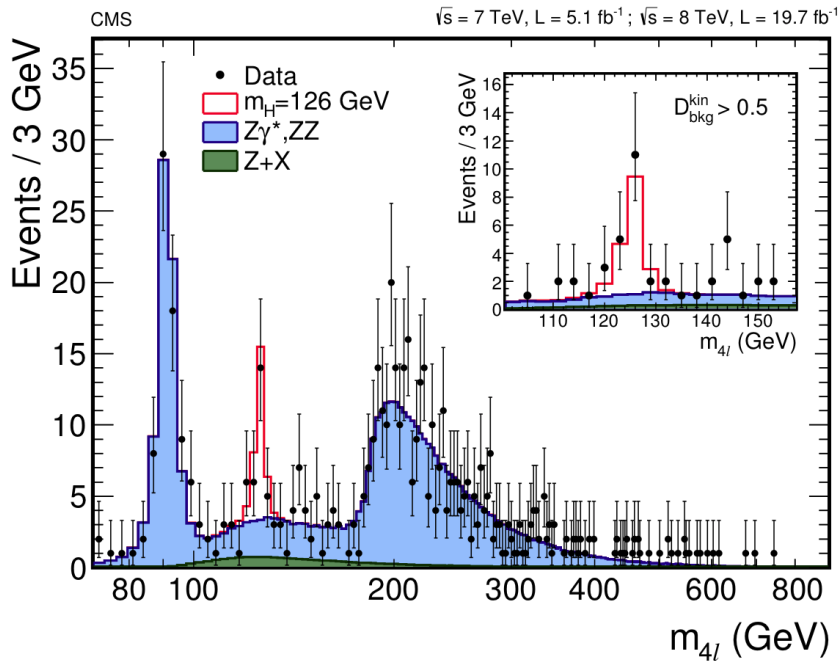
^{*} Events fulfilling the requirements of either selection are combined into one category.

[†] Values for analyses dedicated to the measurement of the mass that do not use the same categories and/or observables.

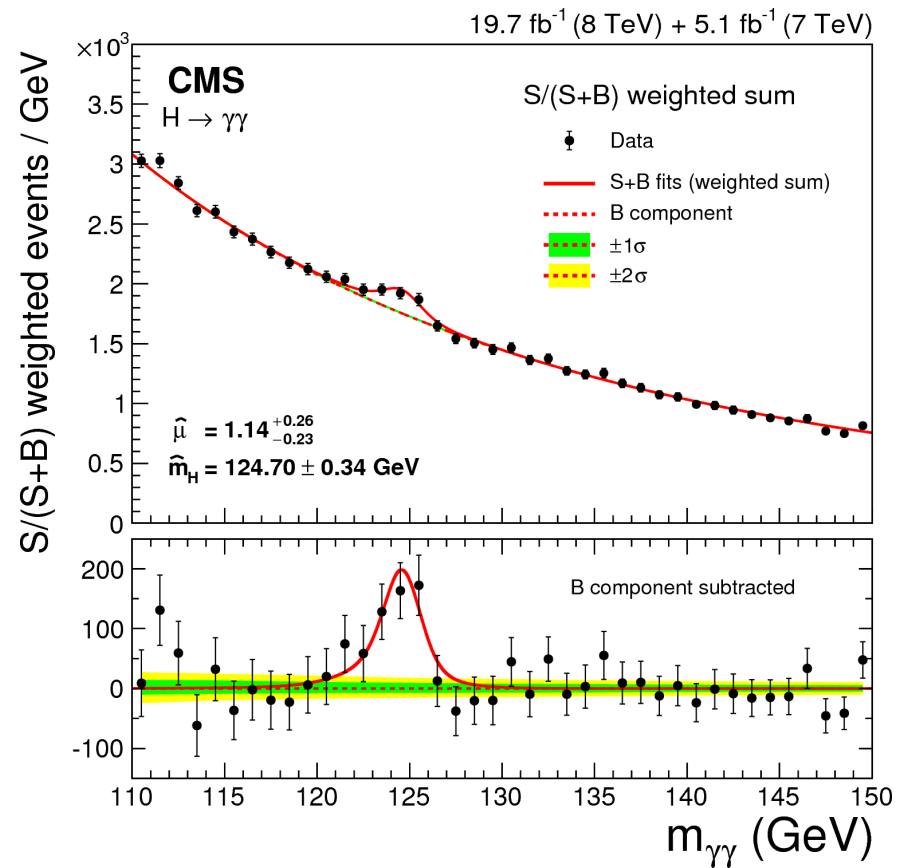
[‡] Composition in the regions for which the ratio between signal and background $s/(s+b) > 0.05$.



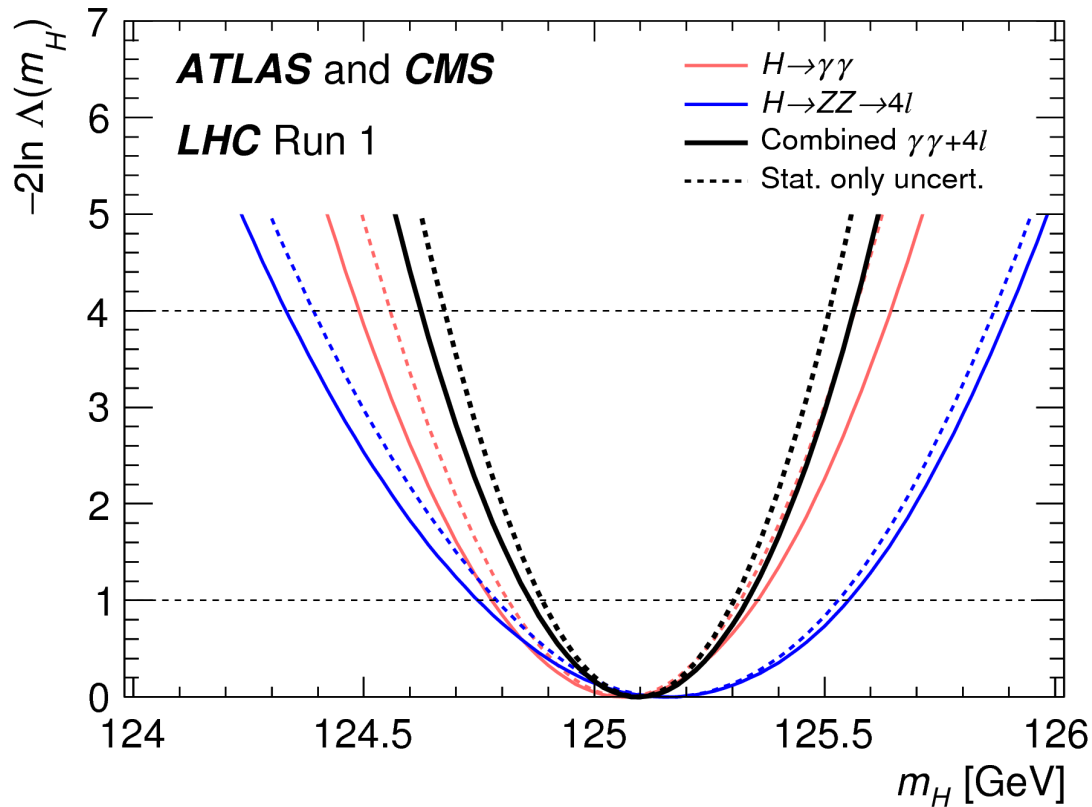
Mass Measurement



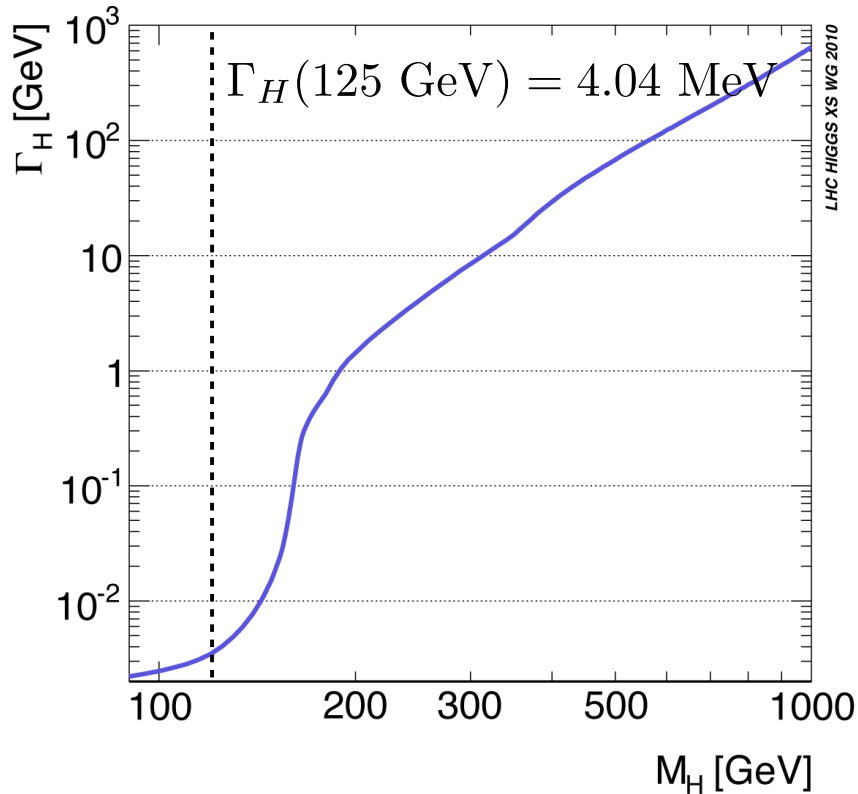
- Only “free parameter” in the SM.
- Can be directly measured in high resolution channels ($H \rightarrow \gamma\gamma, H \rightarrow ZZ$).



Mass: Best Estimate



- Four free parameters in fit: $m_H(POI)$, μ_{ZZ} , $\mu_{\gamma\gamma}(ggH, ttH)$, $\mu_{\gamma\gamma}(qqH, VH)$ (profiled)
- Best estimate: $m_H = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{syst.}) \text{ GeV}$



- Cannot be measured directly from mass peak (**experimental resolution**).
- But **accessible in $H \rightarrow ZZ$ via line shape analysis** of (non-)resonant $gg \rightarrow ZZ, H \rightarrow 4\ell$ production:

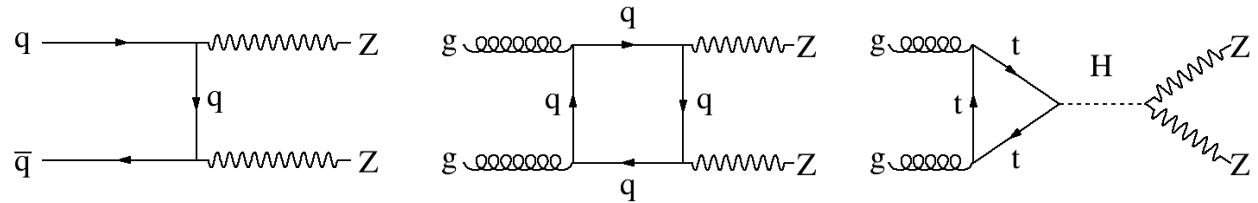
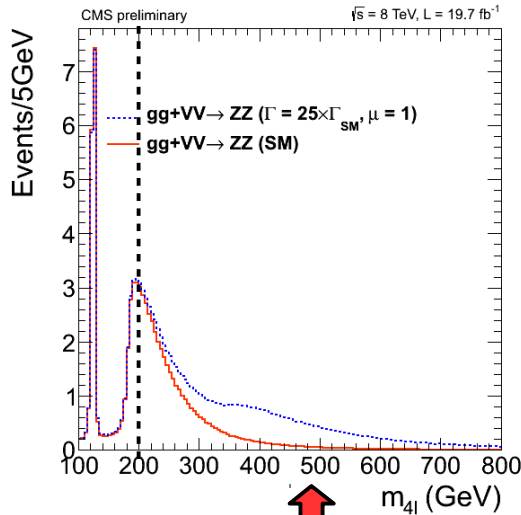
$$\frac{d\sigma(gg \rightarrow H \rightarrow ZZ)}{dm_{4\ell}^2} \propto \frac{\kappa_g^2 \kappa_Z^2}{(m_{4\ell}^2 - m_H^2)^2 + m_H^2 \Gamma_H^2}$$

$$\sigma^{\text{on-shell}} \propto \frac{\kappa_g^2 \kappa_Z^2}{m_H \Gamma_H} \Big|_{m_{4\ell} \approx m_H}$$

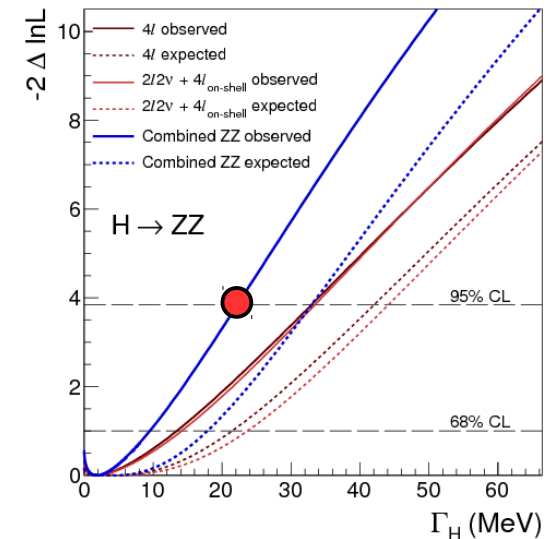
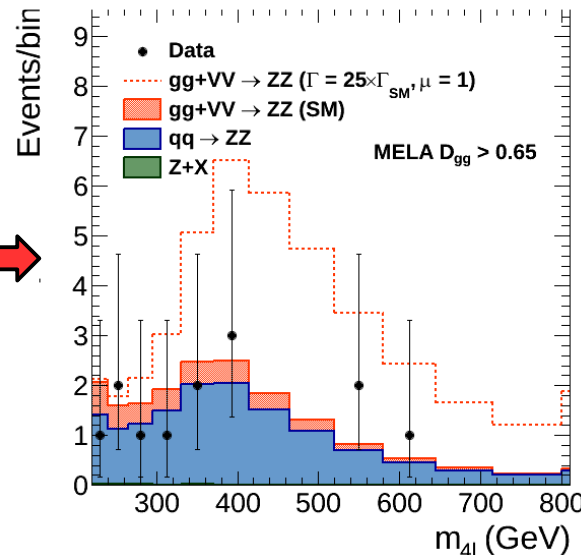
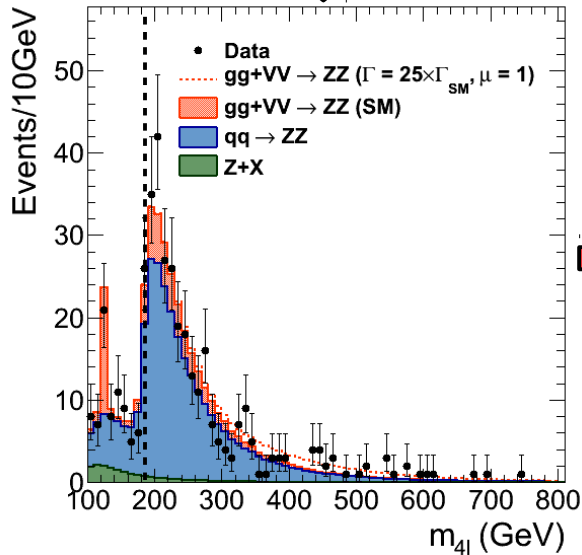
$$\sigma^{\text{off-shell}} \propto \frac{\kappa_g^2 \kappa_Z^2}{(m_{4\ell})^2} \Big|_{m_{4\ell} \approx 2m_Z \ll m_H}$$

- **Off-shell cross sections enhanced** close to ZZ production threshold.
- Best estimate: $m_H = 125.09 \pm 0.21(\text{stat.}) \pm 0.11(\text{syst.}) \text{ GeV}$

Decay Width



- Count ratio of **off-shell over on-shell** events.
- Use $4l$ (on- and off-shell) & $2l2\nu$ (off-shell only).
- **95% CL upper limit $\Gamma_H < 22$ MeV (obs), 33 MeV (exp).**

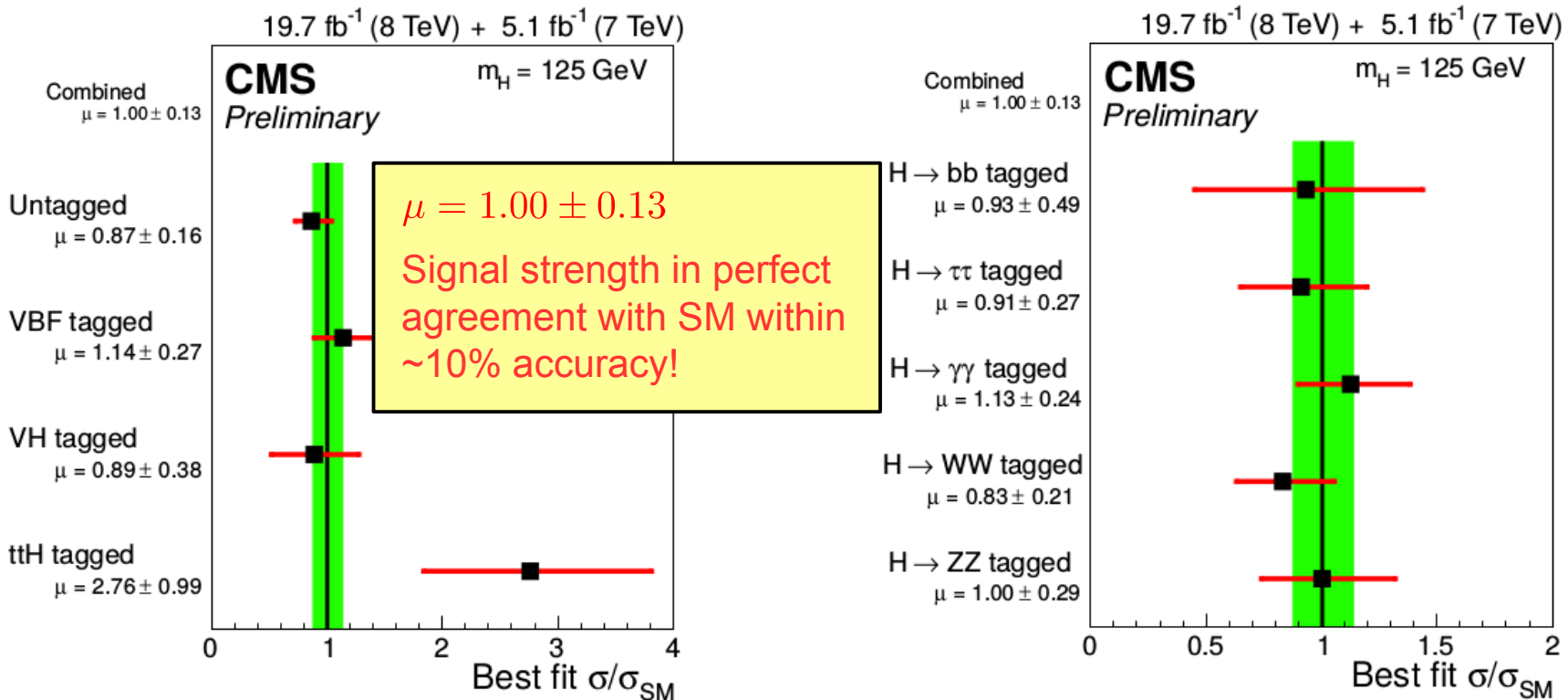


Compatibility of Couplings the SM

8			4		6			7
						4		
	1					6	5	
5		9		3		7	8	
				7				
	4	8		2		1		3
	5	2					9	
		1						
3			9		2			5

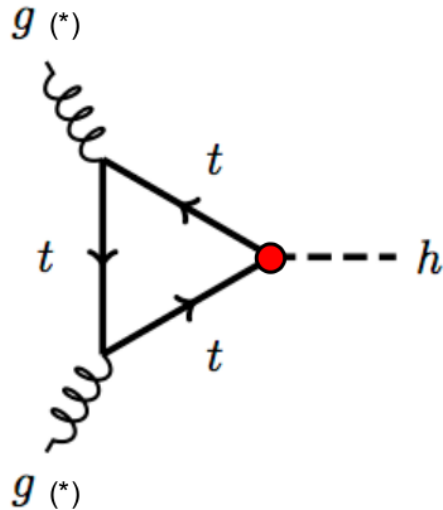
Compatibility of Couplings the SM

- **Fix mass to best fit value** from $H \rightarrow ZZ$ and $H \rightarrow \gamma\gamma$ (125 GeV).
- Introduce signal strength modifier μ_X for each production mode or decay channel.
- Apply **separate fit** for each production mode or decay channel.

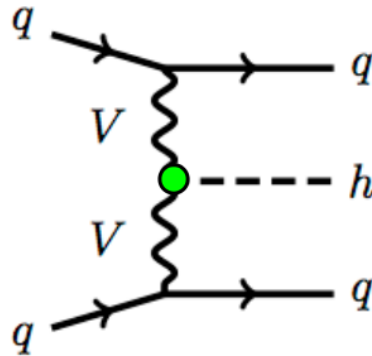


- Determine **couplings from production mode and decay channel**:

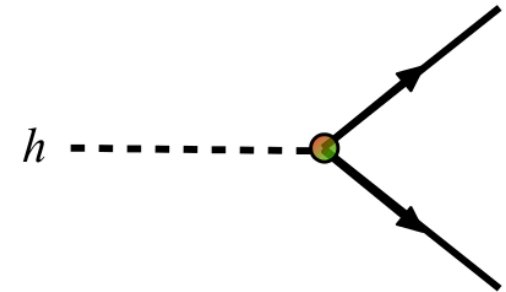
$gg \rightarrow H$ production:



$qq \rightarrow qqH$ production:



Decay to f or V :



● f : $\lambda_{\text{Hff}} = \frac{m_f}{v}$ $\kappa_f = \frac{\lambda}{\lambda_{\text{SM}}}$

● V : $g_{\text{HVV}} = \frac{2m_V^2}{v}$ $\kappa_V = \frac{g}{g_{\text{SM}}}$

- Coupling to gluon can be f or effective (*).

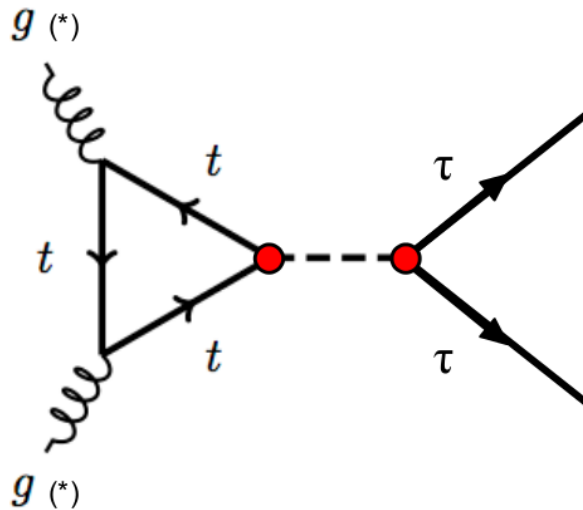
- Coupling to γ can be effective or a mixture of $f + V$.

- Direct measurement not possible since κ_i appear in nominator and denominator of

$$\text{BR}_i = \frac{\Gamma_i}{\Gamma_h} = \frac{\kappa_i}{\sum \kappa}$$

Narrow Width Approximation

- Assume $\Gamma_H \ll m_H$, which is well justified by $\Gamma_H = 4.04$ MeV and $m_H = 125$ GeV.
- Propagator: $\frac{1}{(q^2 - m^2 + m^2\Gamma^2)} \rightarrow \frac{\pi}{m\Gamma} \delta(q^2 - m^2)$ for $\Gamma \rightarrow 0$.

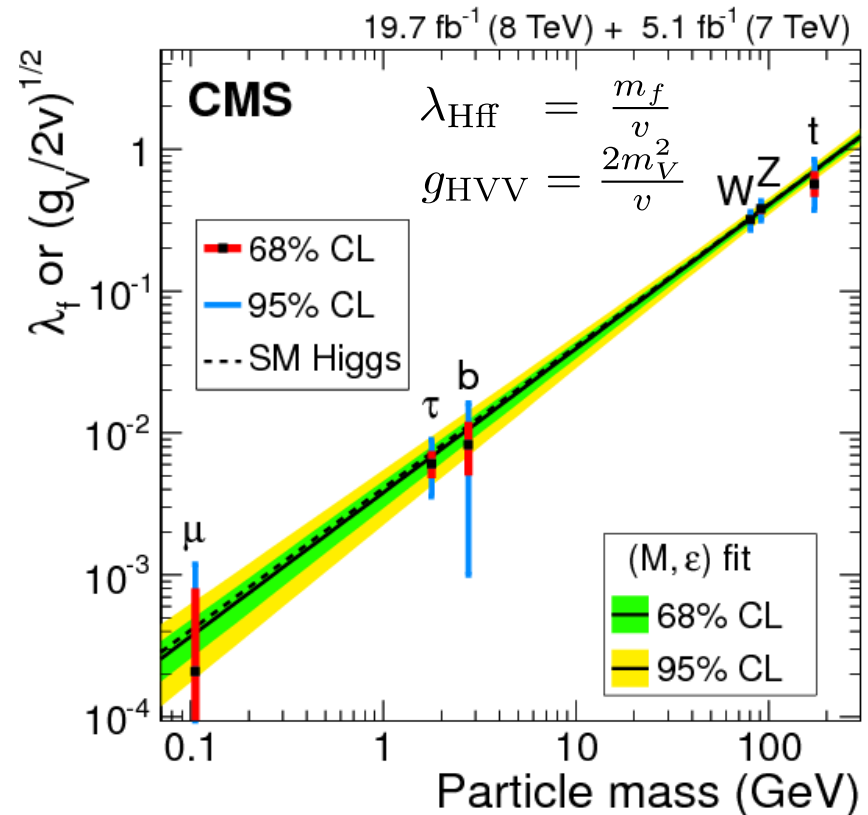
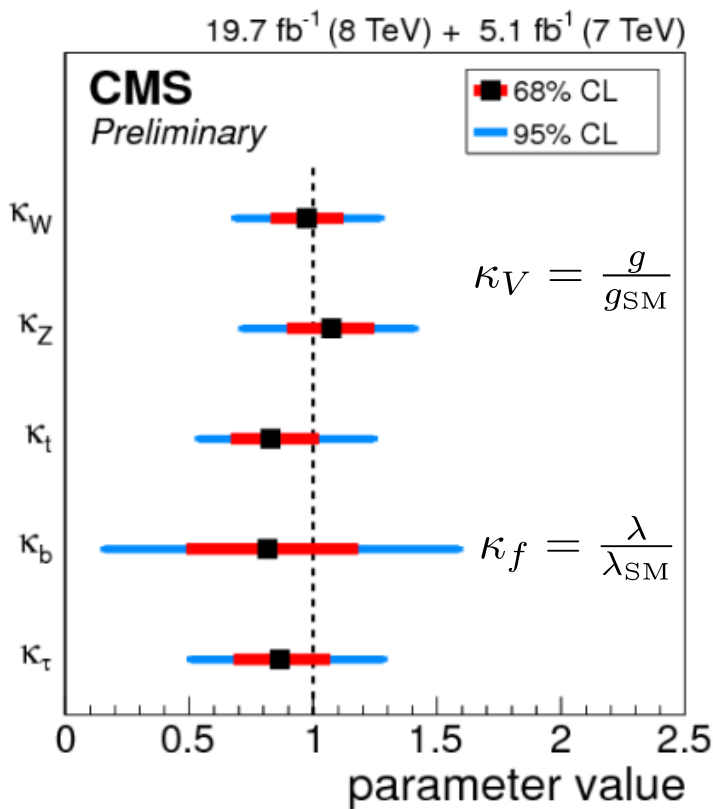


- i.e. put **propagating particle on shell**.
- Calculate cross section as $\sigma \times \text{BR}$.
- $\text{BR}_X = \frac{\Gamma_X}{\Gamma_H}$, $\Gamma_H = \sum_i \Gamma_i$.
- $\sigma \propto (\kappa_t \kappa_\tau)^2 \propto (\kappa_u \kappa_d)^2 \propto (\kappa_q \kappa_f)^2 \propto (\kappa_g \kappa_f)^2$.

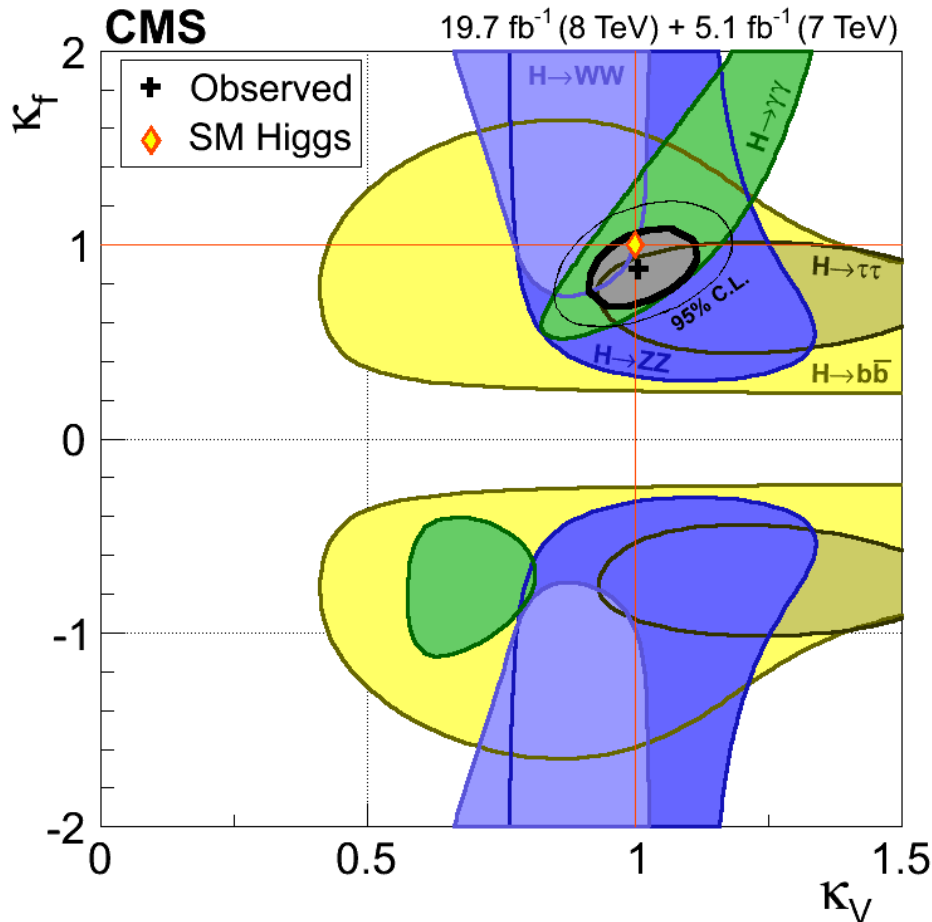
- For each production mode and decay channel **collect κ_i** and express Γ_H as **sum of individual κ_i** .

General Fitting model with 5 POI's

- Five free parameters for each tree-level coupling, m_H fixed to best fit value, κ_γ resolved in W , Z and t contributions, κ_g resolved in t and b contribution.



Fermion versus Vector Boson Couplings



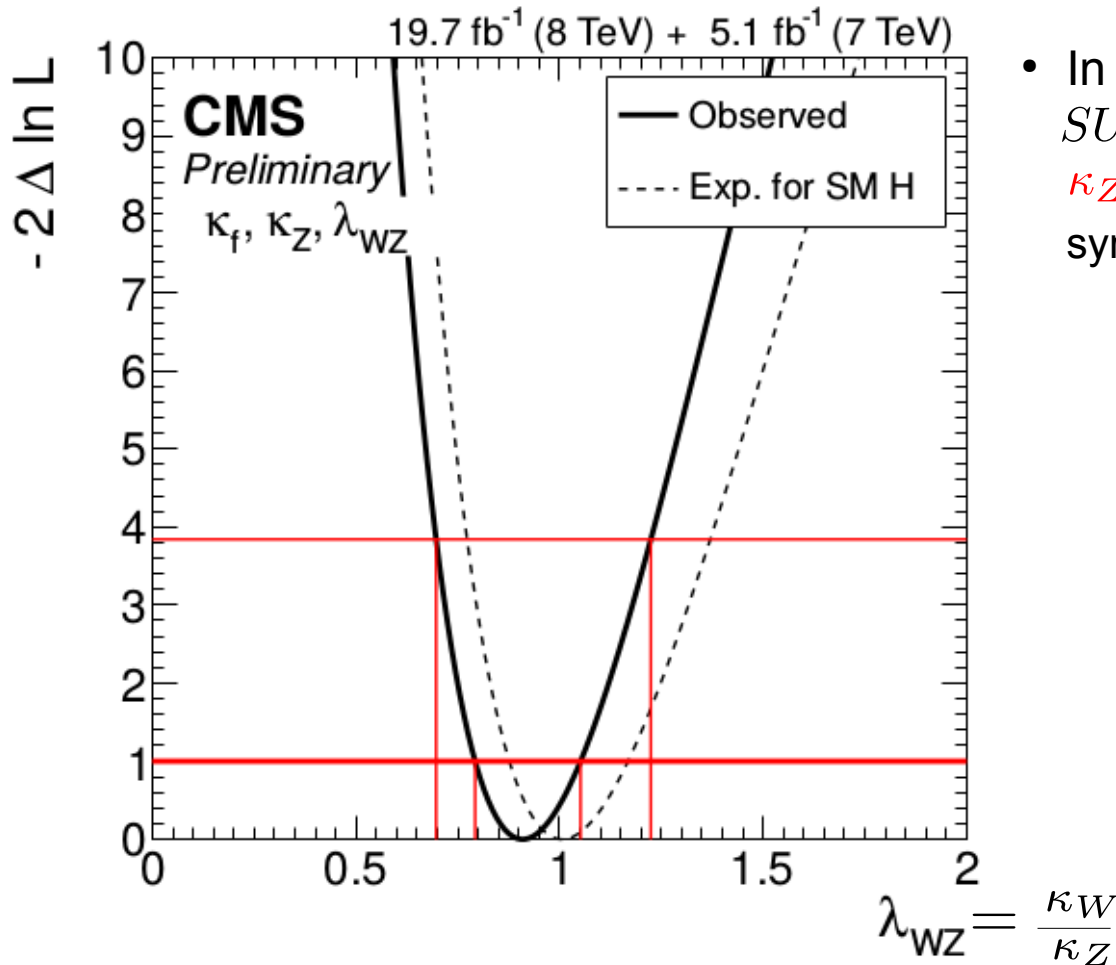
- Cross section $H \rightarrow VV$:

$$\sigma \propto (\kappa_f \kappa_V)^2 + (\kappa_V \kappa_V)^2$$

\downarrow $gg \rightarrow H$ \downarrow $qq \rightarrow qqH$
- Cross section $H \rightarrow ff$:

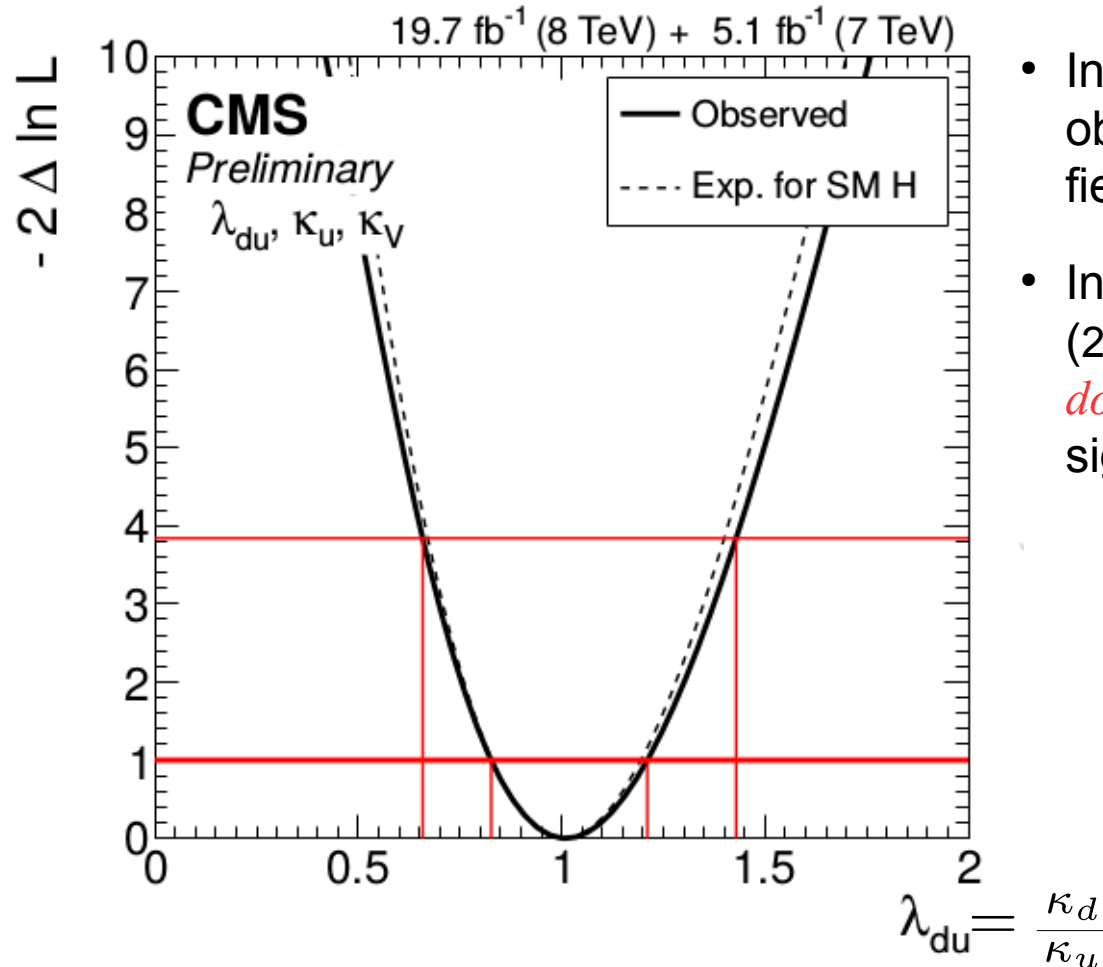
$$\sigma \propto (\kappa_f \kappa_f)^2 + (\kappa_V \kappa_f)^2$$
- Cross section $H \rightarrow \gamma\gamma$:

$$\sigma \propto (\kappa_f^2 - \kappa_f \kappa_V)^2 + (\kappa_V \kappa_f - \kappa_V^2)^2$$
- $H \rightarrow \gamma\gamma$ **only channel to distinguish sign ambiguities** due to interference terms.



- In the SM an additional $SU(2)_L \times SU(2)_R$ symmetry protects κ_W & κ_Z to be the same (→ custodial symmetry).

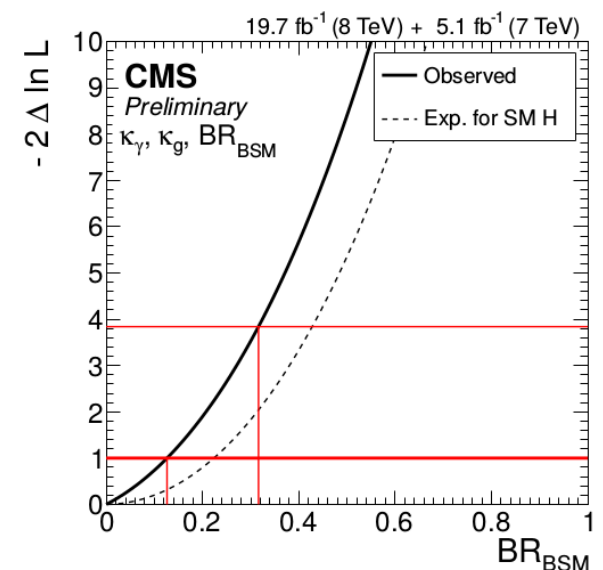
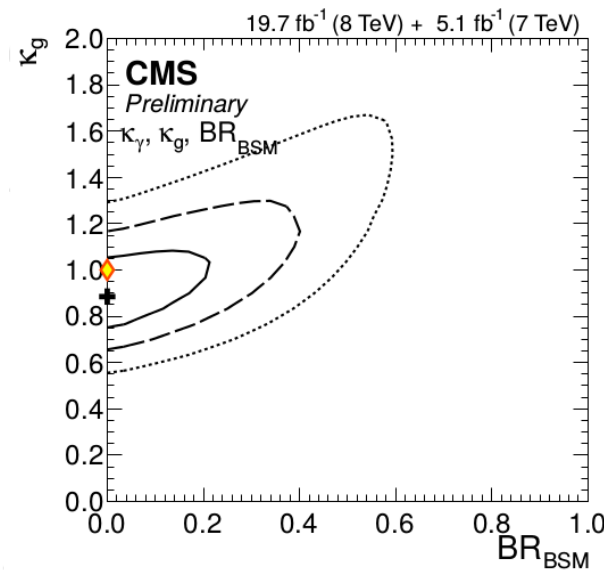
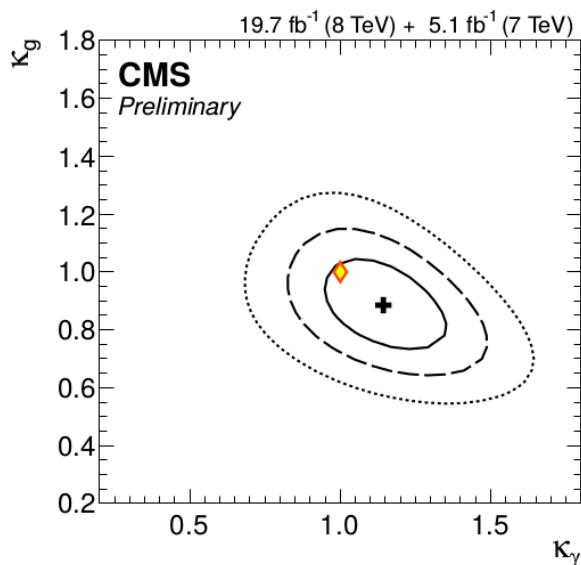
Up-type versus Down-type Fermion Couplings



- In the SM fermion masses can be obtained via only one Higgs doublet field.
- In Two Higgs Doublet Models (2HDM) the coupling to *up-* and *down-type* fermions can differ significantly.

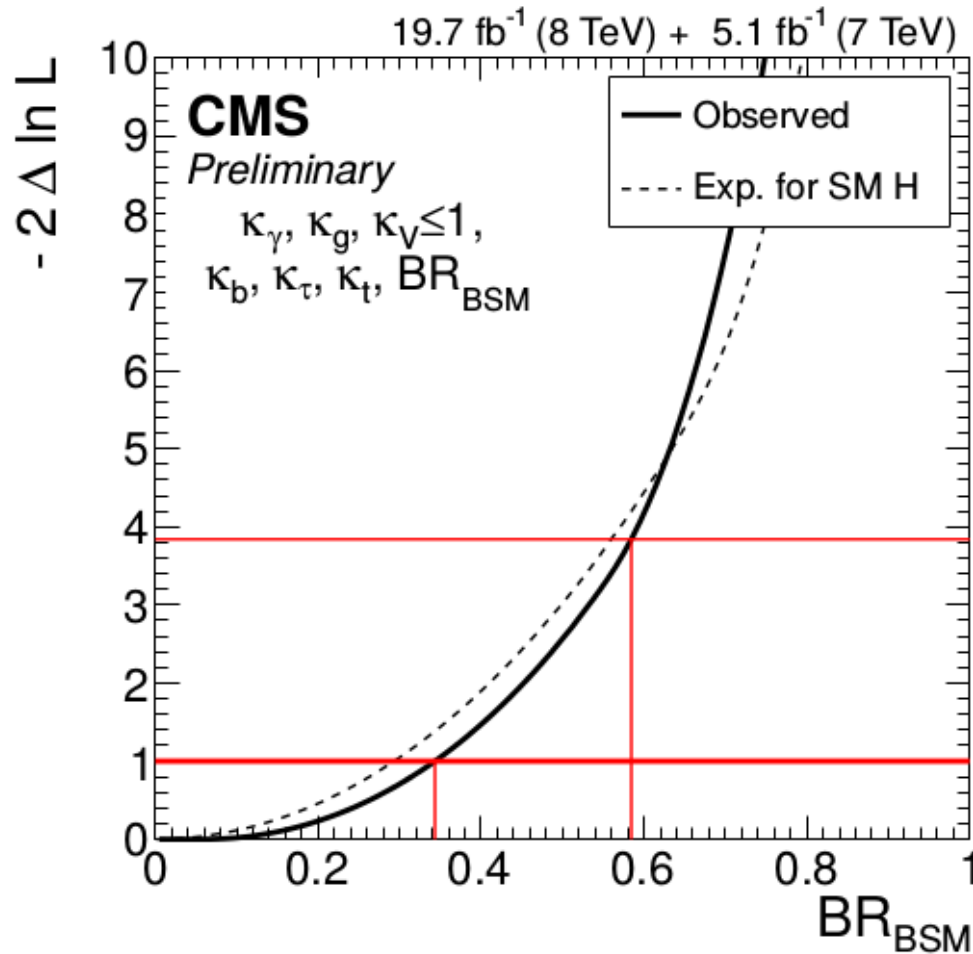
New Physics in Loops

- **New particles in loops** can lead to deviations of the effective couplings to gluons and photons from the SM expectation.
- Such deviations can be expressed by a **BR to new particles**, which have not been observed, yet.

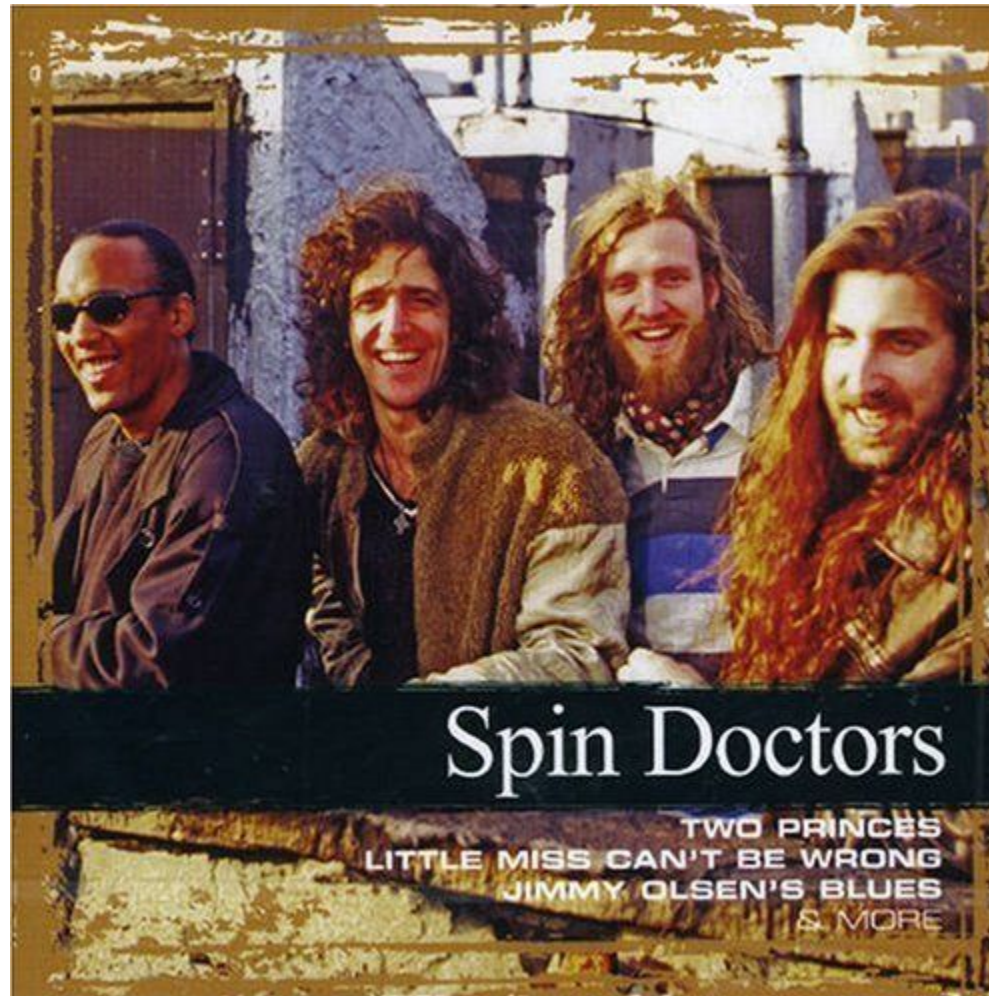


- Assuming SM values for tree-level couplings.

Search for the Invisible

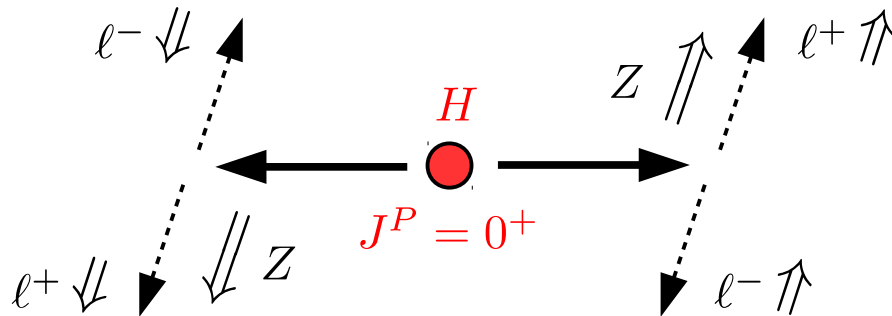


- Most model independent (inclusive) search for the decay, which has not been observed, yet, via deviation of $\sum \kappa_i$ from one.



Spin & Parity Estimates

- Spin and CP studies need something to make spin of particles visible → **spin analyzer**.
- Principle: **angular momentum conservation** in 2-body decay (best high energetic or with ν 's).
- Examples for $H \rightarrow ZZ \rightarrow 4\ell$:



$$Z : \quad P = -1$$

$$f : \quad P = +1$$

$$\bar{f} : \quad P = -1$$

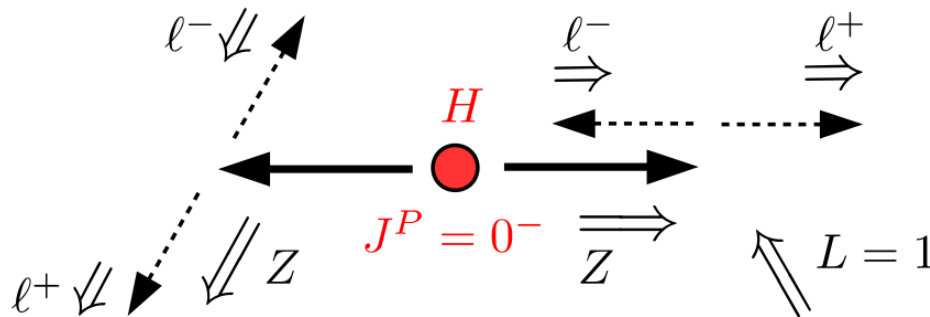
$$P = (-1)^L \prod_i (-1)$$

→ Intrinsic parities

- Both **longitudinal and transverse polarization** states of Z bosons are Spin and Parity sensitive.

Spin & Parity Estimates

- Spin and CP studies need something to make spin of particles visible → **spin analyzer**.
- Principle: **angular momentum conservation** in 2-body decay (best high energetic or with ν 's).
- Examples for $H \rightarrow ZZ \rightarrow 4\ell$:



$$Z : \quad P = -1$$

$$f : \quad P = +1$$

$$\bar{f} : \quad P = -1$$

$$P = (-1)^L \prod_i (-1)$$

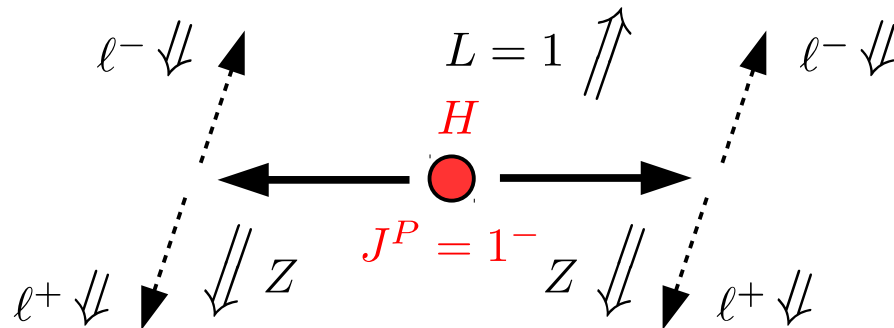
↘ Intrinsic parities

- Both **longitudinal and transverse polarization** states of Z bosons are Spin and Parity sensitive.

Spin & Parity Estimates

- Spin and CP studies need something to make spin of particles visible → **spin analyzer**.
- Principle: **angular momentum conservation** in 2-body decay (best high energetic or with ν 's).

- Examples for $H \rightarrow ZZ \rightarrow 4\ell$:



$$Z : P = -1$$

$$f : P = +1$$

$$\bar{f} : P = -1$$

$$P = (-1)^L \prod_i (-1)$$

↳ Intrinsic parities

- Both **longitudinal and transverse polarization** states of Z bosons are Spin and Parity sensitive.

The $H \rightarrow ZZ$ System

- System described by m_{Z_1} , m_{Z_2} and five more variables:

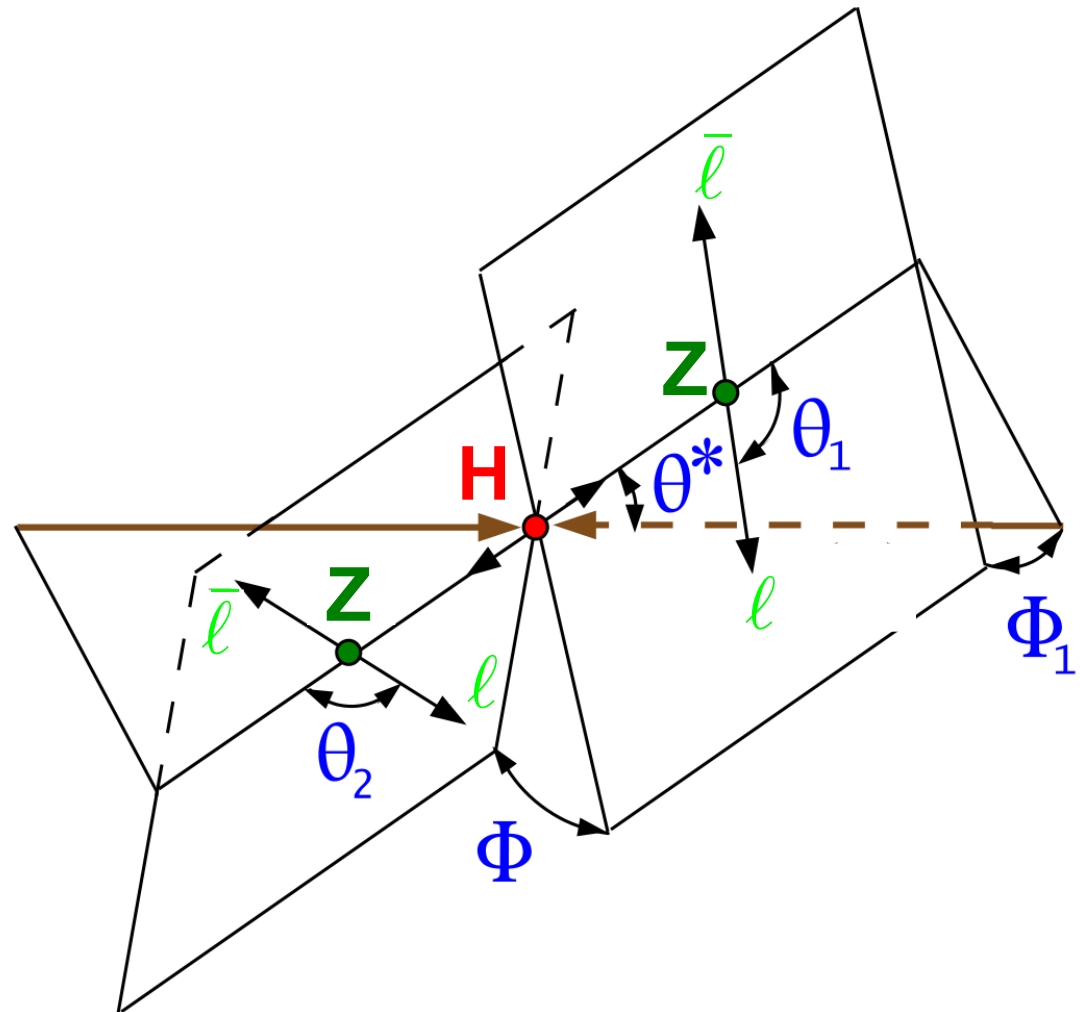
θ_1 decay angle $Z_1 \rightarrow \ell\bar{\ell}$

θ_2 decay angle $Z_2 \rightarrow \ell\bar{\ell}$

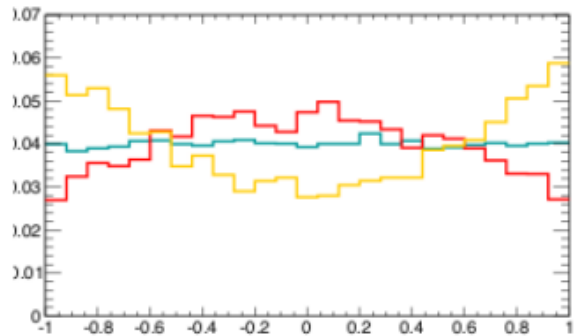
θ^* decay angle $H \rightarrow ZZ$

Φ azimuthal angle $H \rightarrow ZZ$

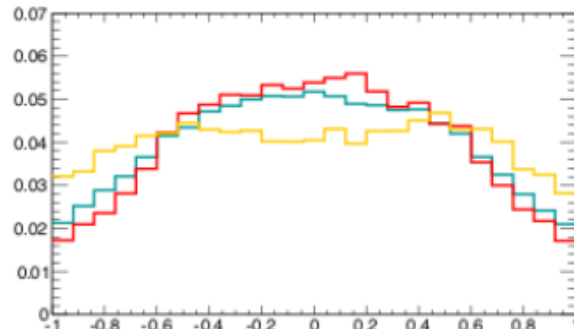
Φ_1 azimuthal angle $Z_1 \rightarrow \ell\bar{\ell}$



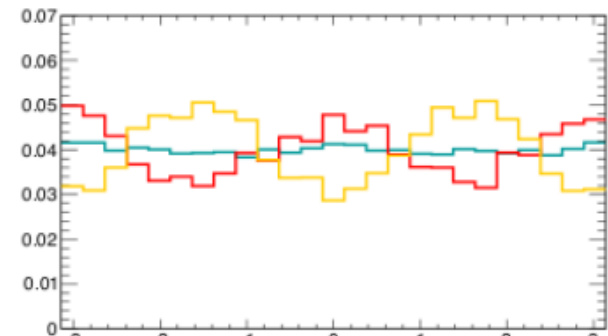
Discriminating Variables



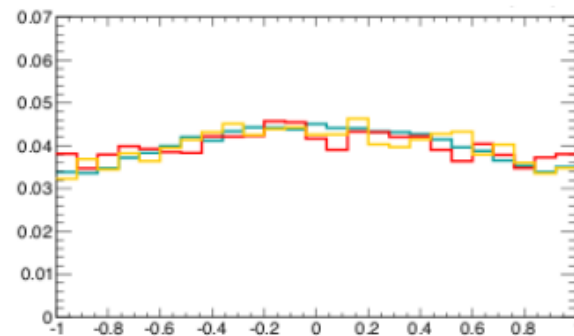
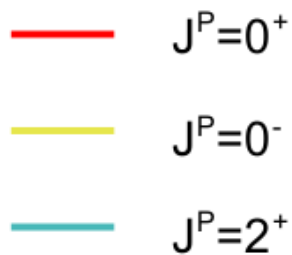
$\cos \theta_1$



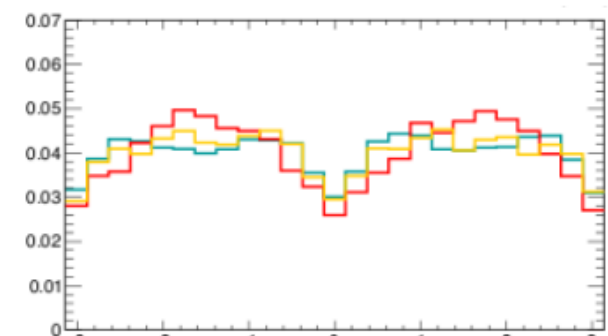
$\cos \theta_2$



Φ



$\cos \theta^*$

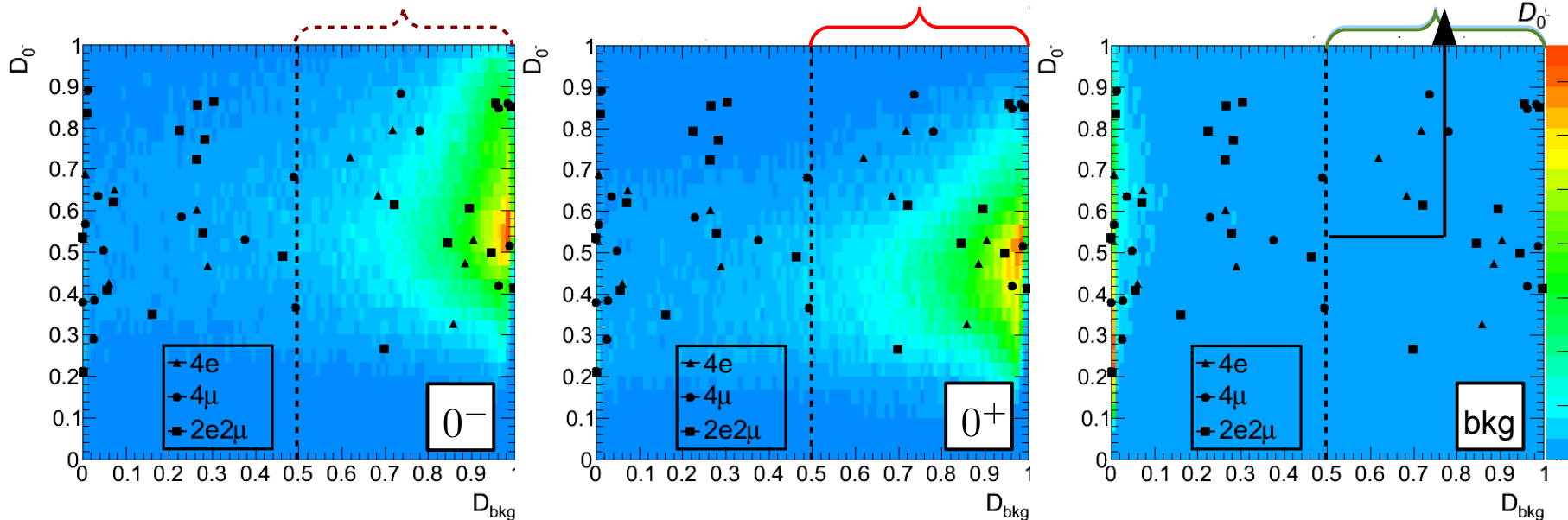
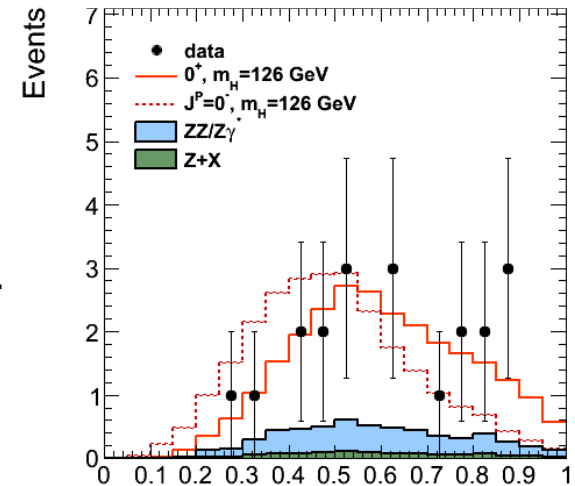


Φ_1

- As obtained from MC simulation (<http://www.pha.jhu.edu/spin/>).
- Taking acceptance and resolution effects into account.

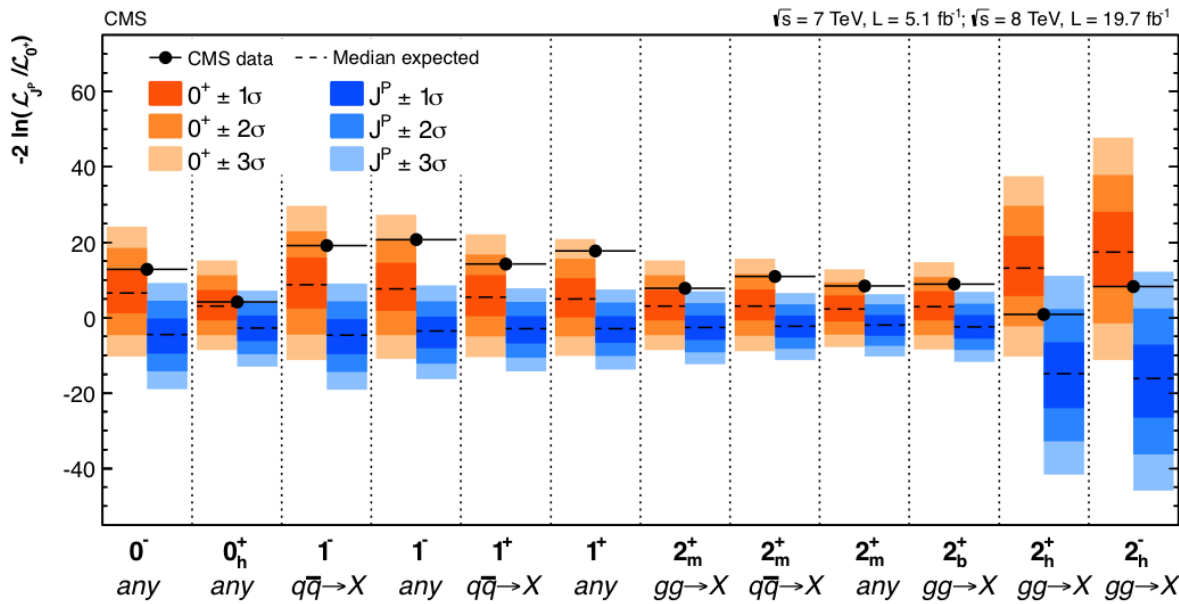
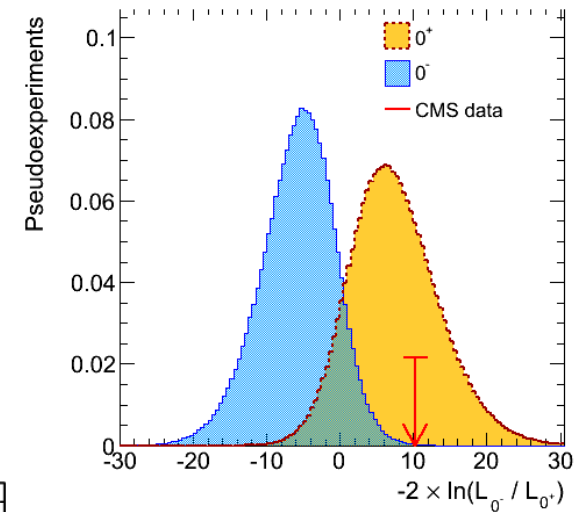
Combination into a Single Discriminating Variable

- Events with $106 \text{ GeV} < m_{4\ell} < 141 \text{ GeV}$ (49 events).
- Example given for 0^- hypothesis.
- For 1d projection a cut has been applied of $D_{\text{bkg}} > 0.5$.
- Statistical **assessment based on hypothesis tests**.



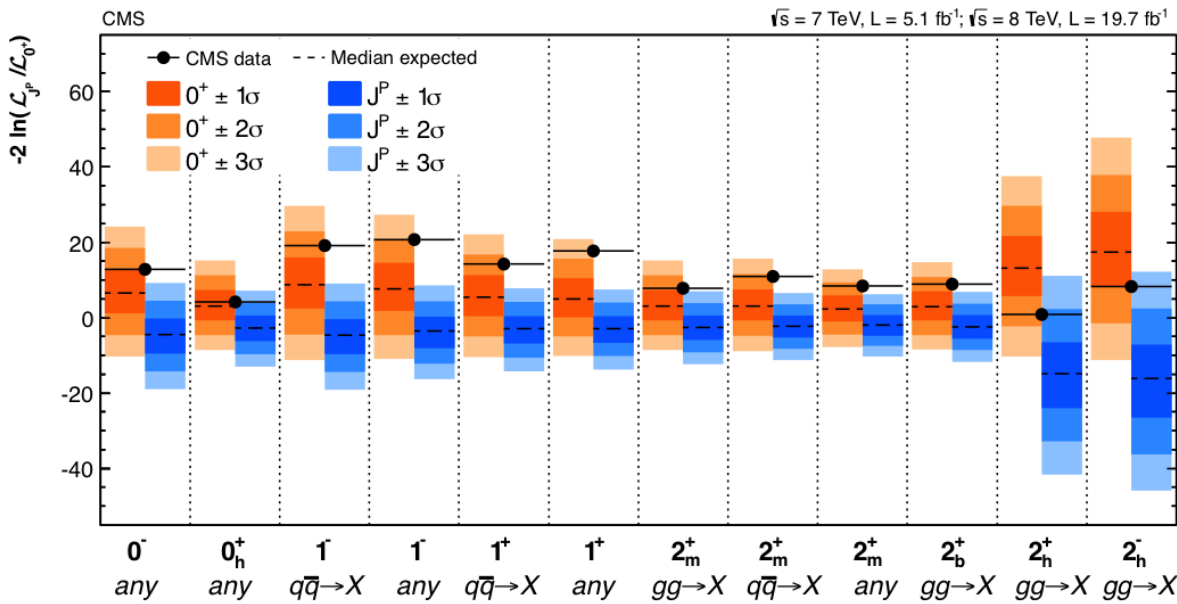
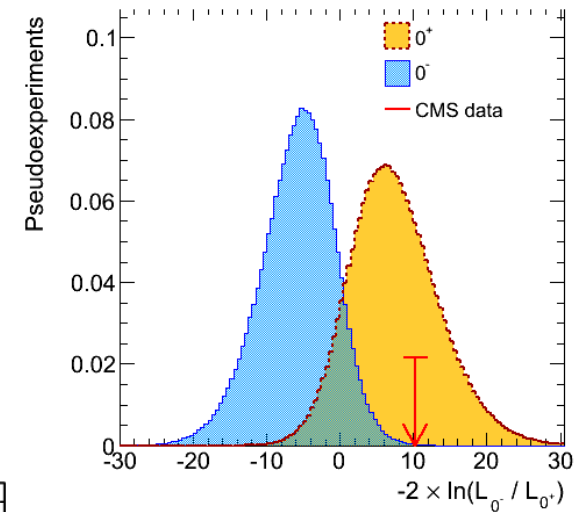
Combination into a Single Discriminating Variable

- Test statistic: $q = -2 \ln \left(\frac{\mathcal{L}(0^+ + BG)}{\mathcal{L}(J^P + BG)} \right)$.
- Expectation for given hypothesis 0^+ or J^P obtained from toy experiments.
- SM hypothesis (0^+) tested against large number of alternative hypotheses. SM favored in each case.



Combination into a Single Discriminating Variable

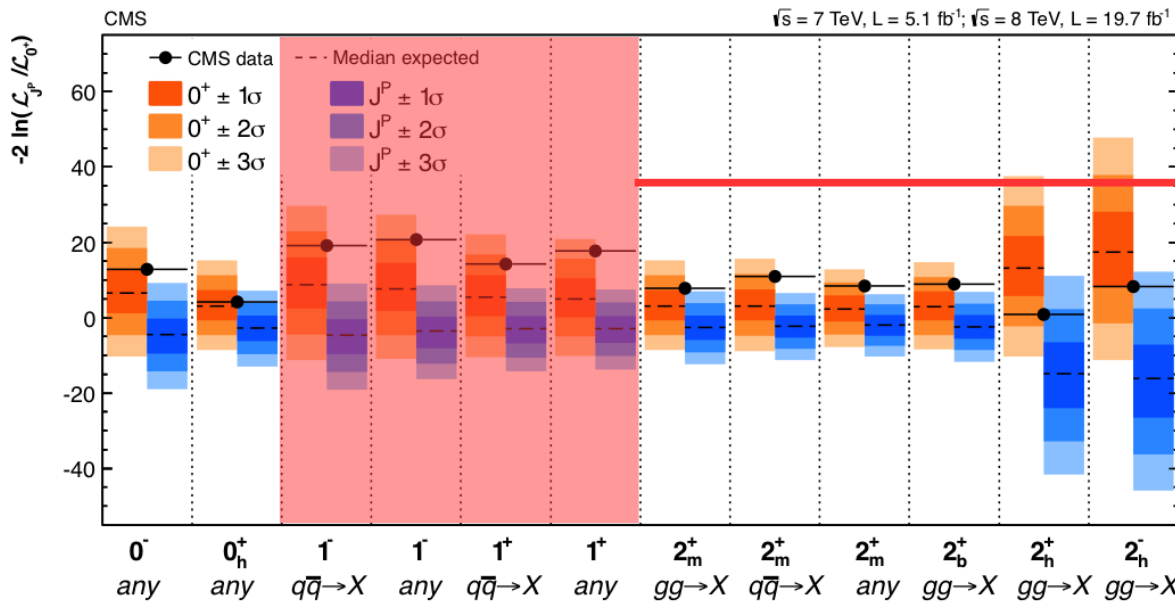
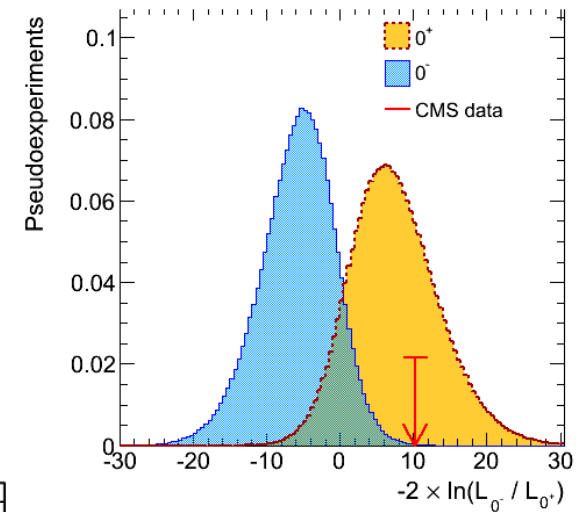
- Test statistic: $q = -2 \ln \left(\frac{\mathcal{L}(0^+ + BG)}{\mathcal{L}(J^P + BG)} \right)$.
- Expectation for given hypothesis 0^+ or J^P obtained from toy experiments.
- SM hypothesis (0^+) tested against large number of alternative hypotheses. SM favored in each case.



0^+ hypothesis favored.

Combination into a Single Discriminating Variable

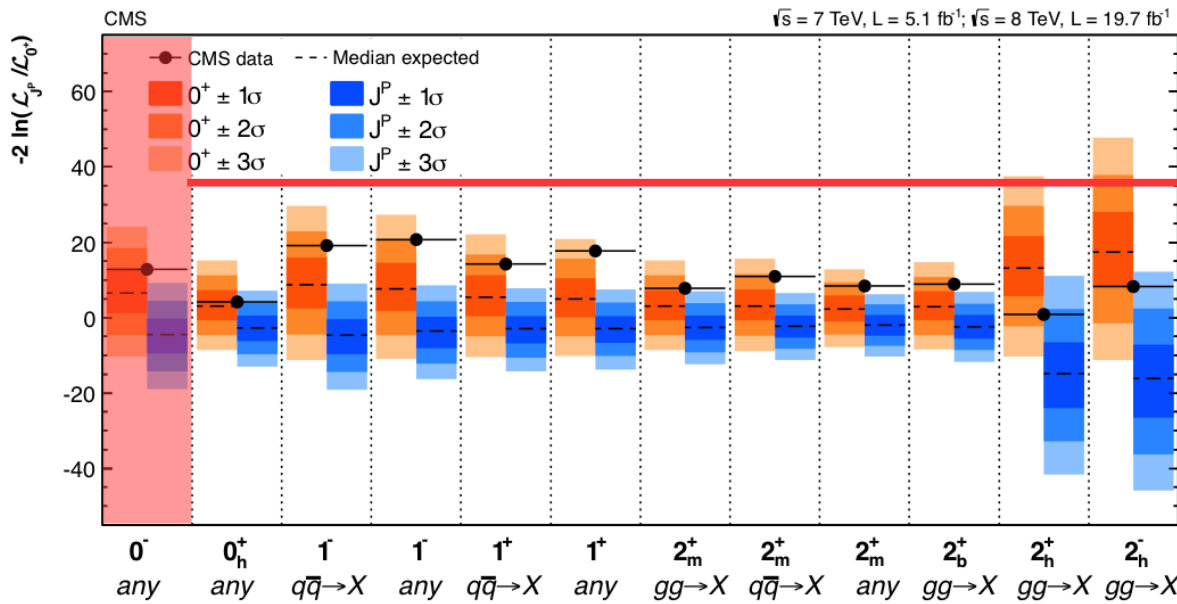
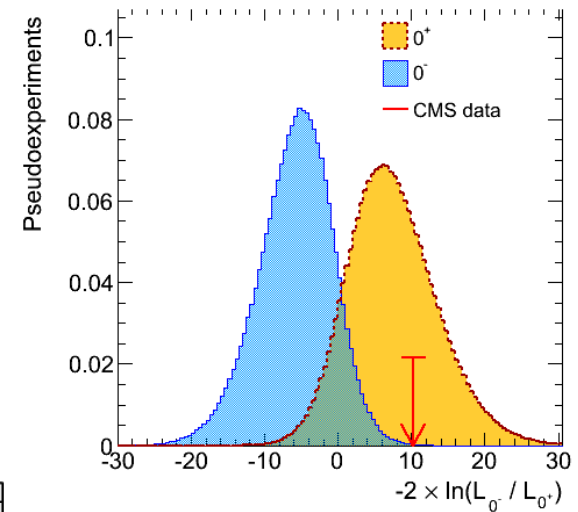
- Test statistic: $q = -2 \ln \left(\frac{\mathcal{L}(0^+ + BG)}{\mathcal{L}(J^P + BG)} \right)$.
- Expectation for given hypothesis 0^+ or J^P obtained from toy experiments.
- SM hypothesis (0^+) tested against large number of alternative hypotheses. SM favored in each case.



Spin 1 already excluded from $H \rightarrow \gamma\gamma$.

Combination into a Single Discriminating Variable

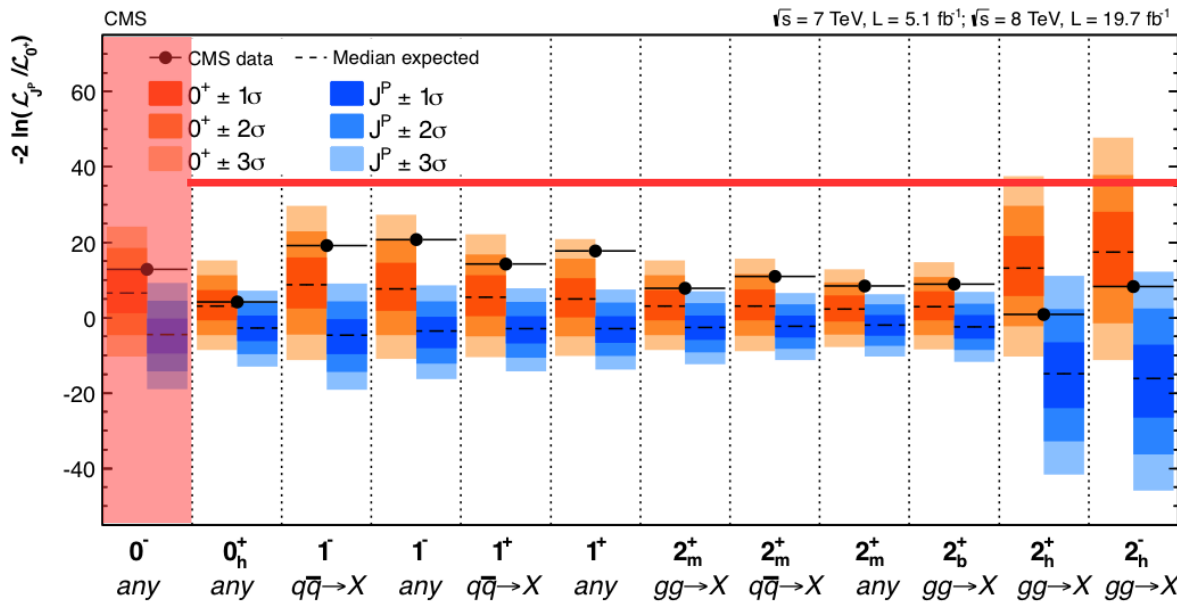
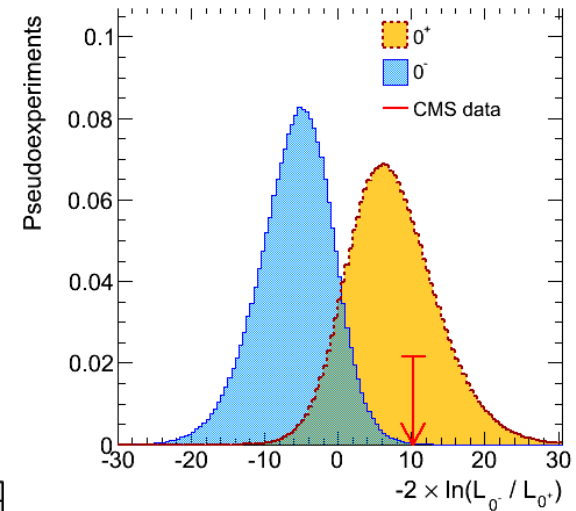
- Test statistic: $q = -2 \ln \left(\frac{\mathcal{L}(0^+ + BG)}{\mathcal{L}(J^P + BG)} \right)$.
- Expectation for given hypothesis 0^+ or J^P obtained from toy experiments.
- SM hypothesis (0^+) tested against large number of alternative hypotheses. SM favored in each case.



Would imply anomalous coupling since no 0^- couplings at tree level in the SM.

Combination into a Single Discriminating Variable

- 0^- most interesting hypothesis, since predicted in many extensions of the SM (e.g. MSSM).
- Only realistic decay channel to study this hypothesis: $H \rightarrow \tau\tau$
- SM hypothesis (0^+) tested against large number of alternative hypotheses. SM favored in each case.




Would imply anomalous coupling since no 0^- couplings at tree level in the SM.

Properties Summary

- New particle is a boson.
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV
- Decay width: $\Gamma_H < 22$ MeV
- Spin: 0 favored
- Parity: +1 favored
- CP:

Properties Summary

- New particle is a boson. 
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV
- Decay width: $\Gamma_H < 22$ MeV
- Spin: 0 favored
- Parity: +1 favored
- CP:

Properties Summary

- New particle is a boson. ✓
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV ✓
- Decay width: $\Gamma_H < 22$ MeV
- Spin: 0 favored
- Parity: +1 favored
- CP:

Properties Summary

- New particle is a boson. ✓
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV ✓
- Decay width: $\Gamma_H < 22$ MeV ✓
- Spin: 0 favored
- Parity: +1 favored
- CP:

Properties Summary

- New particle is a boson. ✓
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV ✓
- Decay width: $\Gamma_H < 22$ MeV ✓
- Spin: 0 favored ✓
- Parity: +1 favored
- CP:

Properties Summary

- New particle is a boson. ✓
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV ✓
- Decay width: $\Gamma_H < 22$ MeV ✓
- Spin: 0 favored ✓
- Parity: +1 favored ✓
- CP:

Properties Summary

- New particle is a boson. ✓
- Mass: $m_H = 125.09 \pm 0.21$ (stat.) ± 0.11 (syst.) GeV ✓
- Decay width: $\Gamma_H < 22$ MeV ✓
- Spin: 0 favored ✓
- Parity: +1 favored ✓
- CP: ?

Sneak Preview for Next Week

- Remaining questions:
 - Is this **A** Higgs bosons?
 - Is this **THE** Higgs bosons?
 - Is there **MORE THAN ONE** Higgs bosons?

Next week: Seminar