

# Teilchenphysik II (Higgs-Physik) (SS 2016)

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**Exercises Sheet 03**  
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## Exercise 9: Projection Operators

(presence)

In the lecture the projection properties of

$$\psi_L = \frac{1}{2}(1 - \gamma^5)\psi$$
$$\psi_R = \frac{1}{2}(1 + \gamma^5)\psi$$

have been discussed. It is obvious that  $\psi_L + \psi_R = \psi$ . Proof the following properties:

a) Both operators are projection operators, i.e.:

$$\left(\frac{1}{2}(1 - \gamma^5)\right)^2 = \frac{1}{2}(1 - \gamma^5)$$
$$\left(\frac{1}{2}(1 + \gamma^5)\right)^2 = \frac{1}{2}(1 + \gamma^5)$$

b) Both operators are orthogonal to each other, i.e.:

$$\frac{1}{2}(1 + \gamma^5) \cdot \frac{1}{2}(1 - \gamma^5) = 0$$

c) The projectors act on the spinors in both directions, i.e.:

$$\bar{e}\gamma^\mu \frac{1}{2}(1 - \gamma^5)\nu = \bar{e}_L\gamma^\mu\nu_L$$

d) Proof the relation:

$$\bar{e}\gamma^\mu\partial_\mu e + \bar{\nu}\gamma^\mu\partial_\mu\nu = \bar{e}_L\gamma^\mu\partial_\mu e_L + \bar{e}_R\gamma^\mu\partial_\mu e_R + \bar{\nu}_L\gamma^\mu\partial_\mu\nu_L.$$

e) Proof on the other hand the relation:

$$\bar{e}e = \bar{e}_L e_R + \bar{e}_R e_L$$

## Exercise 10: Hypercharges of Weak Isospin

(presence)

Complete the following table of hypercharges of the weak isospin for electrons and neutrinos: where  $Y_{L/R}$  is the hypercharge for left(right-)handed fermion,  $I_3$  is the third component of the weak isospin and  $Q$  is the electric charge of the corresponding particle.

$SU(2) \times U(1)$ Hypercharges			
Particle	$Y_{R/L}$	$I_3$	$Q$
$\nu$	-1	$+1/2$	
$e_L$	-1	$-1/2$	
$e_R$		0	-1

### Exercise 11: Allowed Gauge Couplings

(presence)

Which of the following triple gauge couplings are allowed in the SM?

- $\gamma WW$
- $ZWW$
- $ZZZ$
- $ZZ\gamma$
- $Z\gamma\gamma$ ;

which of the following quartic gauge couplings are allowed in the SM?

- $WWZ\gamma$
- $WW\gamma\gamma$
- $WWZZ$
- $ZZ\gamma$
- $ZZ\gamma\gamma$ ;

### Exercise 12: Chiral Transformation

(homework)

The transformation  $\chi : \psi \rightarrow \gamma^5 \psi$  is called *chiral* transformation. It turns e.g. axial vectors into vectors and vice versa.

- a) What is the adjoint of the transformed spinor?
- b) Proof that  $e_L(e_R)$  are *eigenstates* of the chiral transformation with the *eigenvalues*  $-1(+1)$ .
- c) Proof that terms of type  $\bar{\psi}\gamma^\mu\partial_\mu\psi$  are covariant under chiral transformations, while terms of type  $\bar{\psi}m\psi$  are not. As a consequence the presence of light particles is a small perturbation of a chiral symmetry in the SM Lagrangian density.