

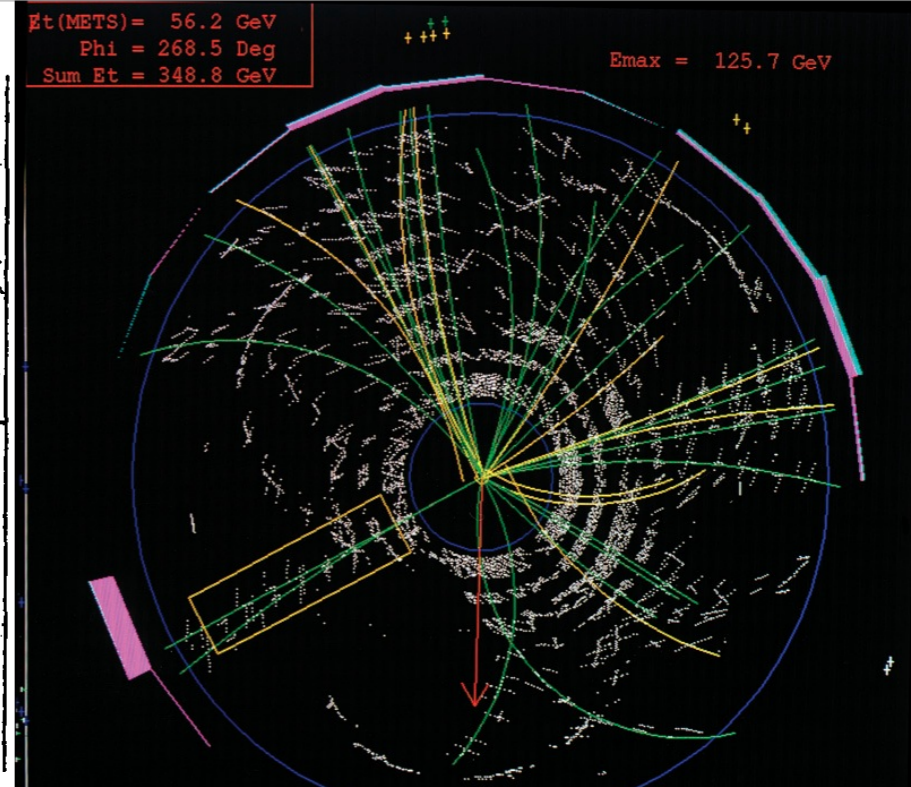
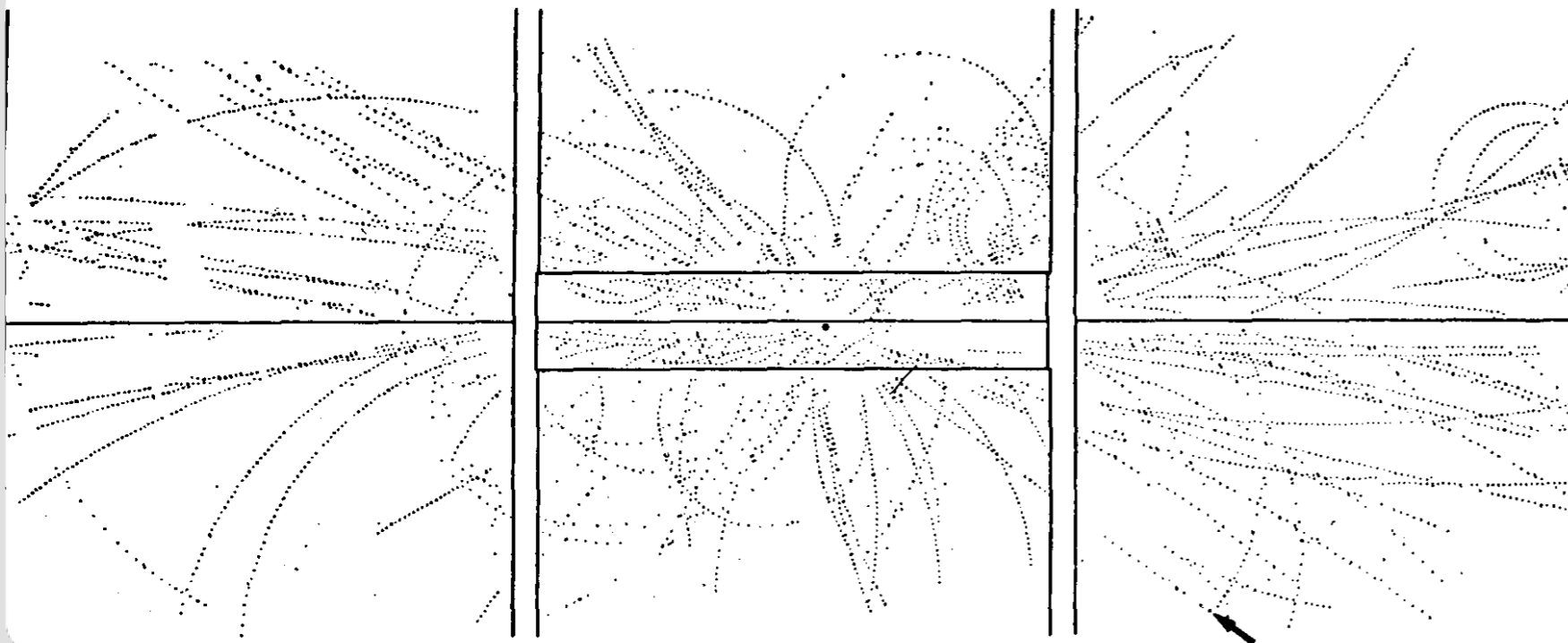
# KSETA-Course: Accelerator-Based Particle Physics

## Electroweak Physics

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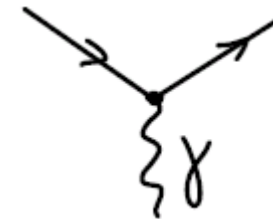
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# Elektromagnetic Interaction & CC

- Electromagnetic Interaction (Fermion with charge e)

$$\mathcal{L}_{em} = \underbrace{e}_{\text{elem. charge}} \cdot \underbrace{j_{\mu}^{em}}_{\text{EM current}} \cdot \underbrace{A^{\mu}}_{\text{photon}} = \frac{gg'}{\sqrt{g^2 + g'^2}} \bar{f} \gamma_{\mu} f A^{\mu}$$



with  $e = g \sin\vartheta_w = g' \cos\vartheta_w$  ← weak mixing angle

- Charged Current: V-A structure

$$\mathcal{L}_{cc} = \frac{g}{\sqrt{2}} [J_{\mu}^{+CC} W^{\mu-} + J_{\mu}^{-CC} W^{\mu+}]$$

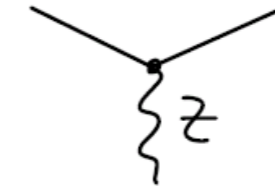
CC for quarks

$$J_{\mu}^{+CC} = (\bar{u}, \bar{c}, \bar{t}) \underbrace{\gamma_{\mu} \frac{1}{2} (1 - \gamma_5)}_{\text{V-A}} V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

← quark mixing



# NC & Selfcoupling

- Neutral Currents  $\mathcal{L}_{NC} = -\frac{\sqrt{g^2 + g'^2}}{2} J_\mu^{NC} Z^\mu$  

with:

$$J_\mu^{NC} = \bar{f} \gamma_\mu \frac{1}{2} (g_V^f - g_A^f \gamma_5) f$$

vector-coupling
axial-coupling

$$g_V^f = (I_3^f - 2q^f \sin^2 \vartheta_W) \quad g_A^f = I_3^f$$

( $I_3^f$  third component of isospin,  $q^f$  fermion charge)

- Selfcouplings of gauge bosons: only  $WW\gamma$ ,  $WWZ$

$$\mathcal{L}_{WW\gamma} = -ie [A_\mu (W^{-\mu\nu} W_\nu^+ - W^{+\mu\nu} W_\nu^-) + F_{\mu\nu} W^{+\mu} W^{-\nu}]$$

$$\mathcal{L}_{WWZ} = -ie \cot \vartheta_w [Z_\mu (W^{-\mu\nu} W_\nu^+ - W^{+\mu\nu} W_\nu^-) + Z_{\mu\nu} W^{+\mu} W^{-\nu}]$$

- +quartic couplings  $WWWW$ ,  $WWZZ$ ,  $WWZ\gamma$ ,  $WW\gamma\gamma$

# Cross Section

- Resonant (s-channel-) production von Z-bosons in  $e^+e^-$ -scattering
  - Photon and Z-boson: identical quantum numbers ( $J^P = 1^-$ )  $\rightarrow$  interference
  - Matrix-element:

$$|M|^2 = \left| \begin{array}{c} e^- \quad \bar{f} \\ \searrow \quad \nearrow \\ \gamma^* \\ \nearrow \quad \searrow \\ e^+ \quad f \end{array} + \begin{array}{c} e^- \quad \bar{f} \\ \searrow \quad \nearrow \\ Z \\ \nearrow \quad \searrow \\ e^+ \quad f \end{array} \right|^2$$

- cross section:  $\sigma(e^+e^- \rightarrow f\bar{f}) = \sigma_{\gamma^*} + \sigma_{\gamma^*/Z} + \sigma_Z$
- $\sqrt{s} \ll m_Z$ : photon exchange dominant  $\rightarrow$  simple QED
- $\sqrt{s} \simeq m_Z$ : Z-boson-exchange dominant, photon- and interference-term negligible

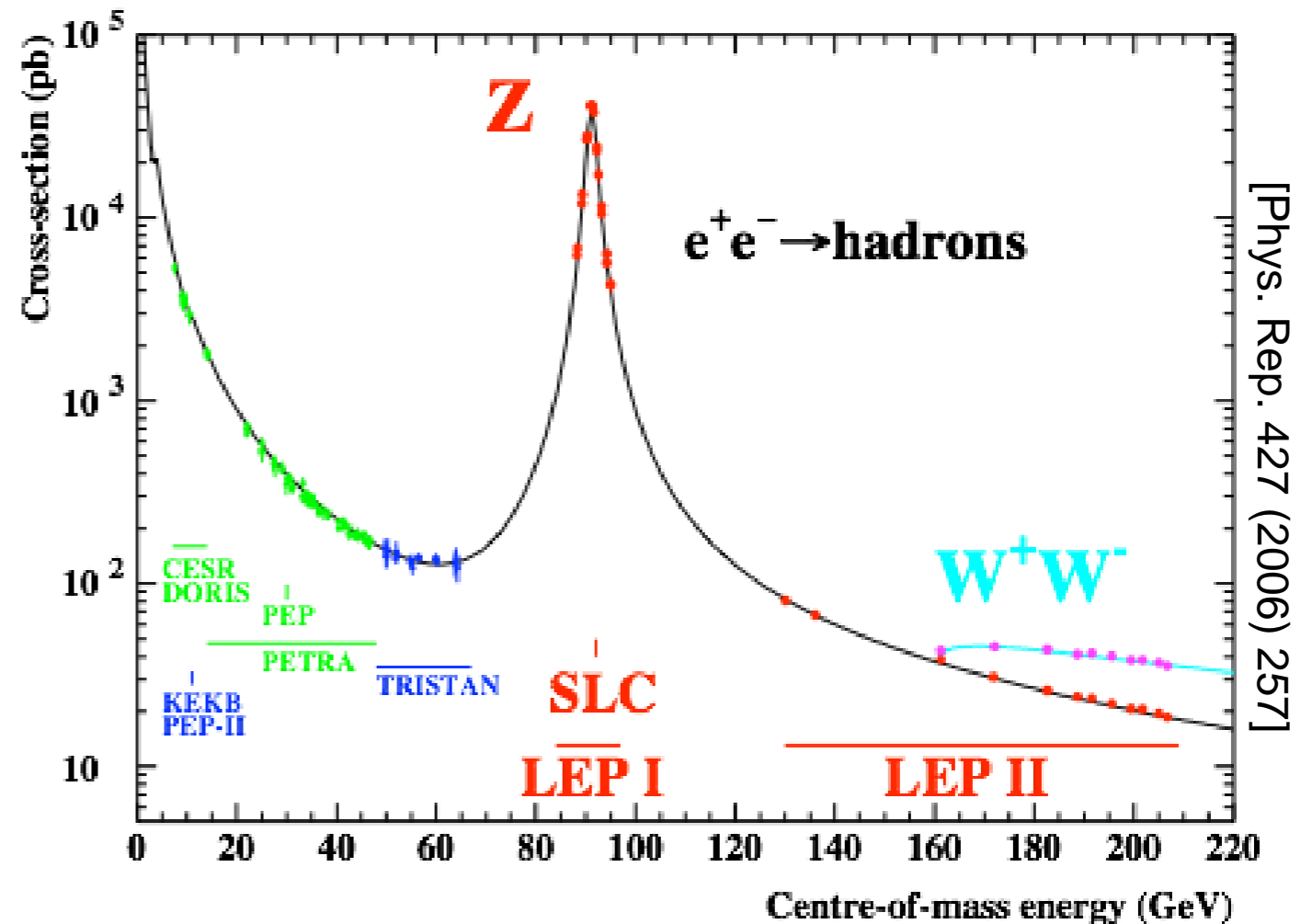
# Width of the Z-Resonance

- Z = unstable particle
  - finite lifetime  $\tau_Z$ 
    - decaywidth  $\Gamma_Z = 1/\tau_Z$  („smeared” mass)
  - modified propagator
- Decay width
  - sum of partial decay widths („partial widths”)
  - for  $\sqrt{s} \simeq m_Z$ :

$$\Gamma_Z = \sum_f \Gamma_f = \sum_{q=u,d,s,c,b} \Gamma_q + \sum_{\ell=e,\mu,\tau} \Gamma_\ell + \sum_{\nu=\nu_e,\nu_\mu,\nu_\tau} \Gamma_\nu$$

- in leading order:

$$\Gamma_f = N_C^f \frac{G_F m_Z^3}{6\sqrt{2}\pi} \left[ (g_V^f)^2 + (g_A^f)^2 \right]$$



# Number of light neutrinos

- Cross section for a fermion f:

$$\sigma_f = \underbrace{\frac{12\pi}{m_Z^2} \cdot \frac{\Gamma_e \cdot \Gamma_f}{\Gamma_Z^2}}_{\sigma_f^0} \cdot \frac{s \cdot \Gamma_Z^2}{(s - m_Z^2)^2 + s^2 \frac{\Gamma_Z^2}{m_Z^2}}$$

Breit-Wigner  
 $\Rightarrow 1$  for  $s = m_Z^2$

- Compare different cross sections to find  $\Gamma_{inv}$  from  $\Gamma_Z$  and other f

$$\frac{\Gamma_{inv}}{\Gamma_e} \equiv R_{inv}^0 = \frac{\Gamma_Z}{\Gamma_e} - 3 - R_e^0 = \sqrt{\frac{12\pi}{m_Z^2} \cdot \frac{R_e^0}{\sigma_{had}^0}} - 3 - R_e^0$$

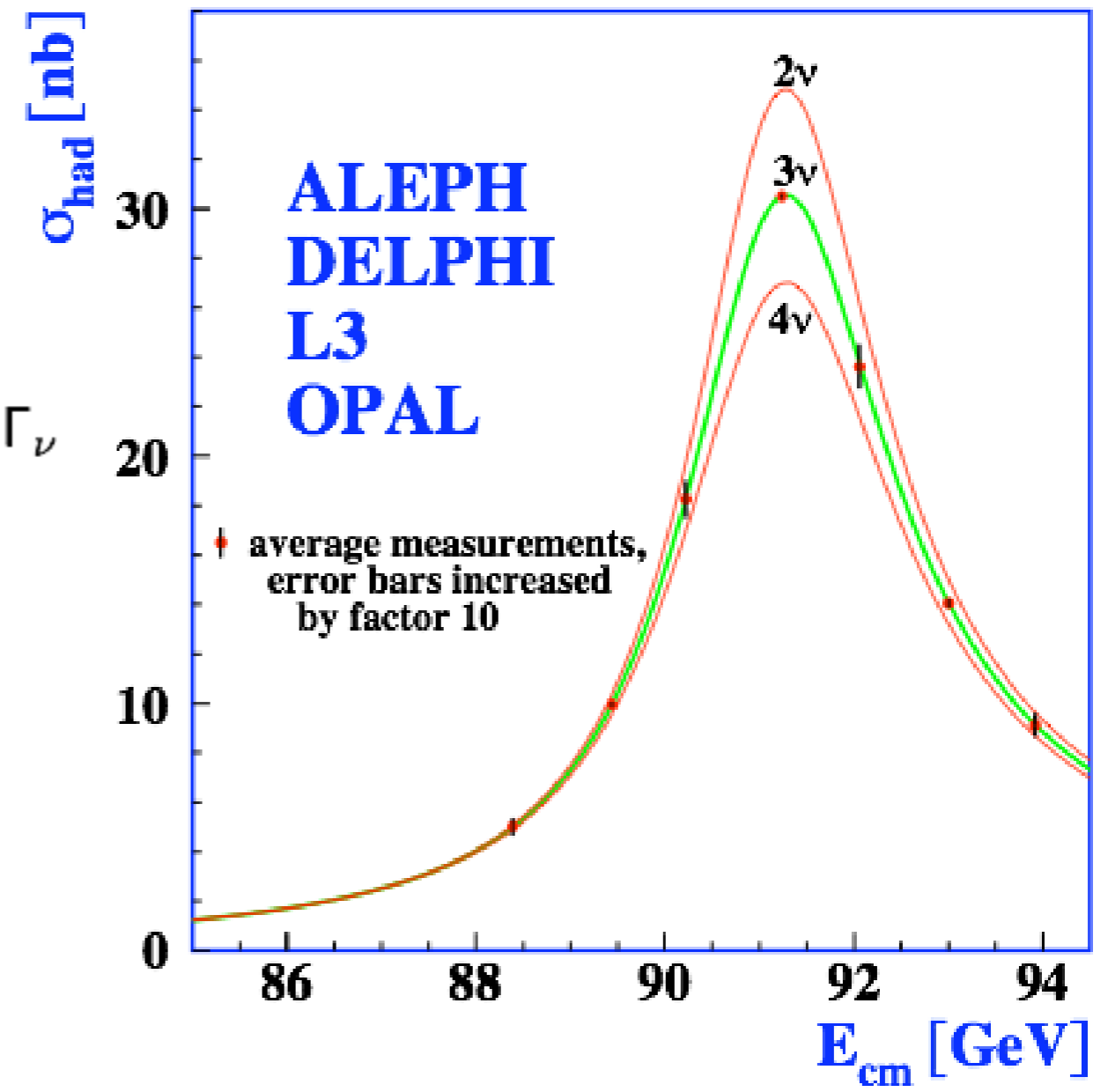
- Divide  $\Gamma_{inv}$  by  $\Gamma_\nu$  derived from theory

$$\Rightarrow N_\nu = 2.9840(82)$$

# Number of neutrinos in pictures

$$\sigma_f = \frac{12\pi}{m_Z^2} \cdot \frac{\Gamma_e \cdot \Gamma_f}{\Gamma_Z^2} \cdot \frac{s \cdot \Gamma_Z^2}{(s - m_Z^2)^2 + s^2 \frac{\Gamma_Z^2}{m_Z^2}}$$

$$\Gamma_Z = \sum_f \Gamma_f = \sum_{q=u,d,s,c,b} \Gamma_q + \sum_{\ell=e,\mu,\tau} \Gamma_\ell + \sum_{\nu=\nu_e,\nu_\mu,\nu_\tau} \Gamma_\nu$$

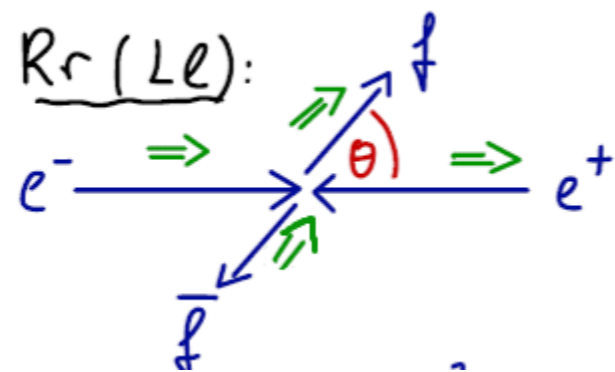


[Phys. Rep. 427 (2006) 257]

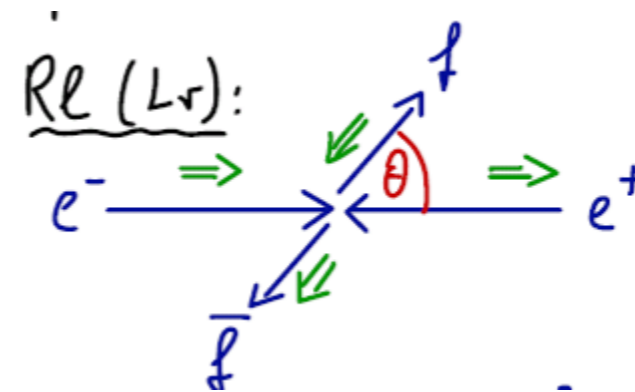
# $\sqrt{s} \ll m_Z$ : differential Xsec

$\sqrt{s} \ll m_Z$ : photon exchange (pure QED)

helicities: photon  $\Rightarrow$  spin 1



$$\sigma \sim (1 + \cos \vartheta)^2$$



$$\sigma \sim (1 - \cos \vartheta)^2$$

$$\Rightarrow \frac{d\sigma_\gamma}{d \cos \vartheta} = N_c^f \cdot q_f^2 \cdot \frac{\pi \alpha^2}{2s} (1 + \cos^2 \vartheta)$$

# colors

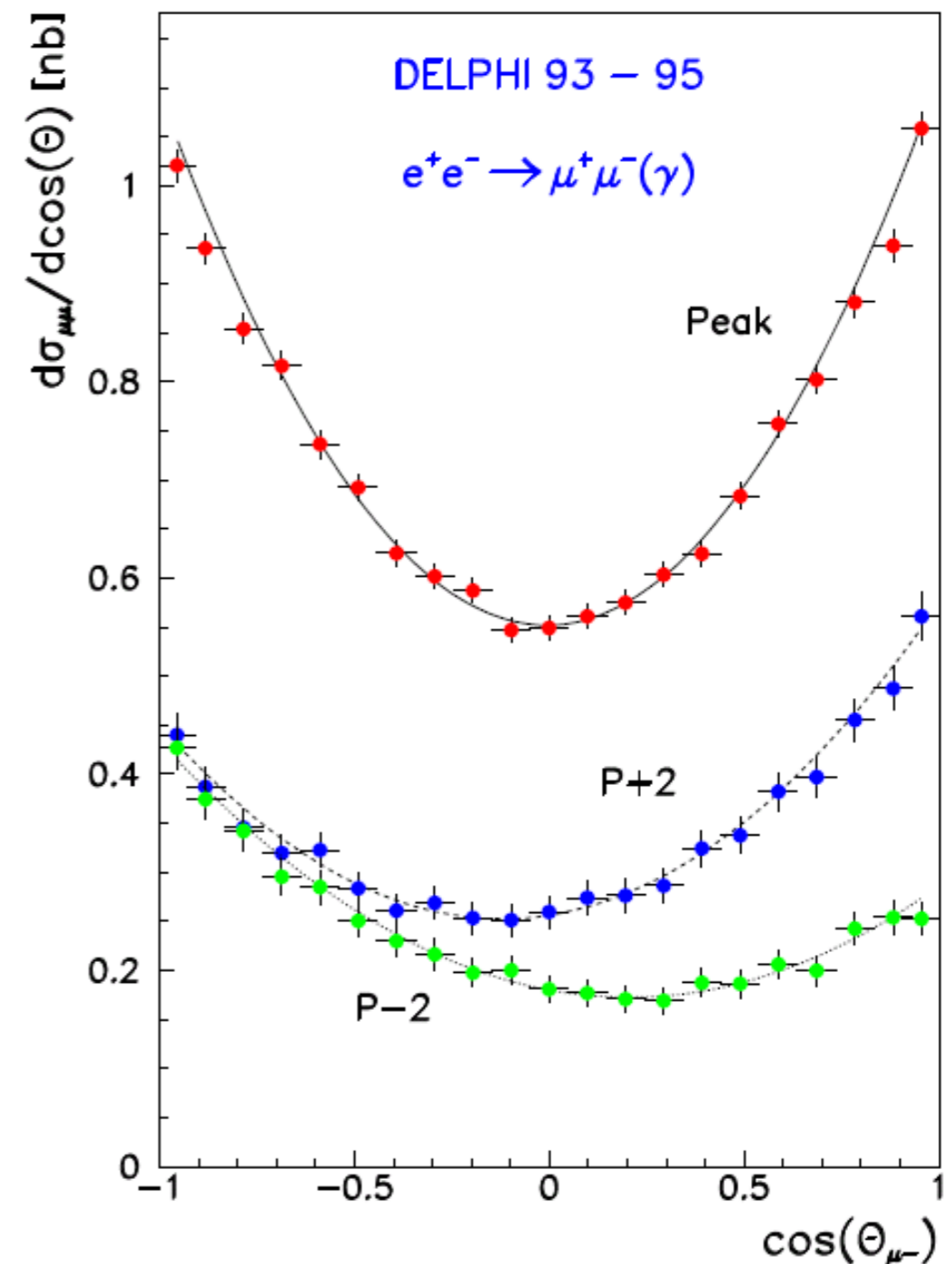
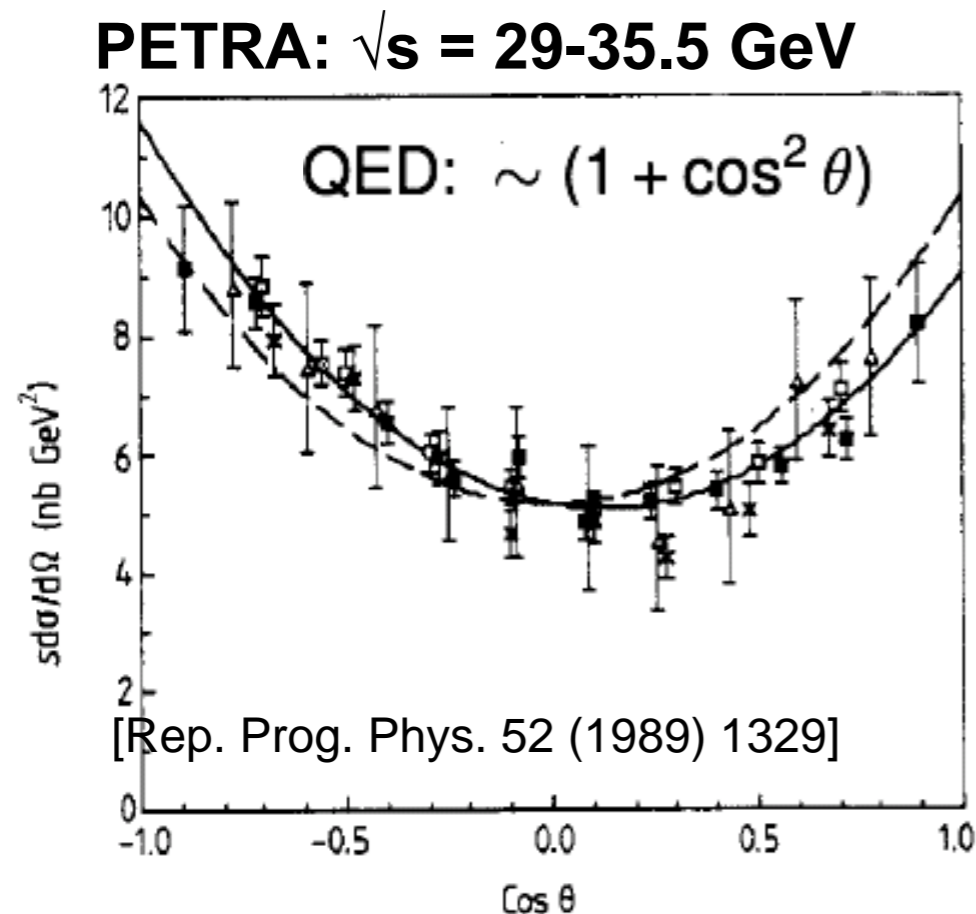
charge



# $\sqrt{s} \ll m_Z$ : Angular Distribution

LEP:  $\sqrt{s} = m_Z \pm 2 \text{ GeV}$

- Before LEP: measurements at PETRA (DESY)  $\rightarrow$  first deviations from pure QED
- LEP:  $\gamma^*/Z$ -interference und Z central physics topic



[Phys. Rep. 427 (2006) 257]

# Asymmetries

- Generic definition of an **asymmetry**:  
Partition a dataset into two parts  $X, Y \rightarrow A = \frac{X - Y}{X + Y}$
- Why asymmetries?
  - Asymmetries = **Ratios**, not absolute rates
  - Backgrounds and systematic effects on numerator/denominator equal or similar  
→ **Reduction of uncertainties** due to cancellations
  - Increased sensitivity to **small differences**

# Differential Cross Section

Angular distribution for Z exchange:

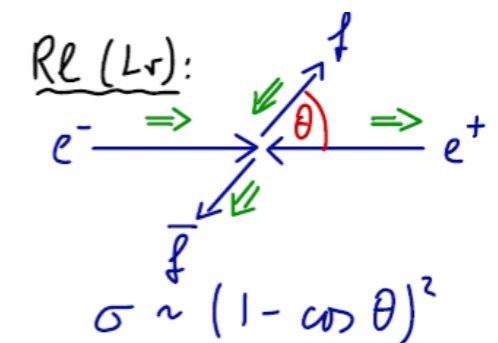
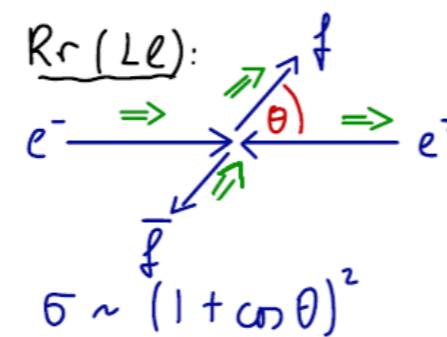
→ 4 helicities (using  $g_R = g_V + g_A, g_L = g_V - g_A$ )

$$\frac{d\sigma_f}{d\cos\theta} \sim (g_L^e)^2 (g_L^f) (1 + \cos\vartheta)^2$$

$$\frac{d\sigma_f}{d\cos\theta} \sim (g_L^e)^2 (g_R^f) (1 - \cos\vartheta)^2$$

$$\frac{d\sigma_f}{d\cos\theta} \sim (g_R^e)^2 (g_R^f) (1 + \cos\vartheta)^2$$

$$\frac{d\sigma_f}{d\cos\theta} \sim (g_R^e)^2 (g_L^f) (1 - \cos\vartheta)^2$$



$$\rightarrow \frac{d\sigma_f}{d\cos\theta} = \frac{3}{8} \sigma_f \left[ (1 + \cos^2\vartheta) + 2 A_e A_f \cos\vartheta \right]$$

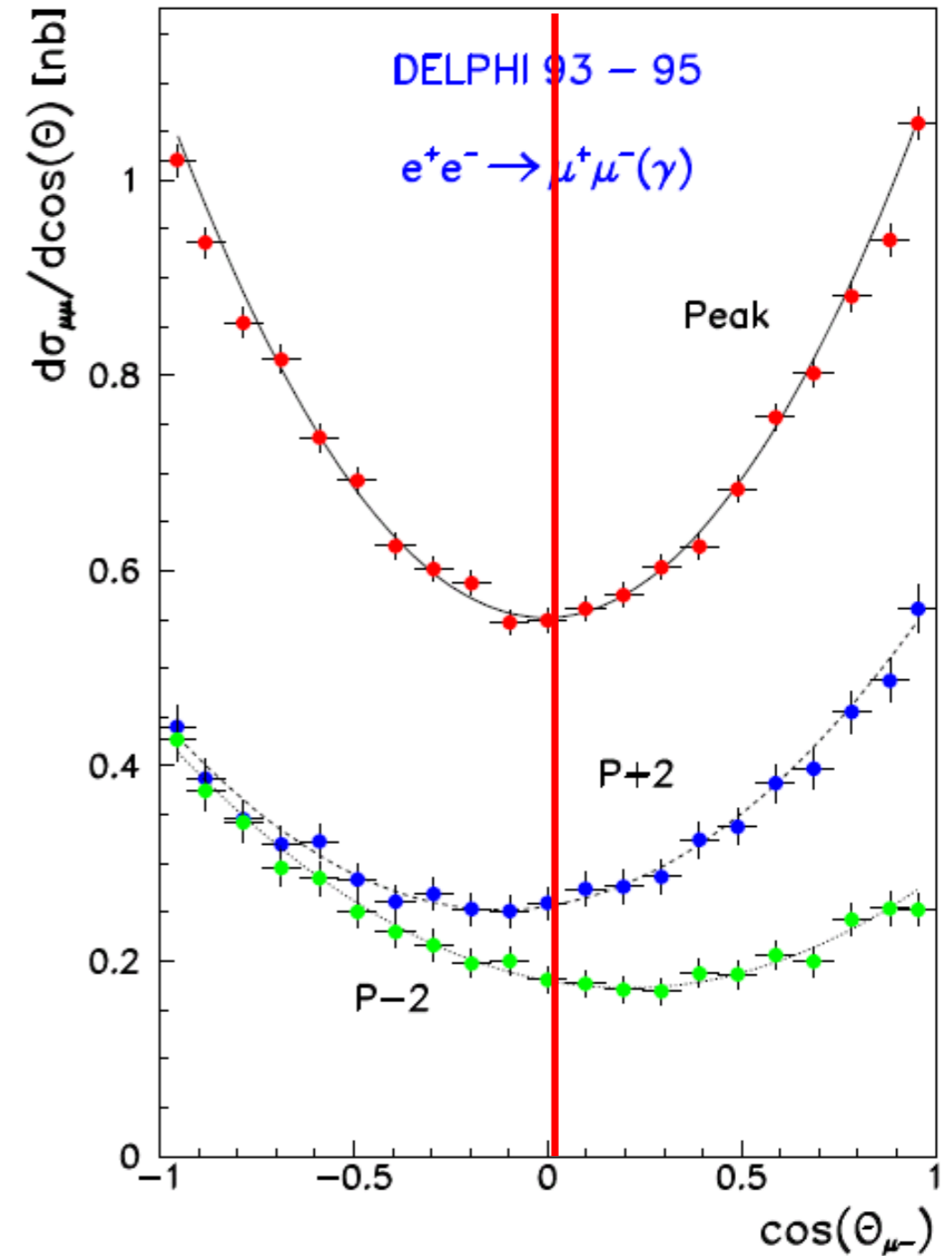
$$A_f = \frac{(g_L^f)^2 - (g_R^f)^2}{(g_L^f)^2 + (g_R^f)^2} = 2 \frac{g_V^f / g_A^f}{1 + \left( \frac{g_V^f}{g_A^f} \right)^2}$$

access ratio  $\left( \frac{g_V^f}{g_A^f} \right)$

# Forward-Backward-Asymmetry

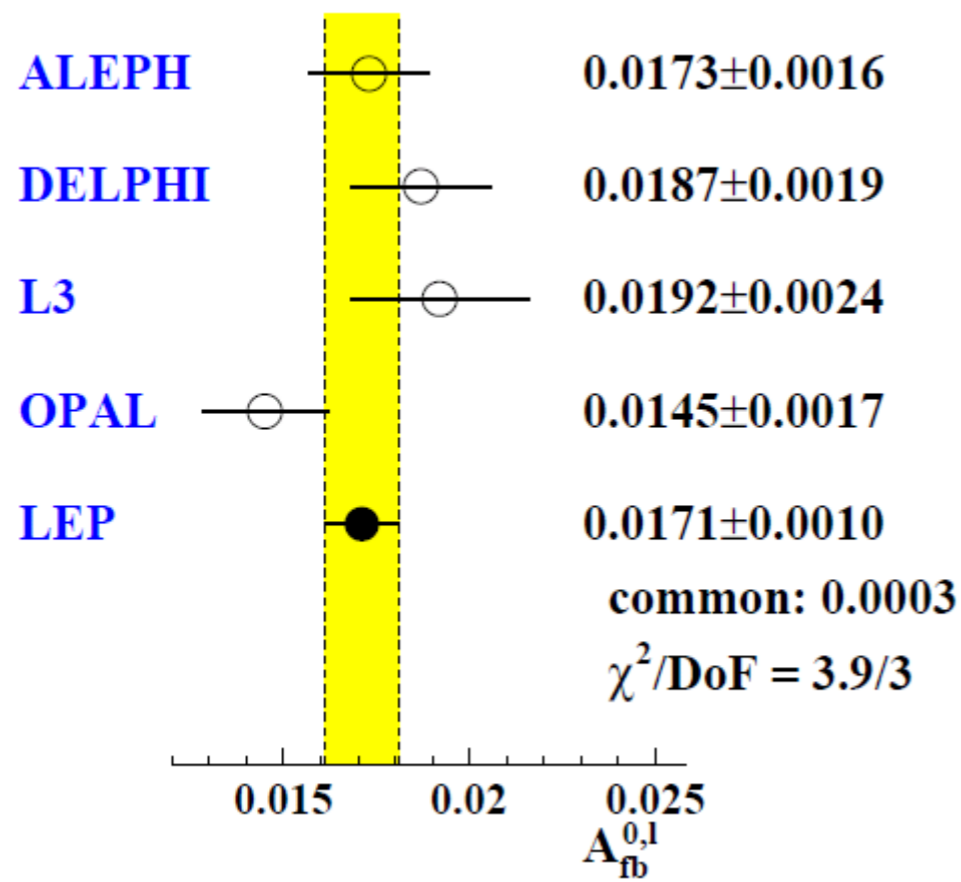
$$\sigma_F \equiv \int_0^{\pi/2} \frac{d\sigma}{d \cos \vartheta} d\vartheta \quad \sigma_B \equiv \int_{\pi/2}^{\pi} \frac{d\sigma}{d \cos \vartheta} d\vartheta$$

$$A_{FB} \equiv \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \dots = \frac{3}{4} A_e A_f$$

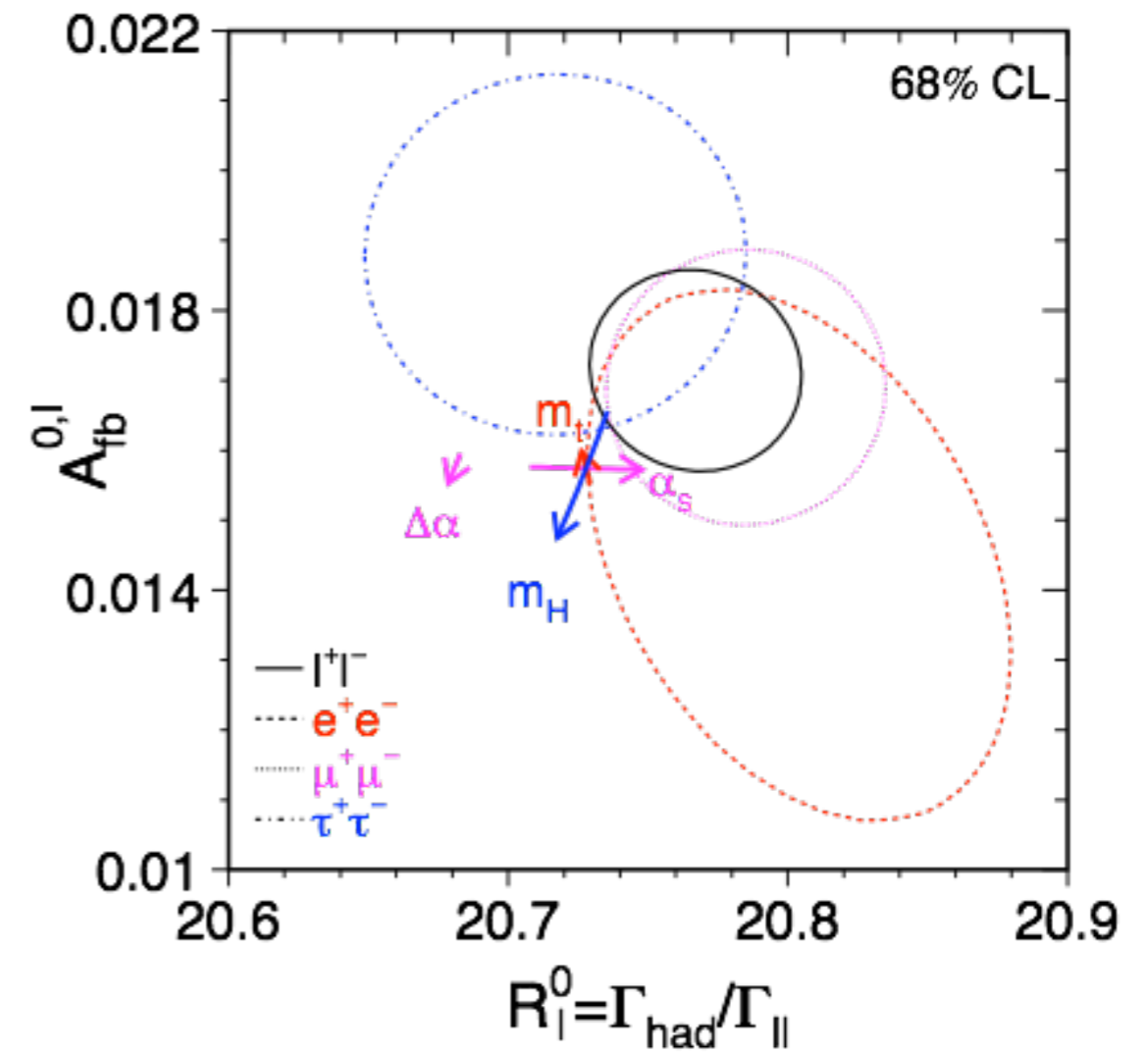


# $A_{FB}$ : Results from LEP

## LEP-average: $A_{FB}$ for leptons



## $A_{FB}$ separately for e, $\mu$ , $\tau$ vs. $R^0$



[Phys. Rep. 427 (2006) 257]

# Final State Polarisation

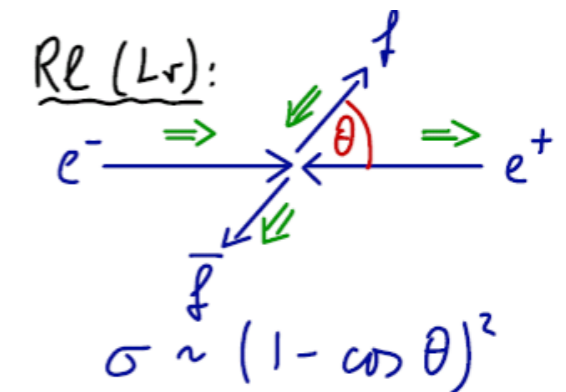
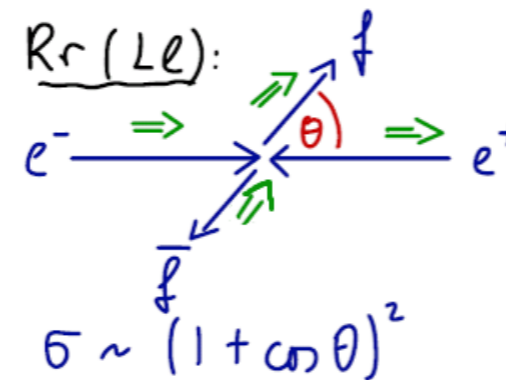
- Measure the **polarization P** of the outgoing particles

- $$P_f \equiv \frac{\sigma_{L^-} - \sigma_R}{\sigma_{L^-} + \sigma_R}$$

- No initial state polarization at LEP

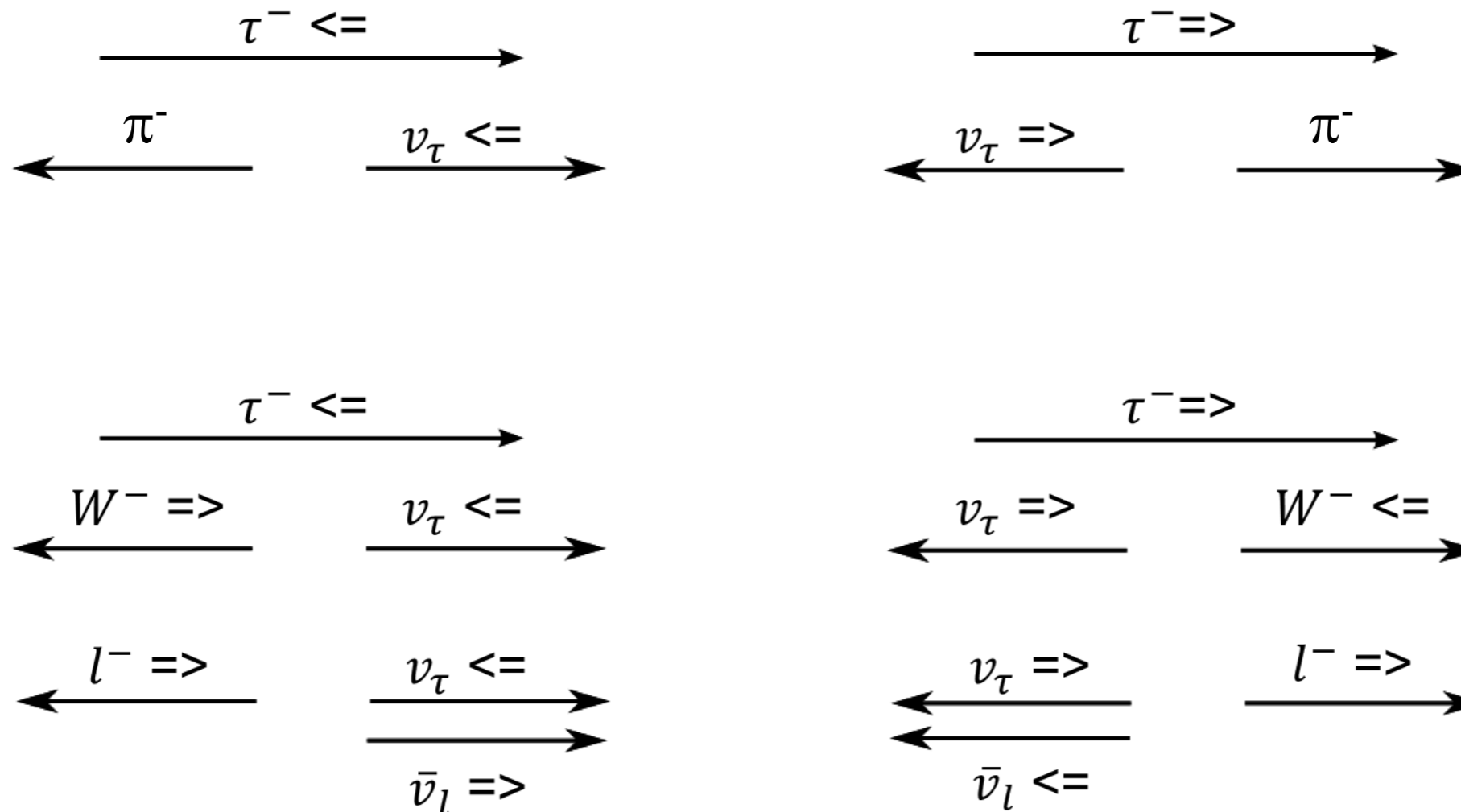
$$\Rightarrow P_f(\cos \vartheta) = \frac{A_f(1 + \cos^2 \vartheta) + 2A_e \cos \vartheta}{(1 + \cos^2 \vartheta) + \frac{8}{3}A_{fFB} \cos \vartheta}$$

- Separate access to  $A_f$  and  $A_e$



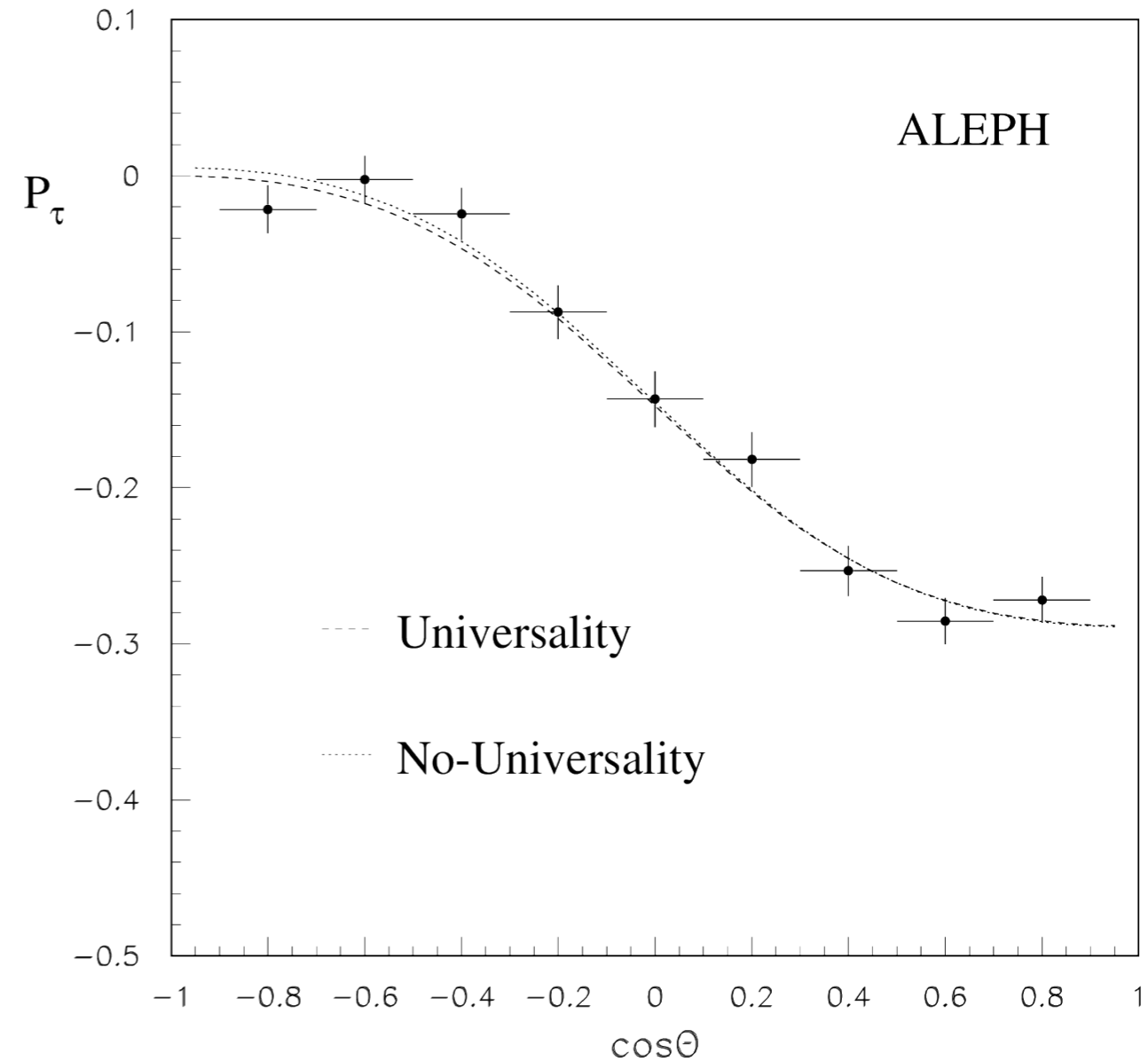
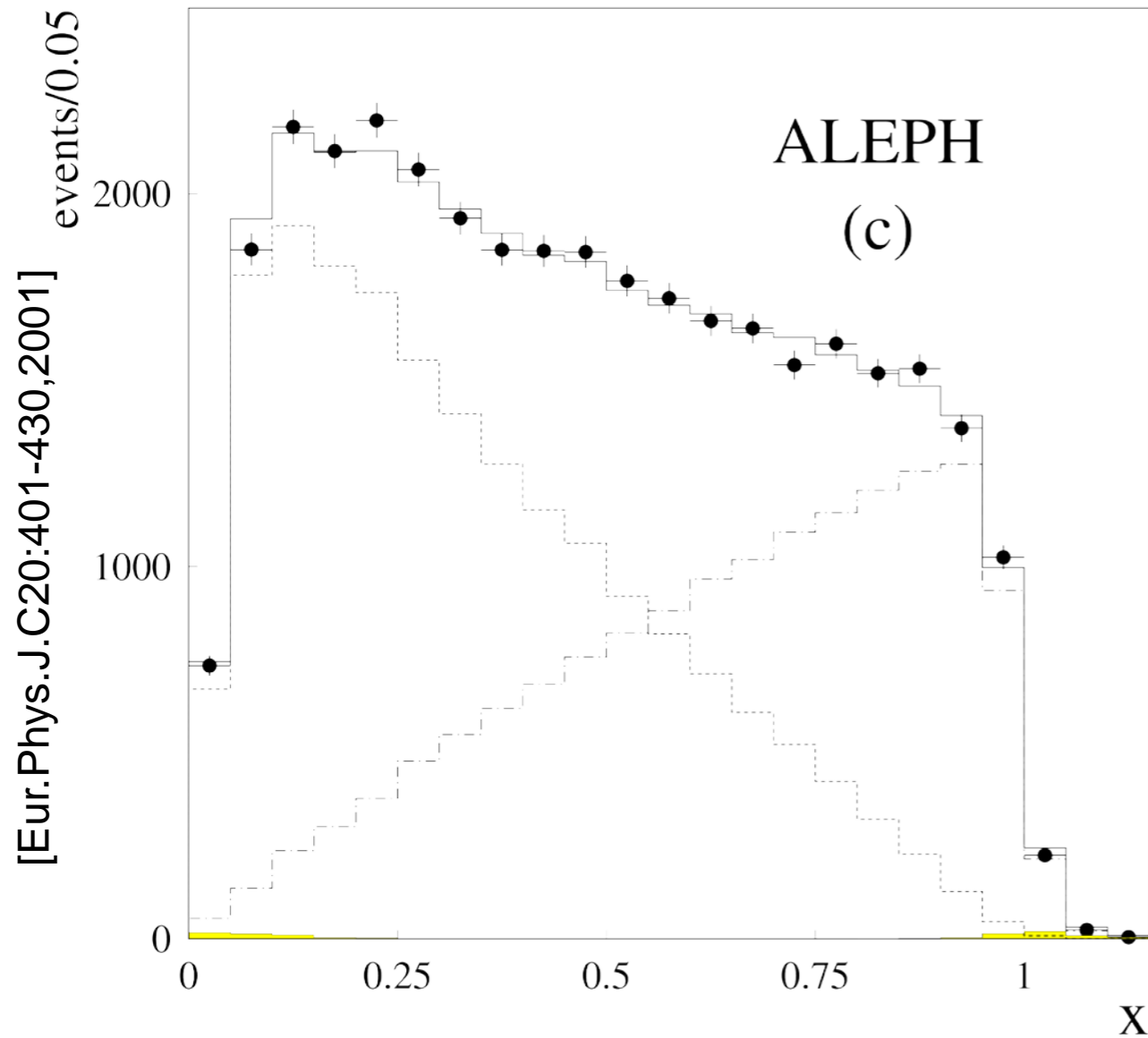
# Polarisation Measurement

- $\tau$ -lepton has self-analyzing decay



- Visible daughter(s) carry larger (smaller) momentum fraction for right- (left-) handed  $\tau$ -leptons

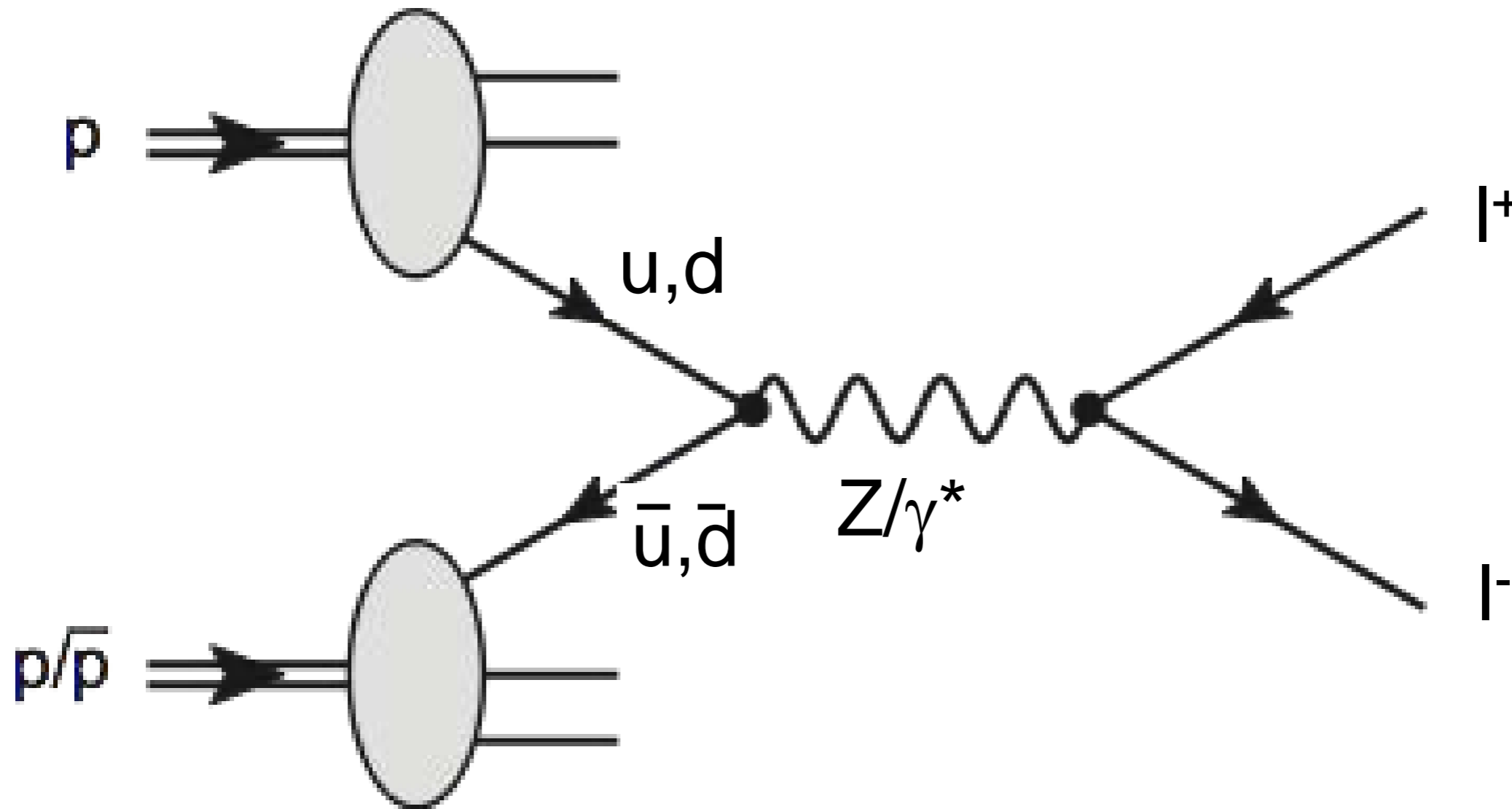
# Polarisation: Results



Fit for  $P$  with  $A_e = A_\tau$  and  $A_e \neq A_\tau$   
 $\Rightarrow$  test lepton universality



# Z at hadron colliders



- Lepton final states preferred for low backgrounds, precise reco
- Learn about proton structure (See other lecture)
- Unknown initial state complicates studies of EWK physics

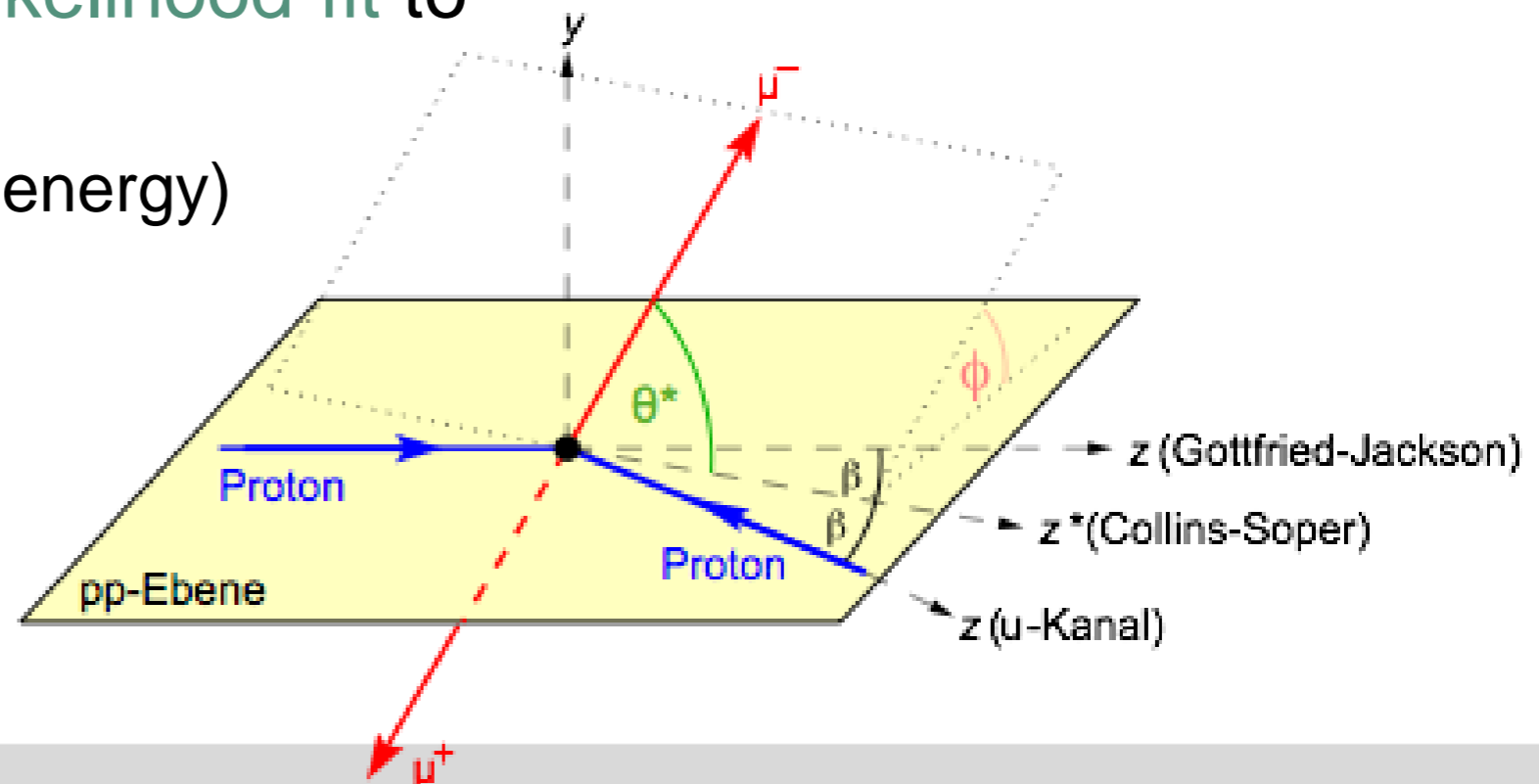
# Weak mixing angle

- Drell-Yan-Prozess:  $qq \rightarrow \gamma^*/Z \rightarrow ff$ 
  - Standard model: **relative couplings** of fermions to  $\gamma/Z$  given by  $\sin^2 \theta_{W,\text{eff}}^f$

$$\sin^2 \theta_{W,\text{eff}}^f = \frac{I_3^f}{2q^f} \left( 1 - \frac{g_V^f}{g_A^f} \right)$$

- Assumption: differential cross section and PDFs **known**  
 → Extraktion von  $\sin^2 \theta_{W,\text{eff}}^f$
- Tricky: which direction did the quark/antiquark come from?
- Simultaneous **maximum-likelihood-fit** to

- Myon pair mass  $M(\mu\mu)$   
 (= partonic center of mass energy)
- Myon pair rapidity  $Y$
- Myon angle  $\theta^*$   
 (Collins-Soper-frame)



# Weak Mixing Angle

- CMS-results:

$$\sin^2 \theta_{W,\text{eff}}^f = 0.2287 \pm 0.0020 \text{ (stat.)} \pm 0.0025 \text{ (syst.)}$$

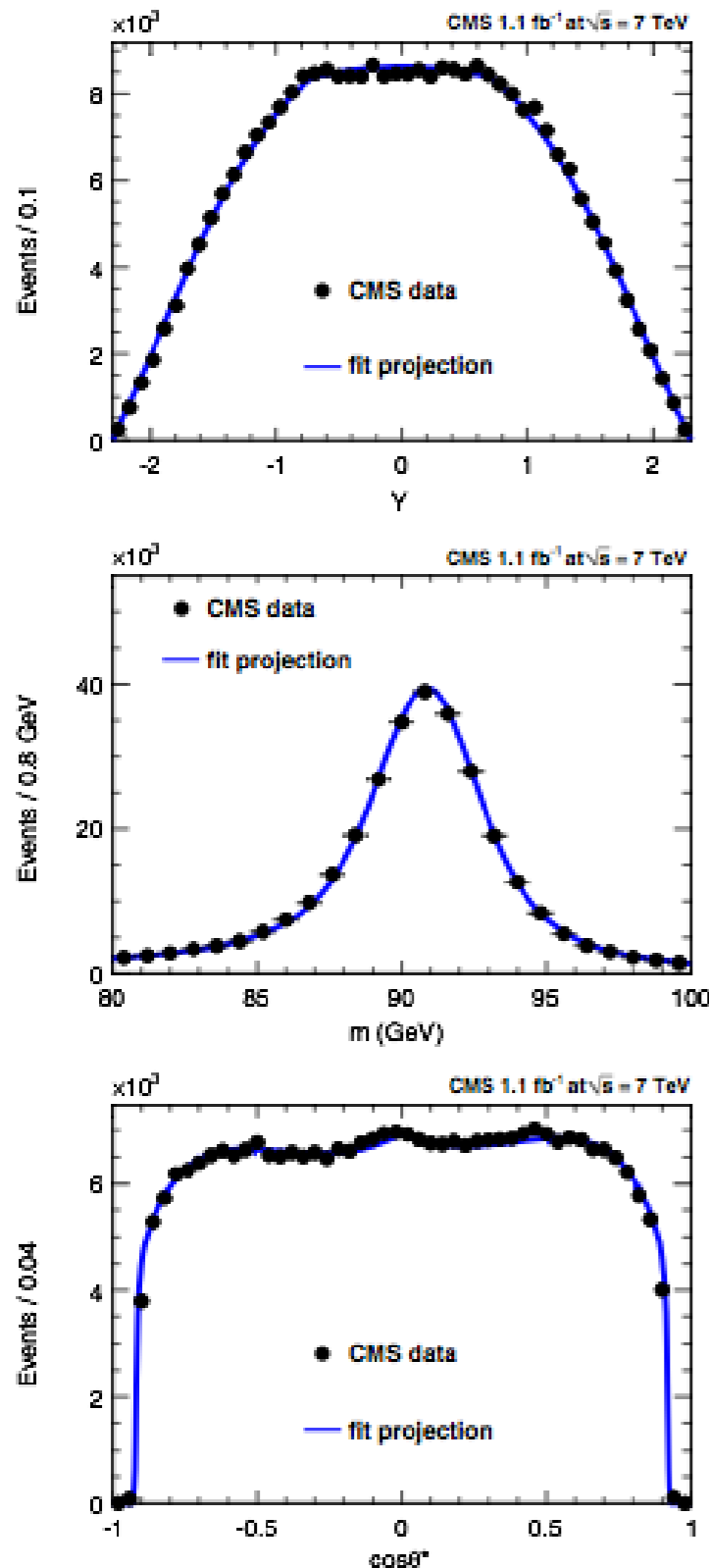
- consistent with LEP- resultat  
( $\sin^2 \theta_{W,\text{eff}}^f = 0.23153 \pm 0.00016$ )

- uncertainty: 1.4% ( LEP: 0.07%)

- Systematic uncertainties:

source	correction	uncertainty
PDF	–	$\pm 0.0013$
FSR	–	$\pm 0.0011$
LO model (EWK)	–	$\pm 0.0002$
LO model (QCD)	+0.0012	$\pm 0.0012$
resolution and alignment	+0.0007	$\pm 0.0013$
efficiency and acceptance	–	$\pm 0.0003$
background	–	$\pm 0.0001$
total	+0.0019	$\pm 0.0025$

[Phys. Rev. D84 (2011) 112002]

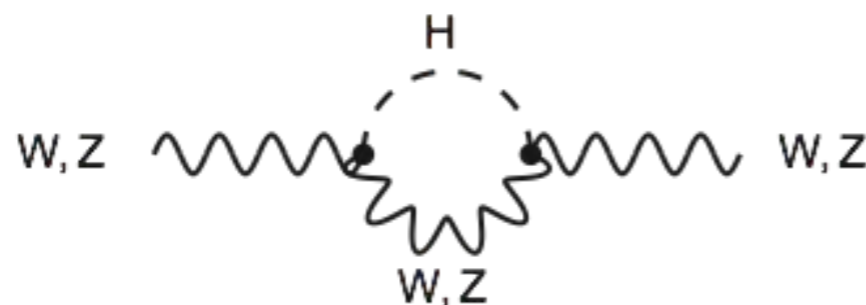


# Measuring the W-mass

- electroweak theory predicts
  - Connection of W- and Z-mass by the weak mixing angle

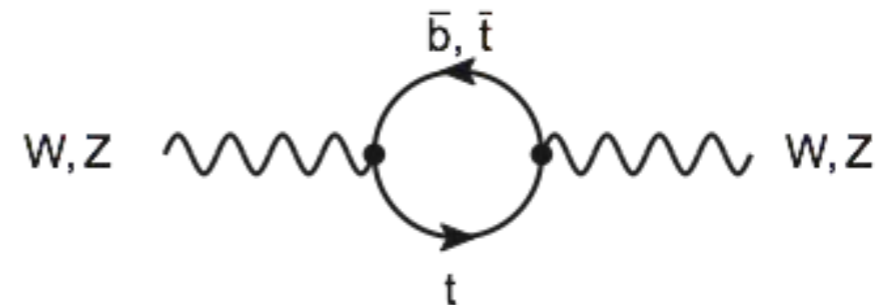
$$m_W^2 = \frac{g^2 v^2}{4}, \quad m_Z^2 = \frac{v^2}{4} (g^2 + g'^2) \quad \rightarrow \quad \rho_0 = \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = 1$$

- Connection with Top-quarks and Higgs-Boson masses through loop diagram, i.e. „self-energy” of W and Z



$$\sim g' \ln(m_H / m_W)$$

weak dependence  
(logarithmic)



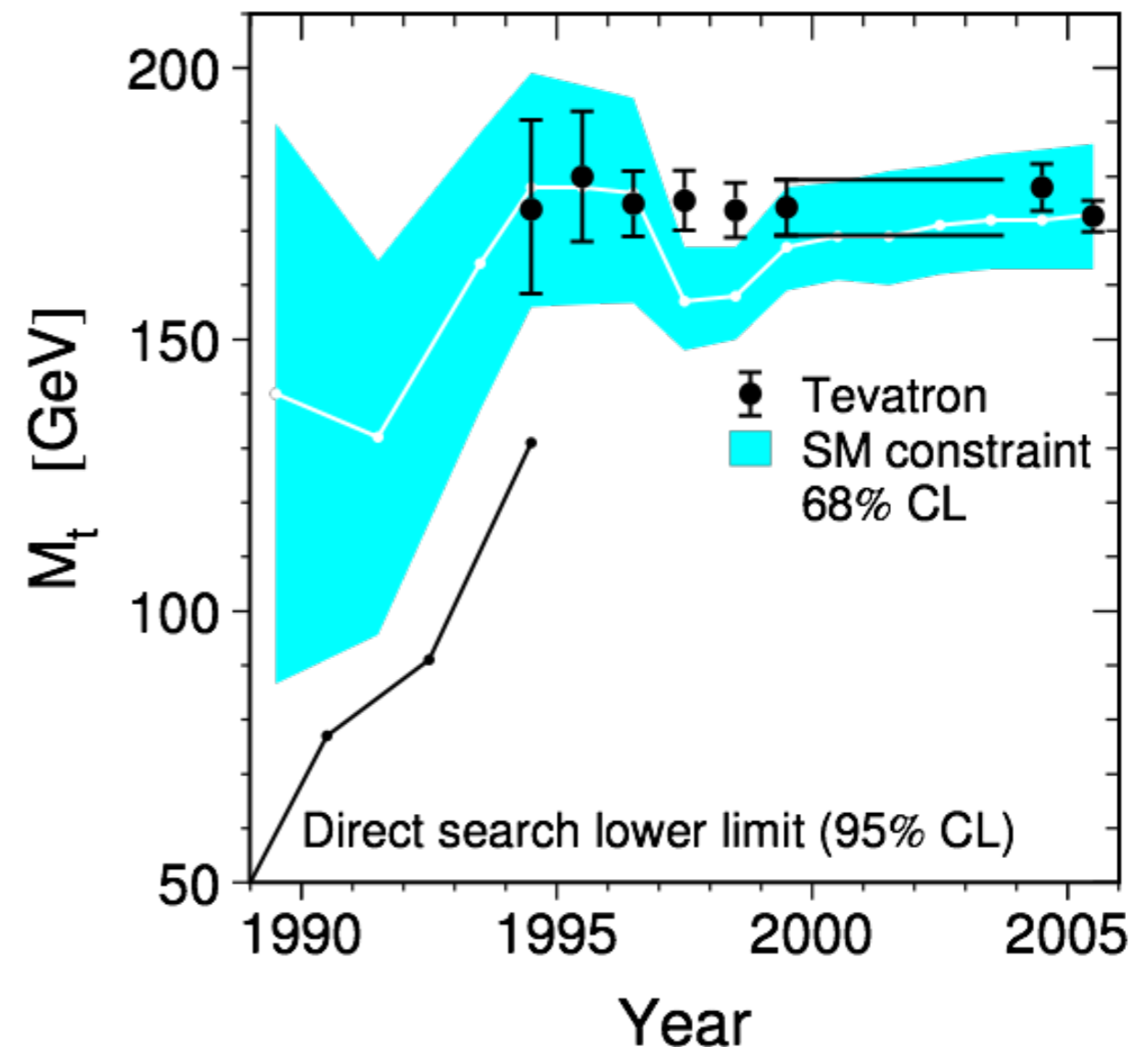
$$\sim G_F m_t^2$$

strong dependence  
(quadratic)

# Measuring the W-mass

- Looking for indirect effect needs **highest precision**
- Z-mass: **extremely precise** measurements at LEP (uncertainty:  $2 \cdot 10^{-5}$ )
- W-mass: LEP + Tevatron
- **Prediction** of Top-quark mass before discovery
- bounds on **allowed Higgs-boson masses** before discovery

vgl. Tevatron (2012):  
 $m_t = 173.2 \pm 0.9 \text{ GeV}$

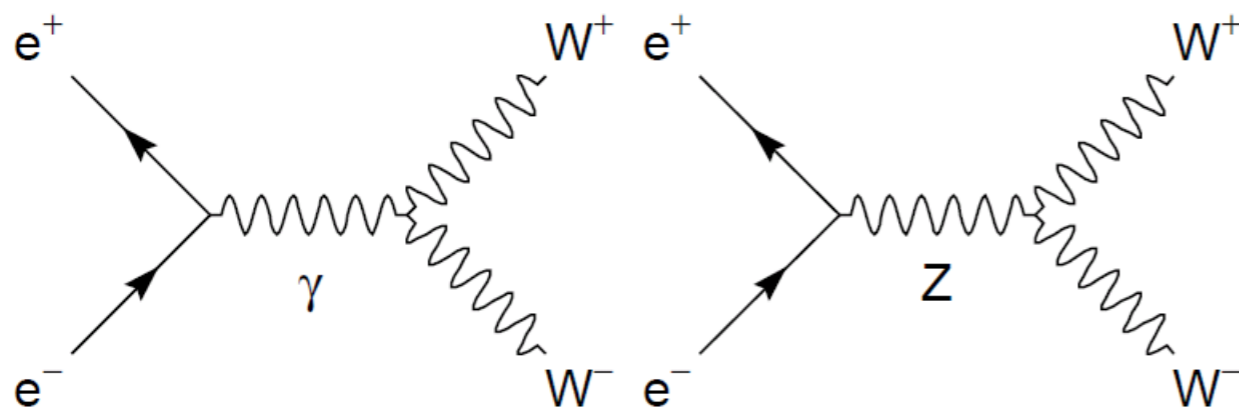


[Phys. Rept. 427 (2006) 257]

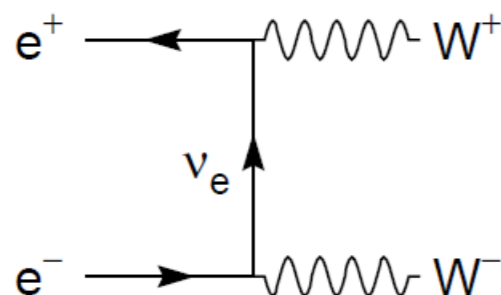
# W-pair creation at LEP-II

- LEP-II: passes **kinematic Threshold** for W-boson-pair creation

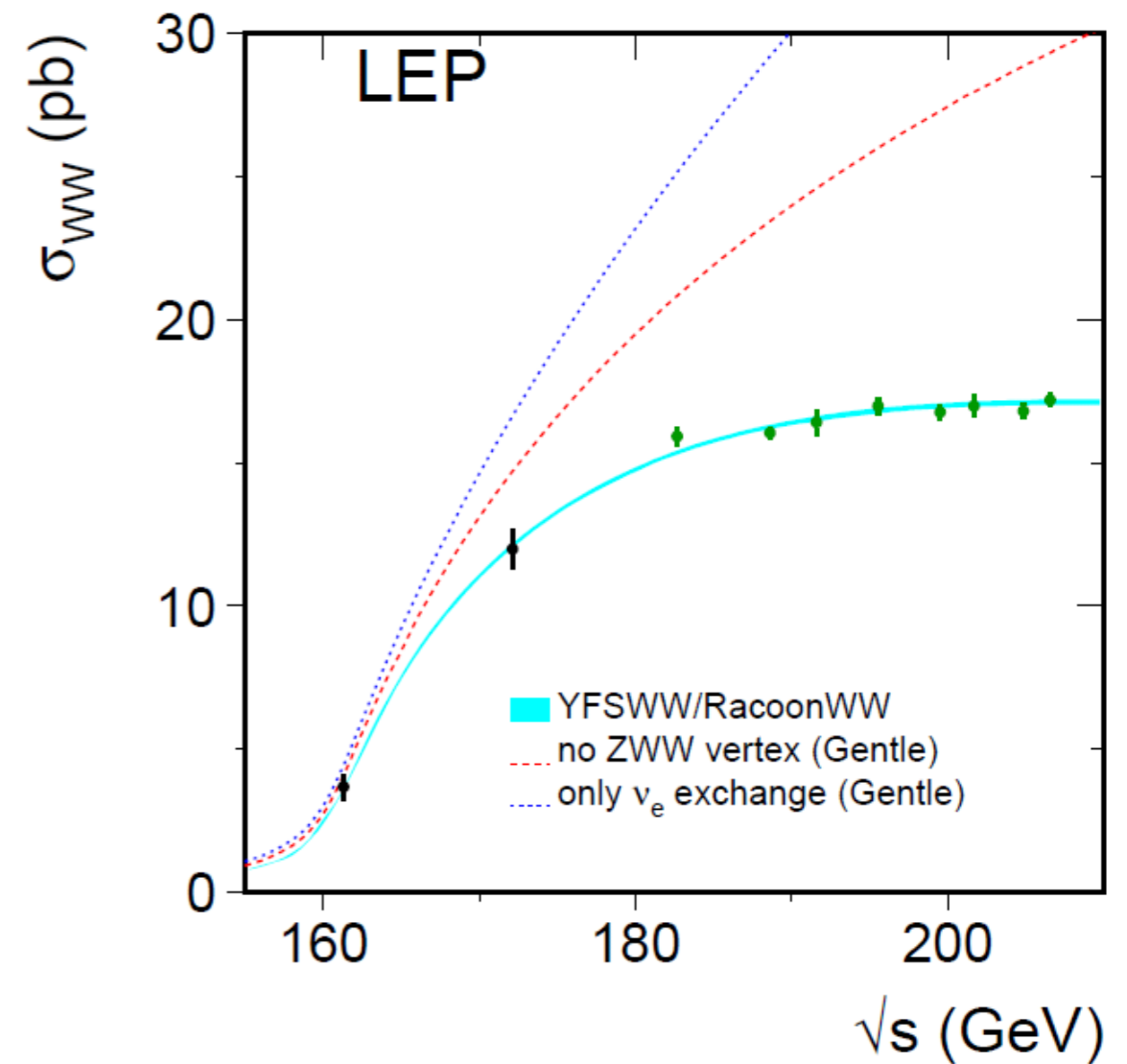
- Feynman-diagrams (Born)
  - TGC:  $\gamma WW$  und  $ZWW$



- Neutrino-exchange



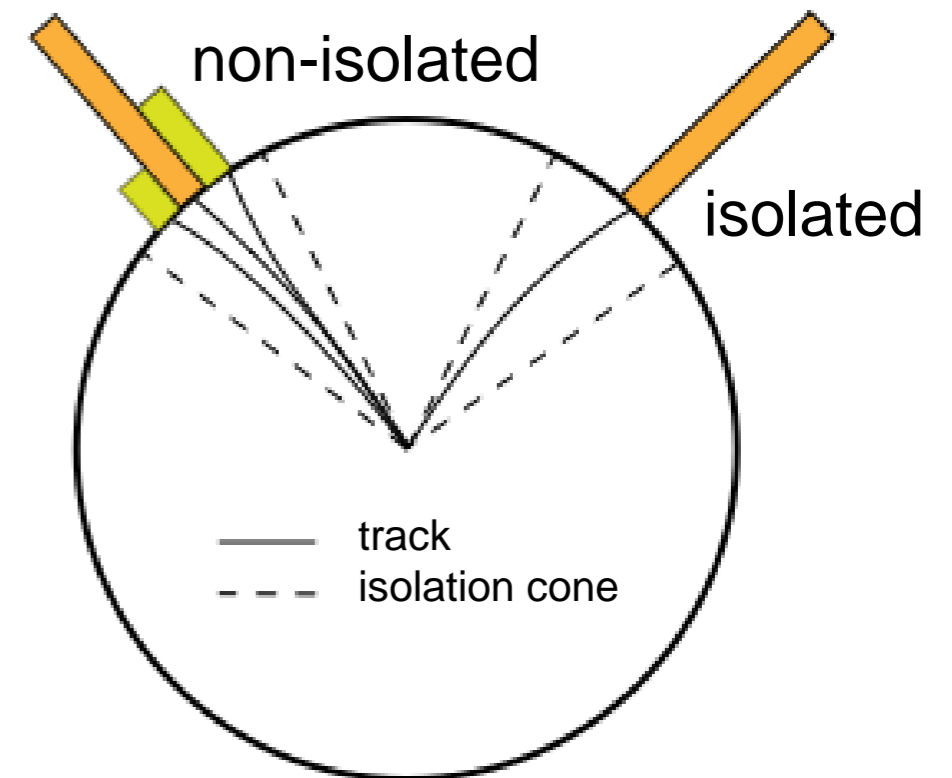
Cross section:  $e^+e^- \rightarrow W^+W^-$



[arXiv:1302.3415]

# W-Mass at Hadron-Colliders

- Start the reconstruction with **lepton**
  - **Isolated** leptons with high transverse momentum → suppress multijet background
  - **Prototype** for many high- $p_T$ -analyses at hadron-colliders
  - Additional hadronic activity → recoil against W

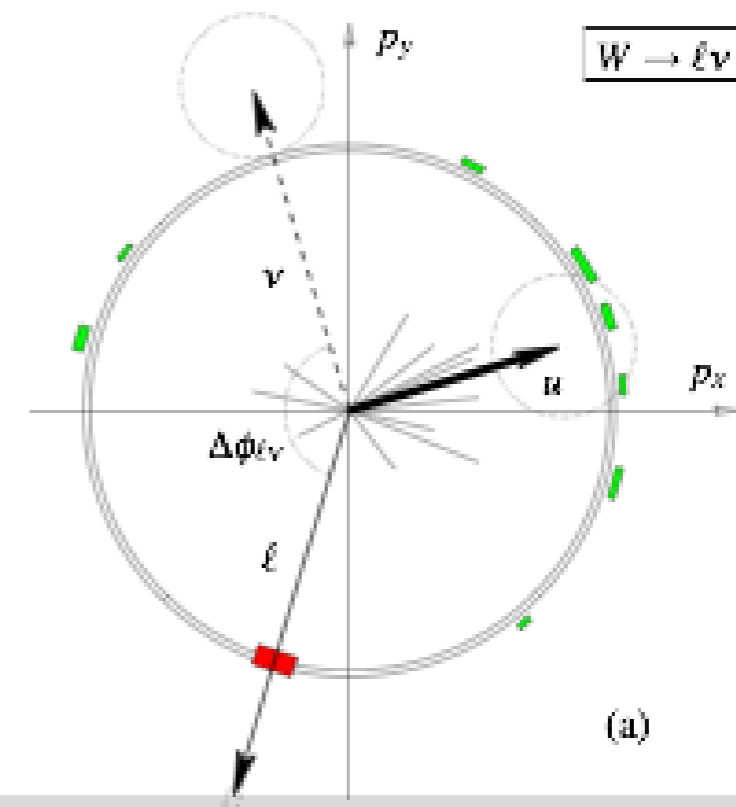


- Observable: **transverse mass**

$$m_T^2 = (E_T^\ell + E_T^\nu)^2 - (\vec{p}_T^\ell + \vec{p}_T^\nu)^2$$

$$\approx 2 |\vec{p}_T^\ell| |\vec{p}_T^\nu| (1 - \cos \Delta\phi_{\ell\nu})$$

- $p_T^\nu$  missing transverse energy in the event → assumed to represent neutrino



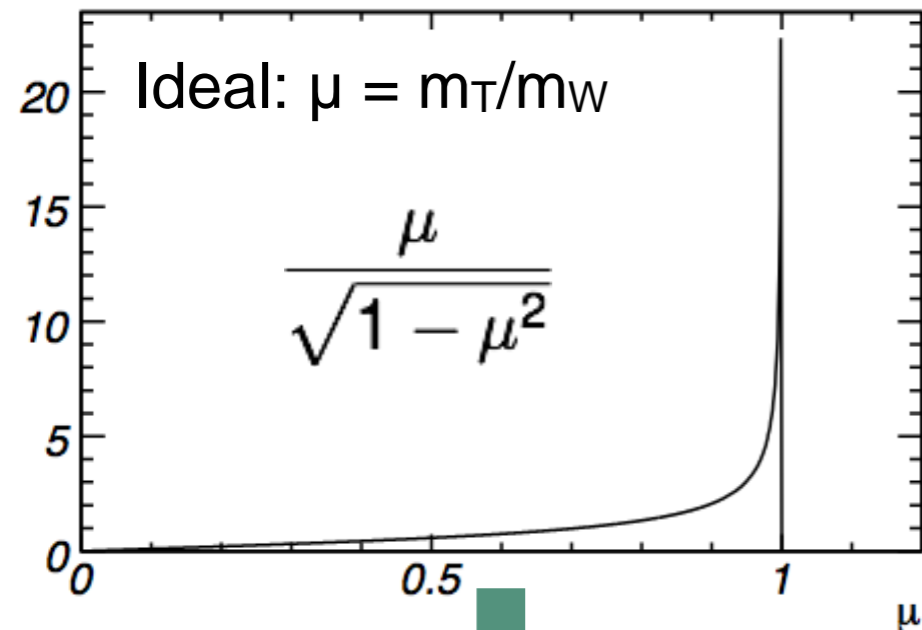
[CERN-OPEN-2008-020]

# W-Mass at Hadron-Colliders

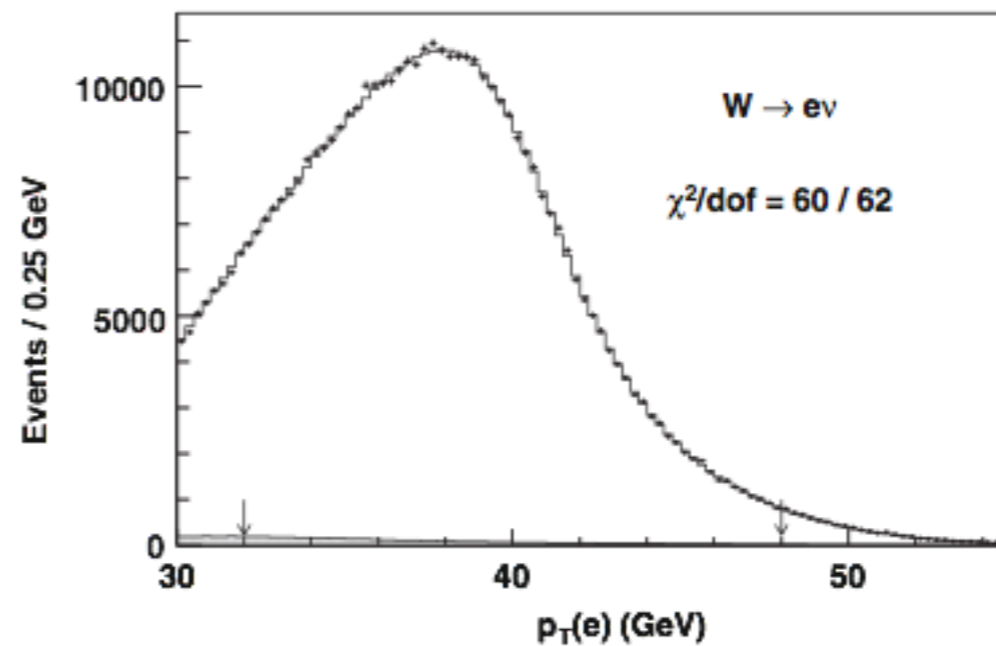
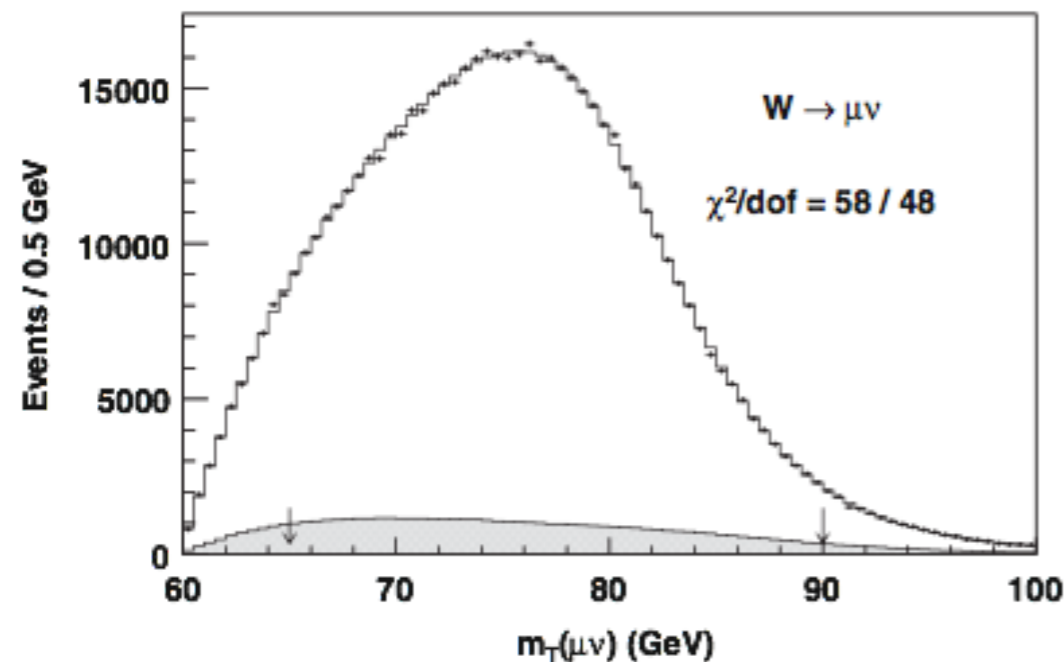
- Extraction of the W-boson Mass: differential cross sections as function of  $p_T^\nu$ ,  $p_T^\ell$ ,  $m_T$  (different systematic uncertainties)
- Look for edge/flank in the cross section:  
Jacobian edge
  - W-boson: created approximately at rest  $\rightarrow$  two-body decay
$$p_T^\ell = p_T^\nu = \frac{m_W}{2} \sin \theta, \quad \cos \Delta\phi_{\ell\nu} = -1 \quad \rightarrow m_T = m_W \sin \theta$$
  - $\mu := \frac{m_T}{m_W}$  :  $\frac{d\sigma}{d\mu} = \frac{d\sigma}{d\cos\theta} \cdot \left| \frac{d\cos\theta}{d\mu} \right| = \frac{d\sigma}{d\cos\theta} \cdot \left| \frac{d\sqrt{1-\mu^2}}{d\mu} \right| = \frac{d\sigma}{d\cos\theta} \cdot \left| \frac{-\mu}{\sqrt{1-\mu^2}} \right|$   
 $\rightarrow$  singular for  $\mu = 1$
  - Jacobi edge is smeared: finite W boson width ( $\Gamma_W \approx 2$  GeV)  
W boson not exactly at rest  
detector resolution effects



# W-Mass at Hadron-Colliders

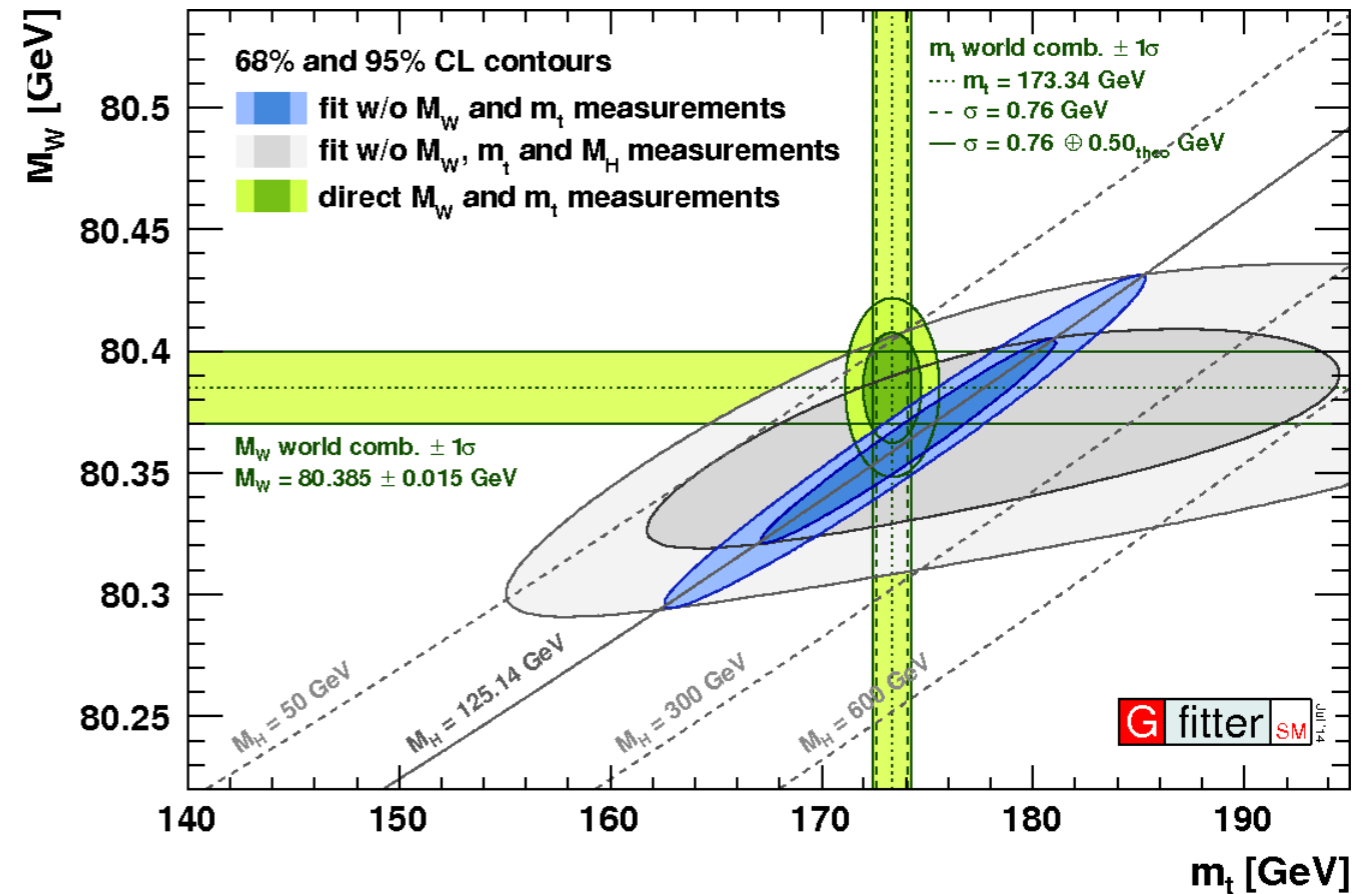
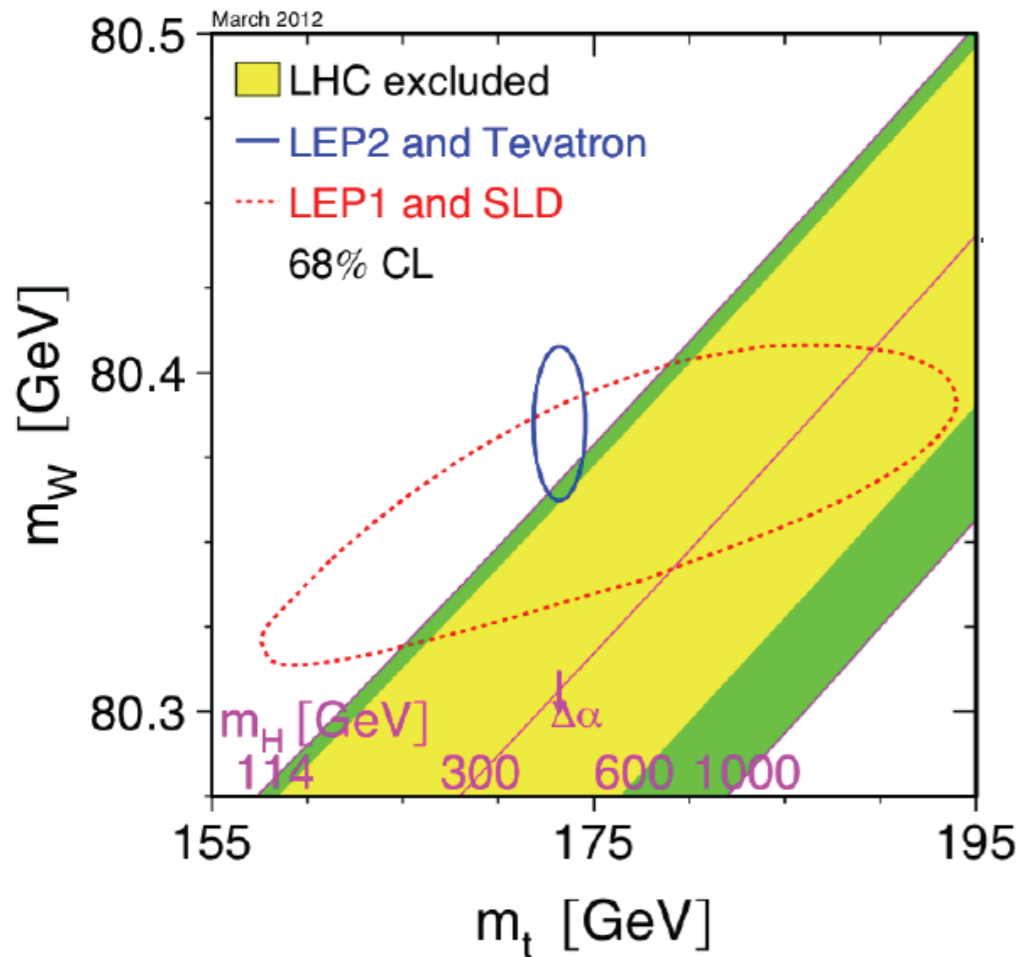


- Analysis: Likelihood-fit with **templates** from simulations with different W-masses
- Precision limited by **systematic uncertainties**: parton-densities, lepton energies, ...



[Phys. Rev. Lett. 108 (2012) 151803]

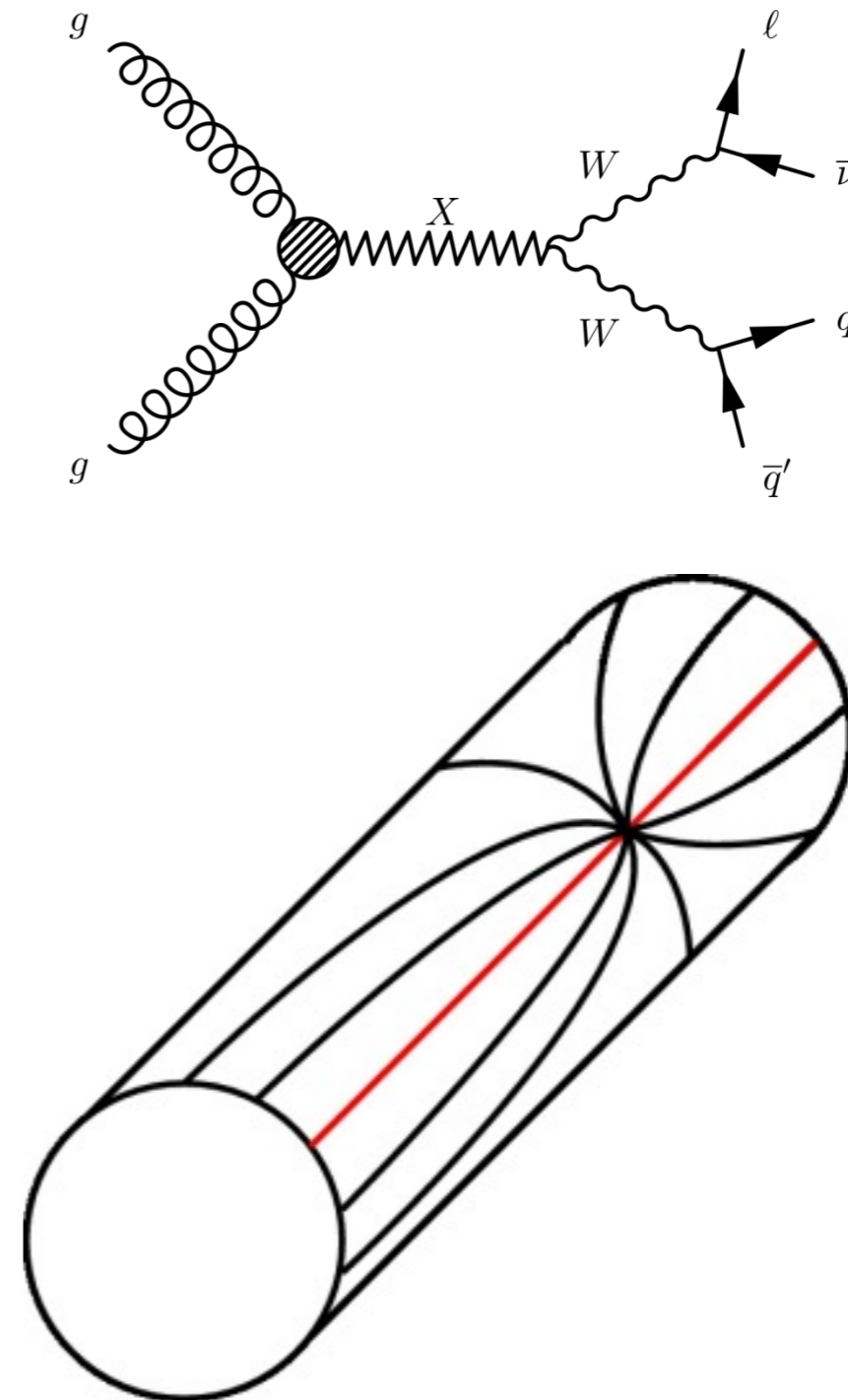
# Then and Now



- Pre-Higgs discovery: use  $M_W + M_{top}$  to constrain Higgs mass
- Post Higgs discovery: use  $M_W + M_{top} + M_H$  to constrain exotic theories that could add more particles to the loops  
→ very strong limits on supersymmetry

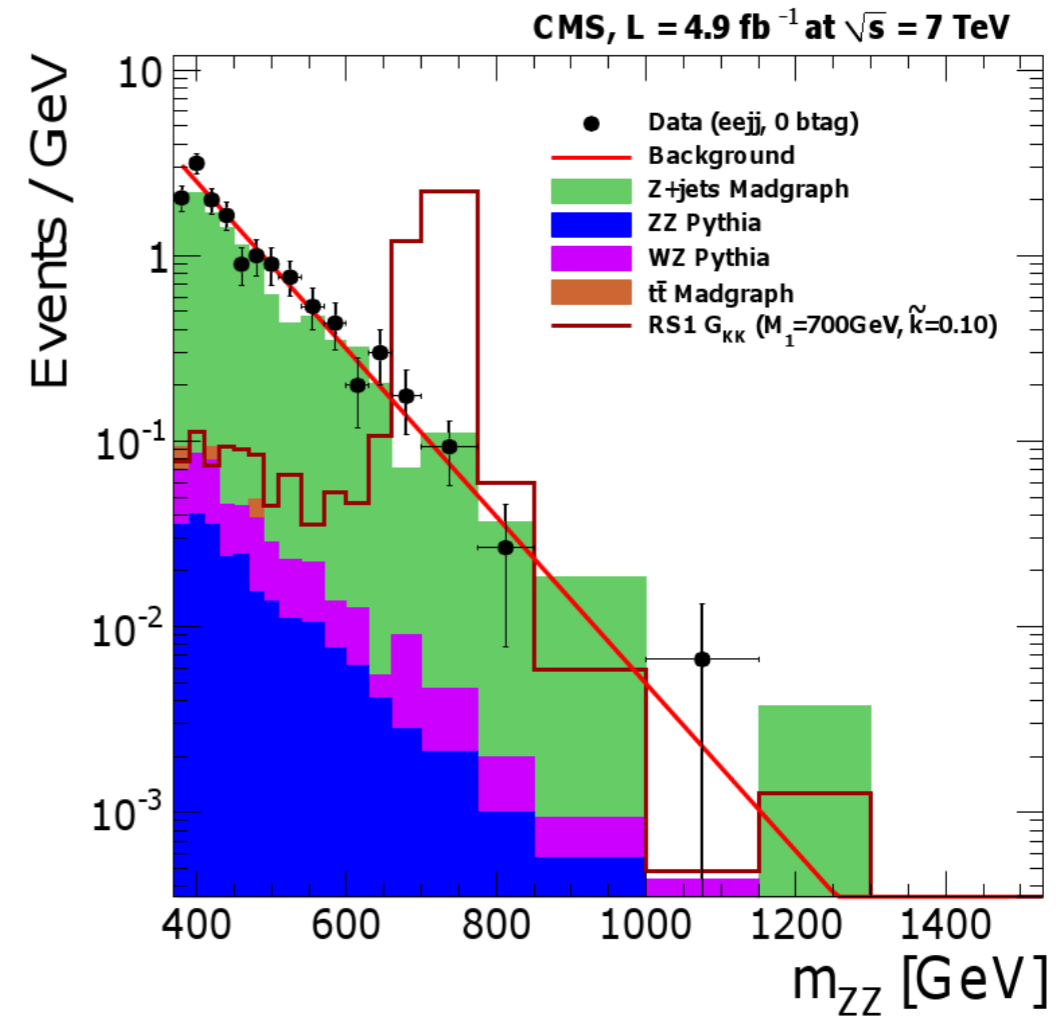
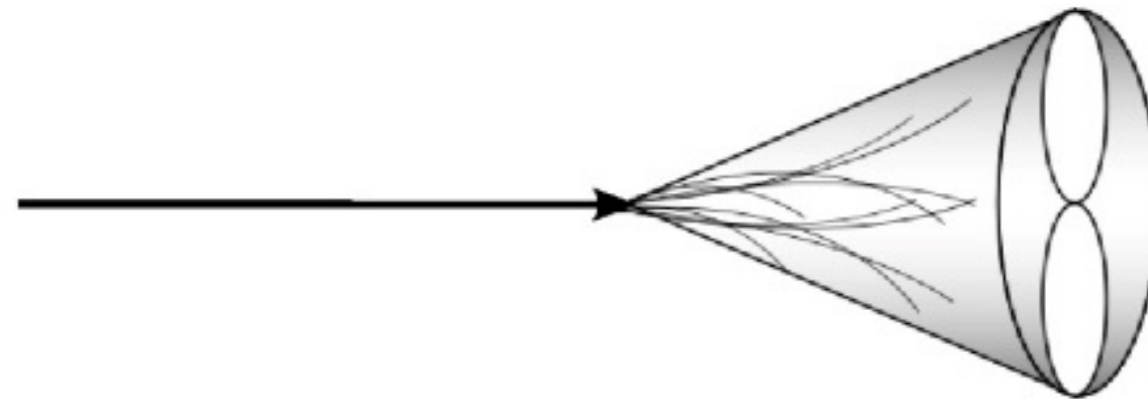
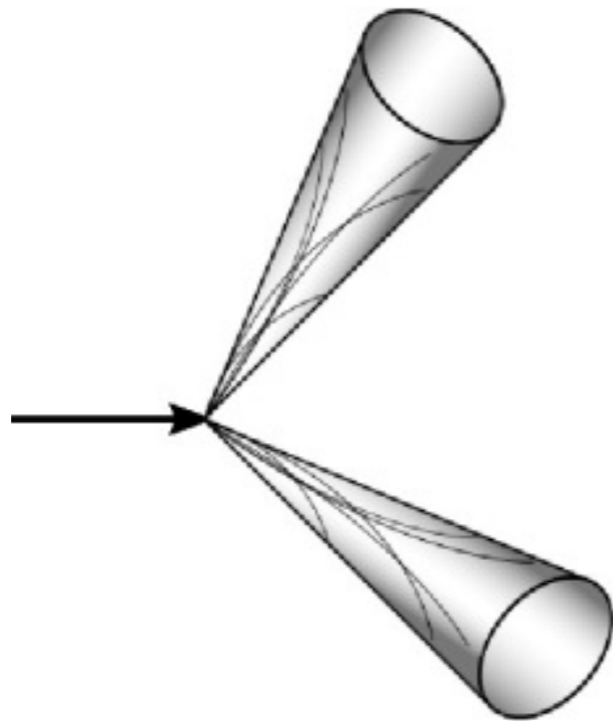
# Resonant Di-Boson Production

- Typical model: Graviton with extra-dimensionen
- would explain relatively weak gravitational force
- EWK + QCD confined to usual 3 dimensions
- Gravitation also propagates in extra-dimension(s)
- „curled up“ extra-dimension prohibits macroscopic effects



# Graviton Search

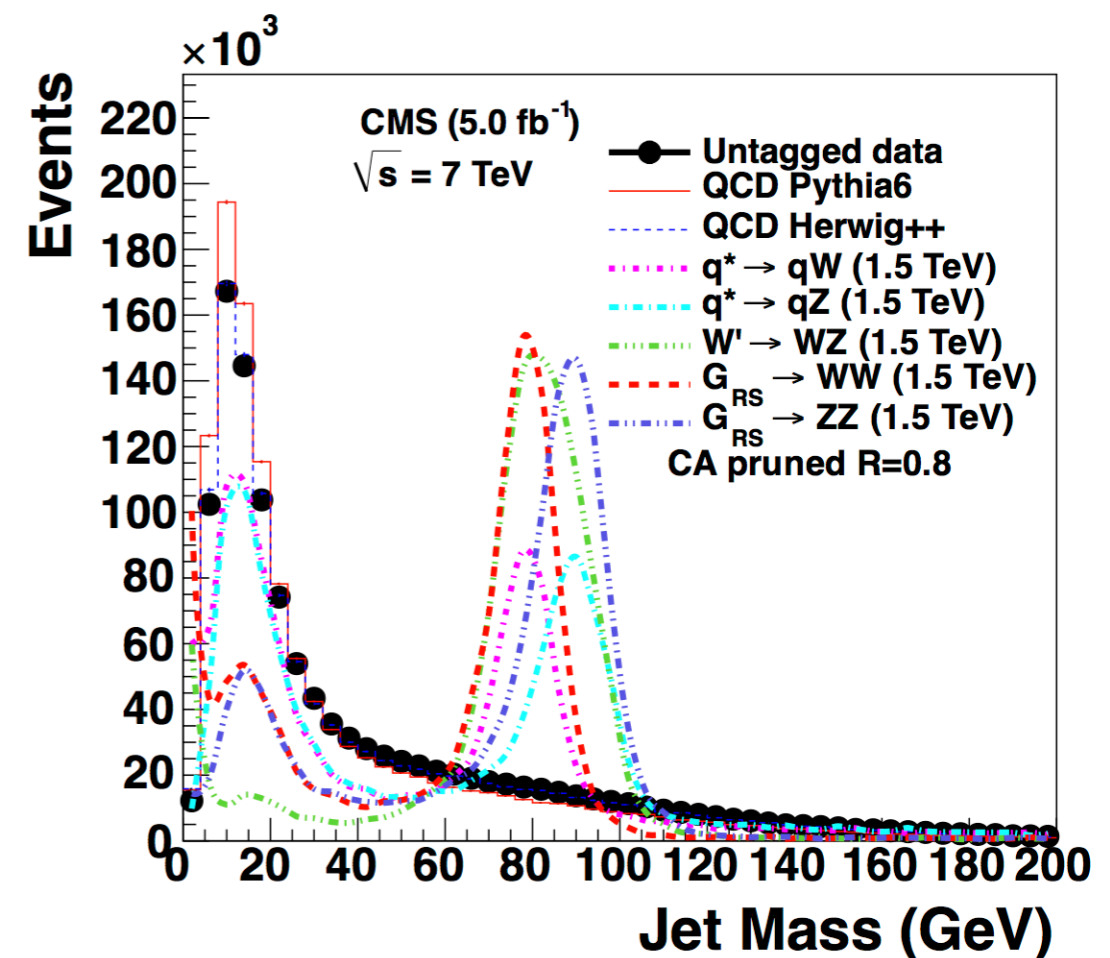
- Semi-leptonic Decay  
best compromise  
of purity/backgrounds  
and branching ratio
- „Merged Decays“ for high  
graviton masses



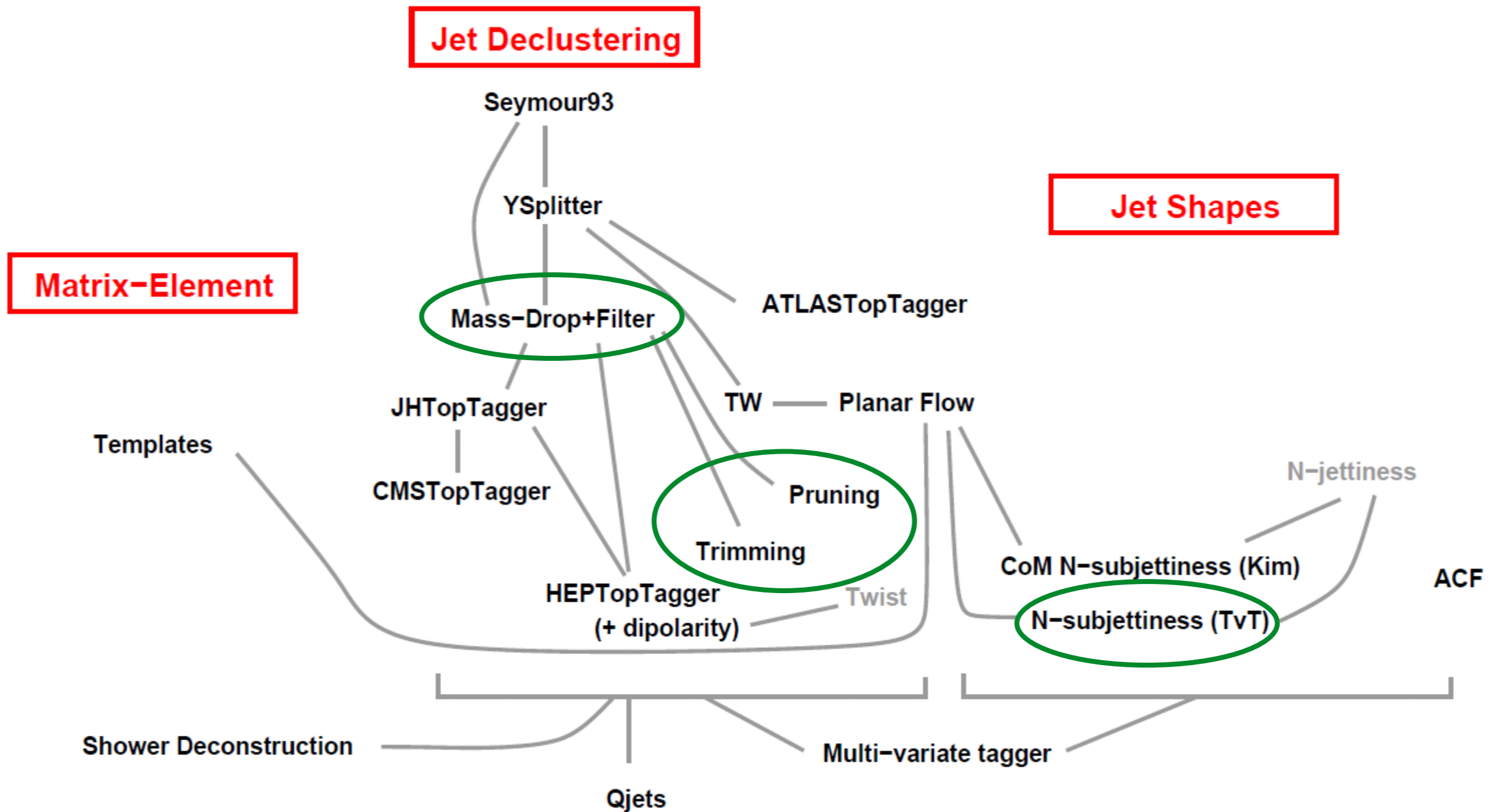
[10.1016/j.physletb.2012.11.063]

# V-tag

- Finding „fat jets“ compatible with W/Z decay  
=> jet mass  
=> jet substructure
- Jet mass:
  - sum of constituent four-vectors
  - falling steeply for quark/gluon jets (~ virtuality of outgoing particles)
  - peak at 83/91 GeV for W/Z
  - W/Z hard to separate



# Jet-Substruktur-Landscape



apologies for omitted taggers, arguable links, etc.



# Example: Massdrop + Filter

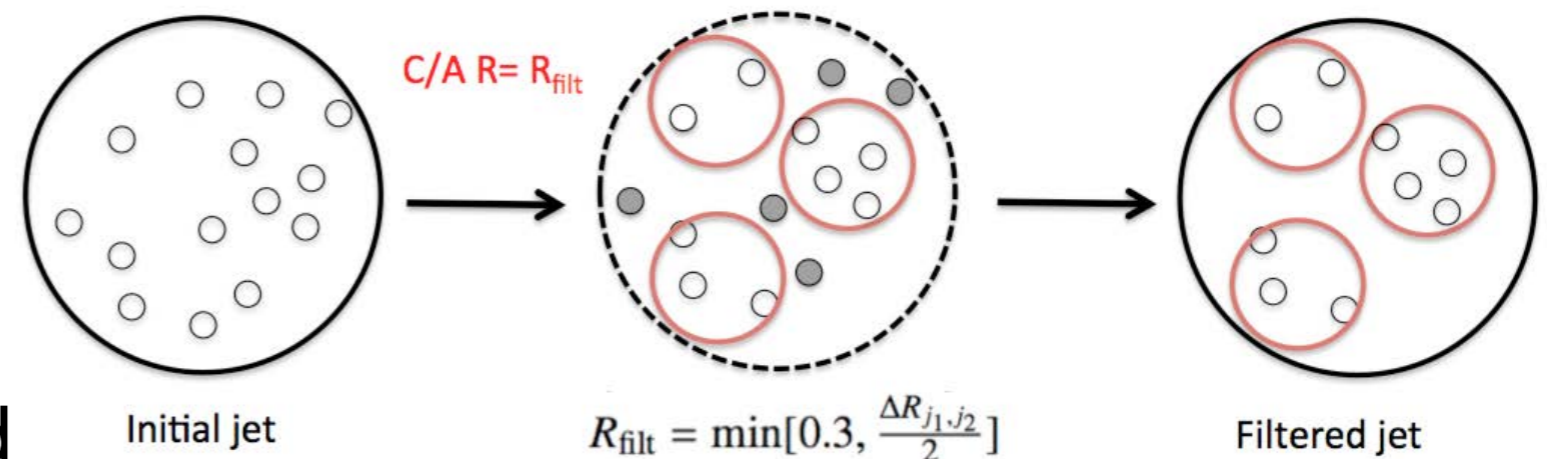
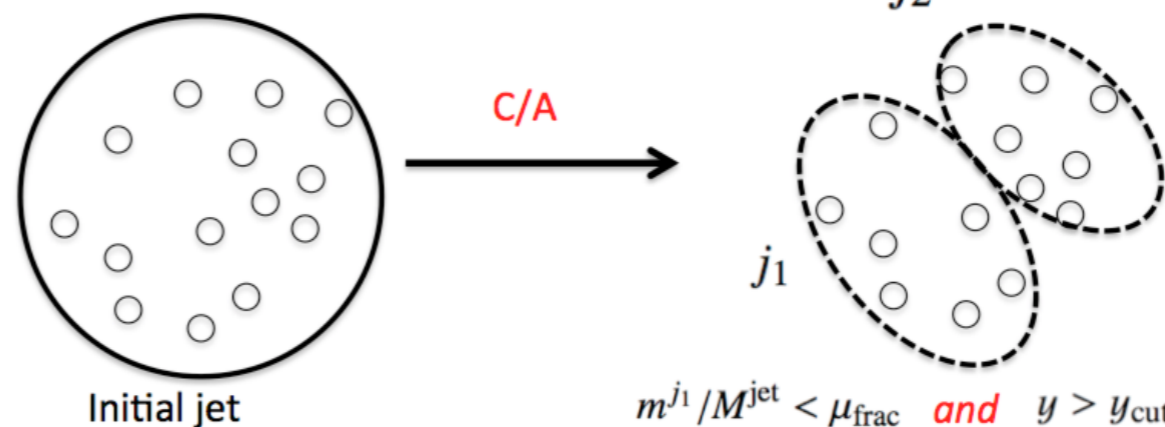
■ Start: **fat jet** from Cambridge-Aachen-Algorithmus

■ **Uncluster** jet into pair of subjets if significant **mass drop** occurs

→ candidate for jet with substructure

■ Re-clustering with smaller  $R$ , remove all particles not caught in hard subjets

$$d_{ij} = \frac{\Delta R_{ij}}{R}$$



<https://atlas.web.cern.ch/Atlas/GROUPS/PHYSICS/CONFNOTES/ATLAS-CONF-2012-065>

# Beispiel: N-Subjettiness

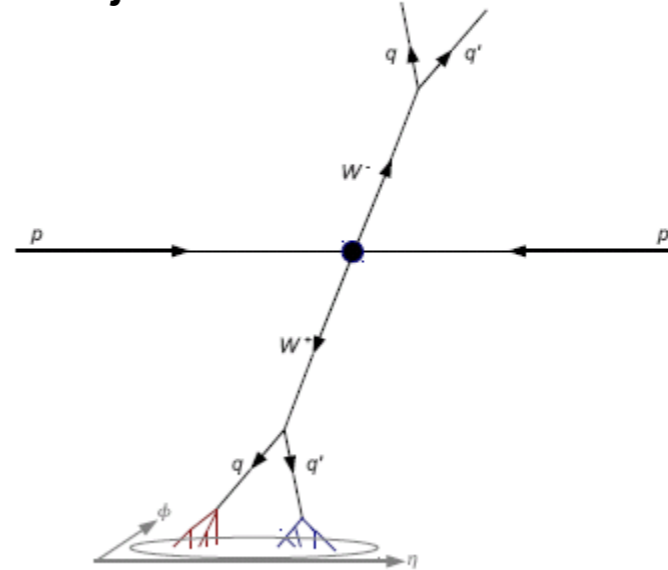
average distance to closest  
of N subjet axis

$$\tau_N = \frac{\sum_{i=1}^M p_{T,i} \min\{\Delta R_{i1}, \dots, \Delta R_{iN}\}}{\sum_{i=1}^M p_{T,i} R_0}$$

small if N real subjets exist  
large otherwise

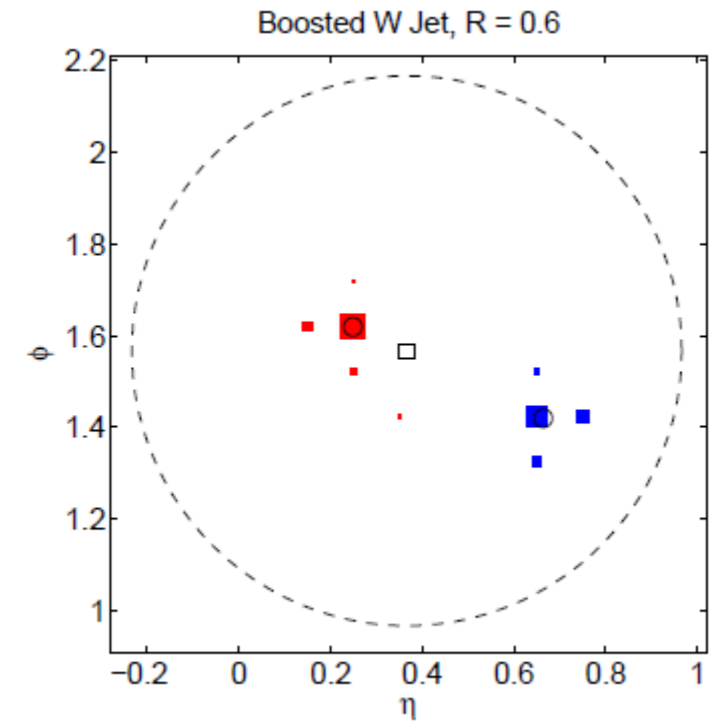
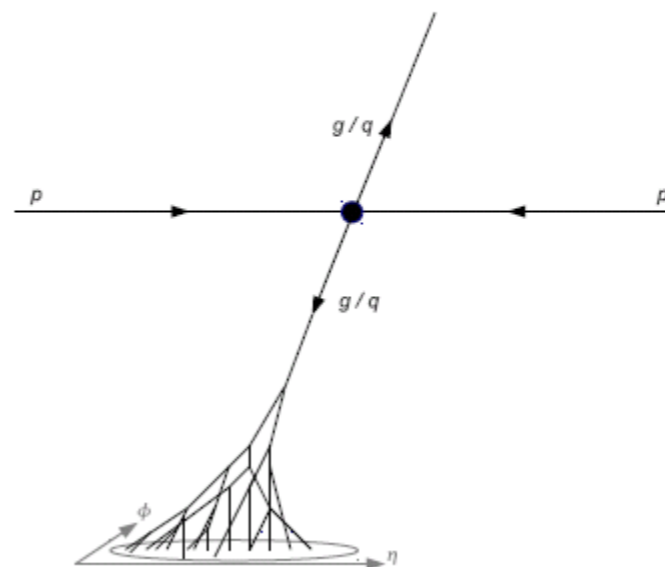
=> use ratio  $\tau_2/\tau_1$   
small for W/Z  
large for QCD

W: 2-jet structure

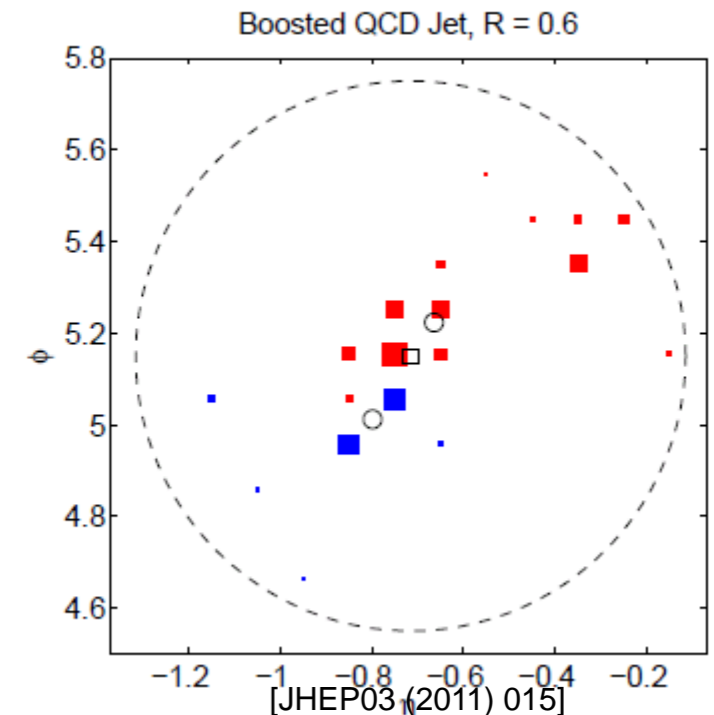


(a)

QCD: diffuse/round

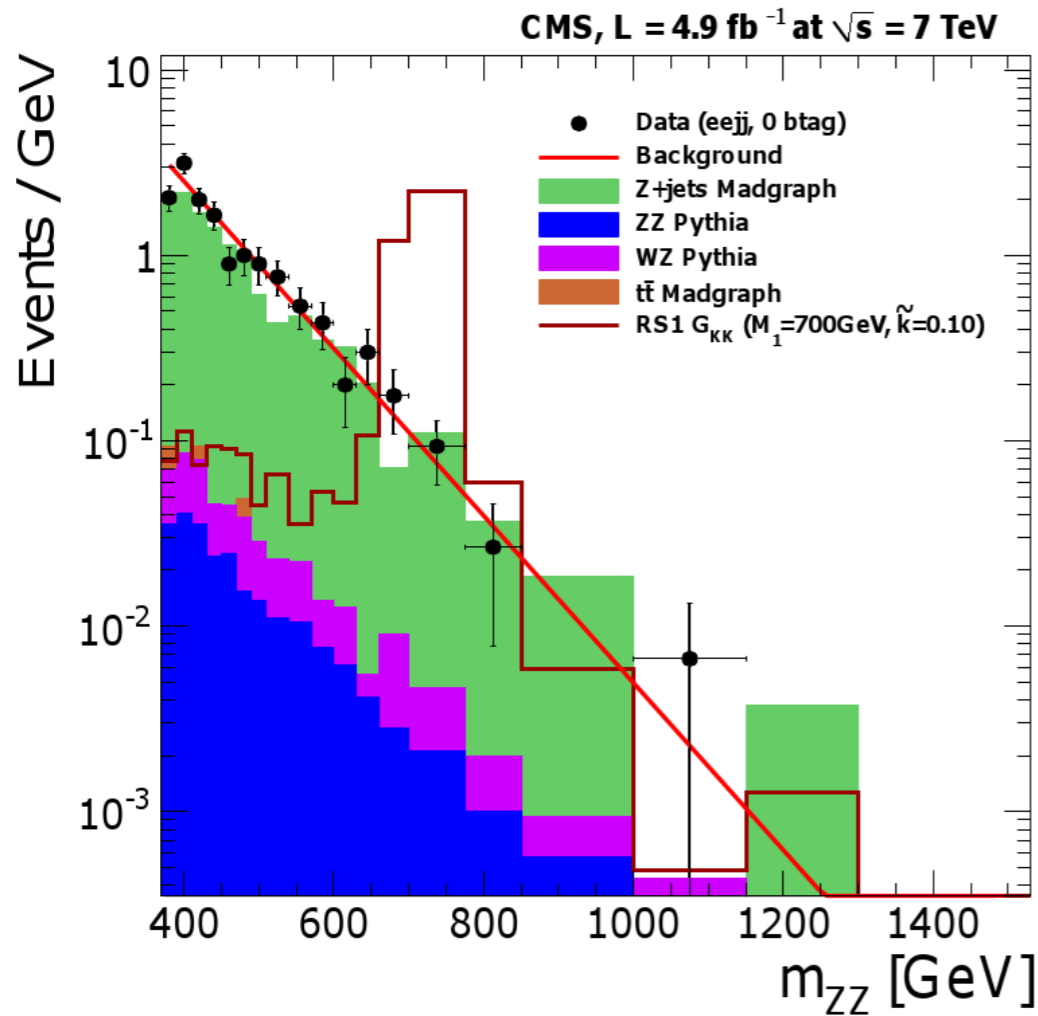


(b)

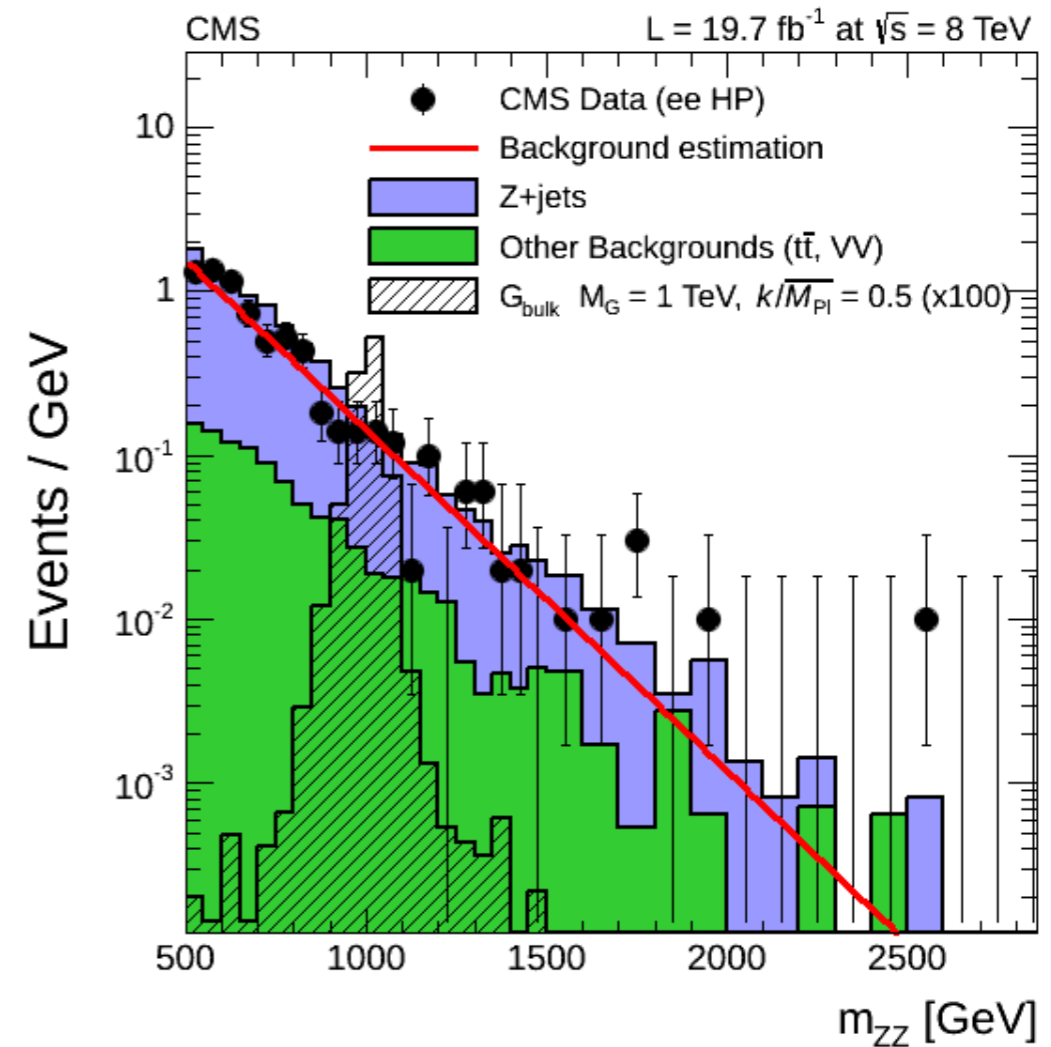




# Graviton with boosted W/Z





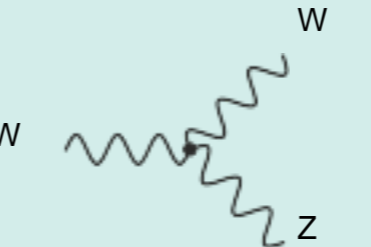


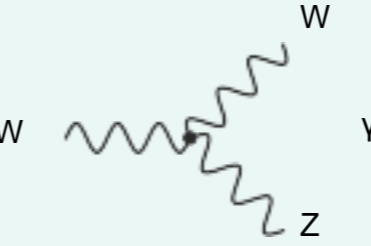
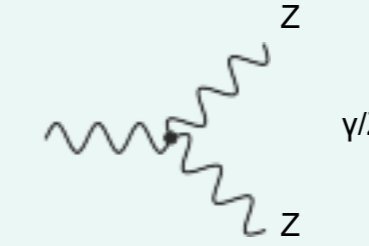
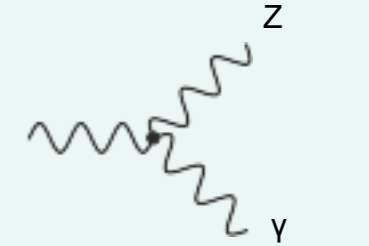
[10.1016/j.physletb.2012.11.063]



[10.1007/JHEP08(2014)174]

But: nothing found yet, looking again at 13TeV

# Anomalous TGC

	WW	W $\gamma$	WZ	ZZ	Z $\gamma$
SM					
aTGC					

- Modified **couplings** caused by physics beyond the SM:  
higher cross sections, especially at high **V-transverse-momentum**

# Anomalous TGC: Lagrange density

- Remember: SM only allows  $WW\gamma$  and  $WWZ$  triple boson vertices

$$\mathcal{L}_{WW\gamma} = -ie[A_\mu(W^{-\mu\nu}W_\nu^+ - W^{+\mu\nu}W_\nu^-) + F_{\mu\nu}W^{+\mu}W^{-\nu}]$$

$$\mathcal{L}_{WWZ} = -ie \cot\vartheta_w[Z_\mu(W^{-\mu\nu}W_\nu^+ - W^{+\mu\nu}W_\nu^-) + Z_{\mu\nu}W^{+\mu}W^{-\nu}]$$

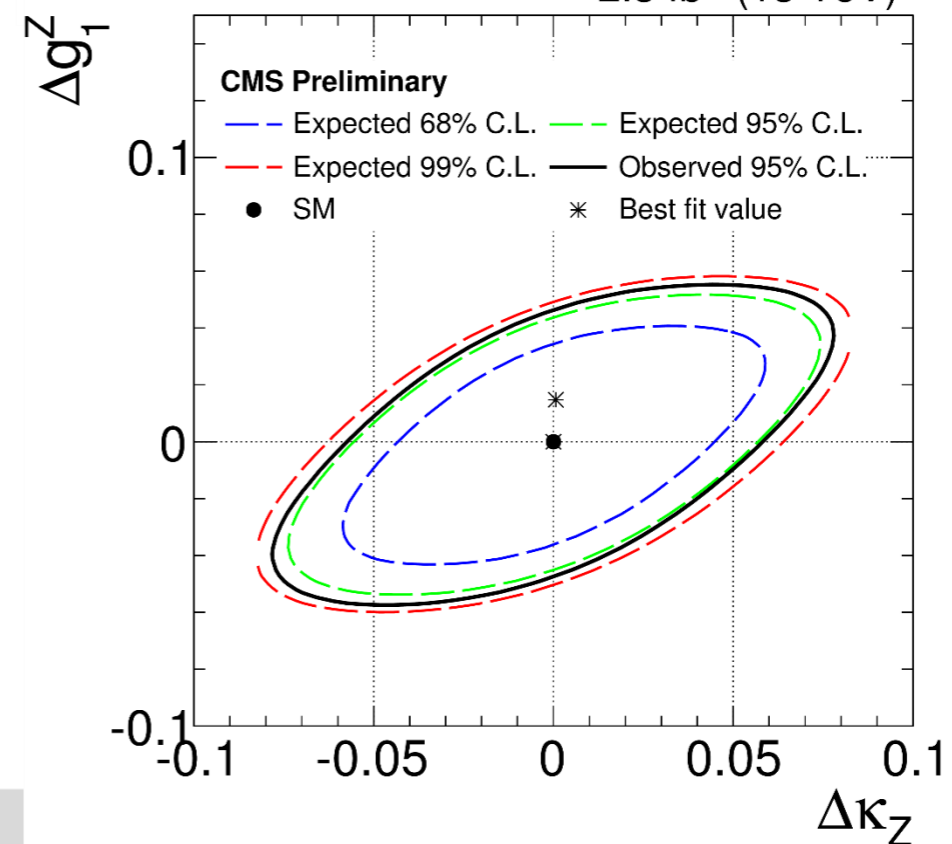
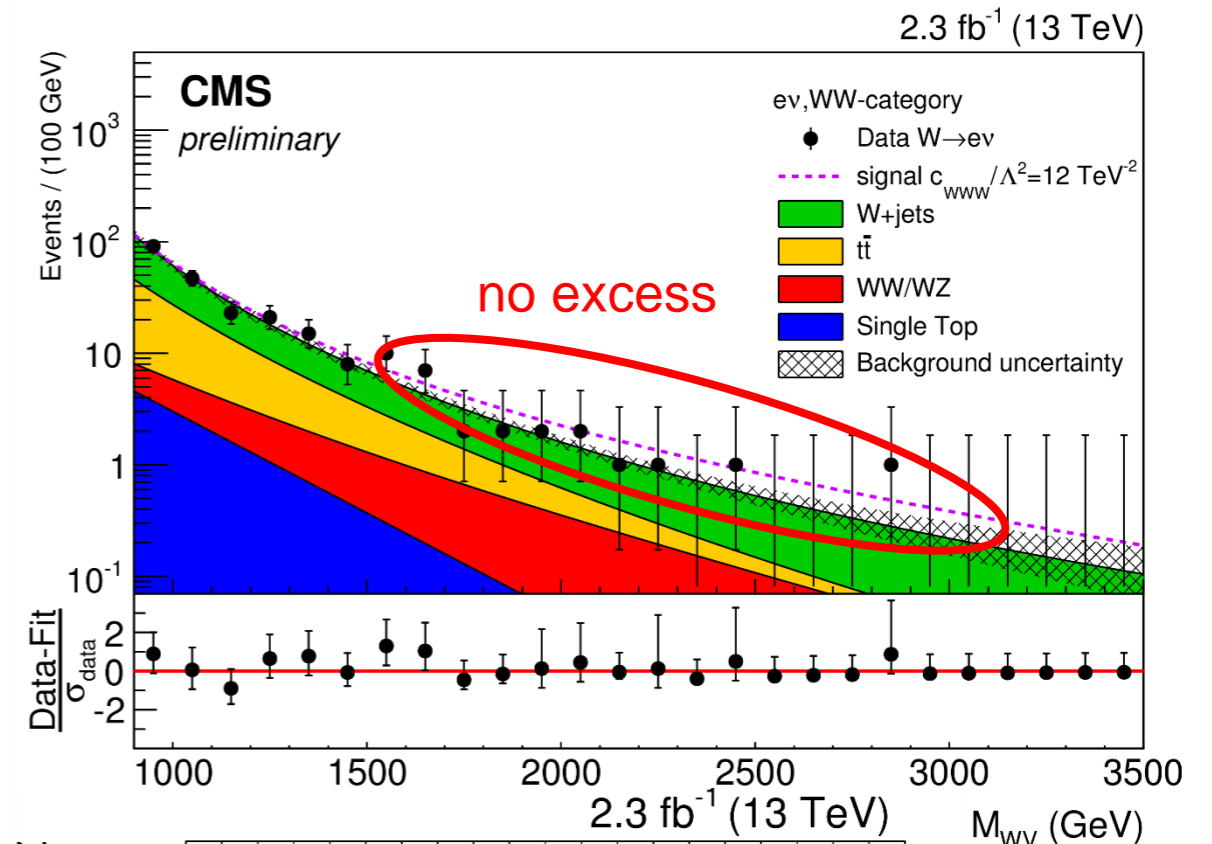
- Most general possible effective Lagrange density ( $V = \gamma, Z$ )

$$\begin{aligned} \mathcal{L}_{WWV}^{\text{eff}} = & -ig_{WWV} \left[ g_1^V V_\mu (W^{-\mu\nu}W_\nu^+ - W_{\mu\nu}^+ W_\nu^-) + \kappa_V V_{\mu\nu} W^{+\mu}W^{-\nu} \right. \\ & + \frac{\lambda_V}{m_W^2} V_{\mu\nu} W^{+\nu\rho}W_\rho^{-\mu} + ig_5^V \epsilon_{\mu\nu\rho\sigma} ((\partial^\rho W^{-\mu})W^{+\nu} - W^{-\mu}(\partial^\rho W^{+\nu})) V^\sigma \\ & \left. + ig_4^V W_\mu^- W_\nu^+ (\partial^\mu V^\nu + \partial^\nu V^\mu) - \frac{\tilde{\kappa}_V}{2} W_\mu^- W_\nu^+ \epsilon^{\mu\nu\rho\sigma} V_{\rho\sigma} - \frac{\tilde{\lambda}_V}{2m_W^2} W_{\rho\mu}^- W_\nu^{+\mu} \epsilon^{\nu\rho\alpha\beta} V_{\alpha\beta} \right] \end{aligned}$$

- SM:  $g_1^V = \kappa_V = 1$ , all other couplings vanish
- C- und P-Erhaltung:  $g_1^V, \kappa_V \neq 1, \lambda_V \neq 0, g_4^V = g_5^V = \tilde{\kappa}_V = \tilde{\lambda}_V = 0$

# Limits on aTGCs

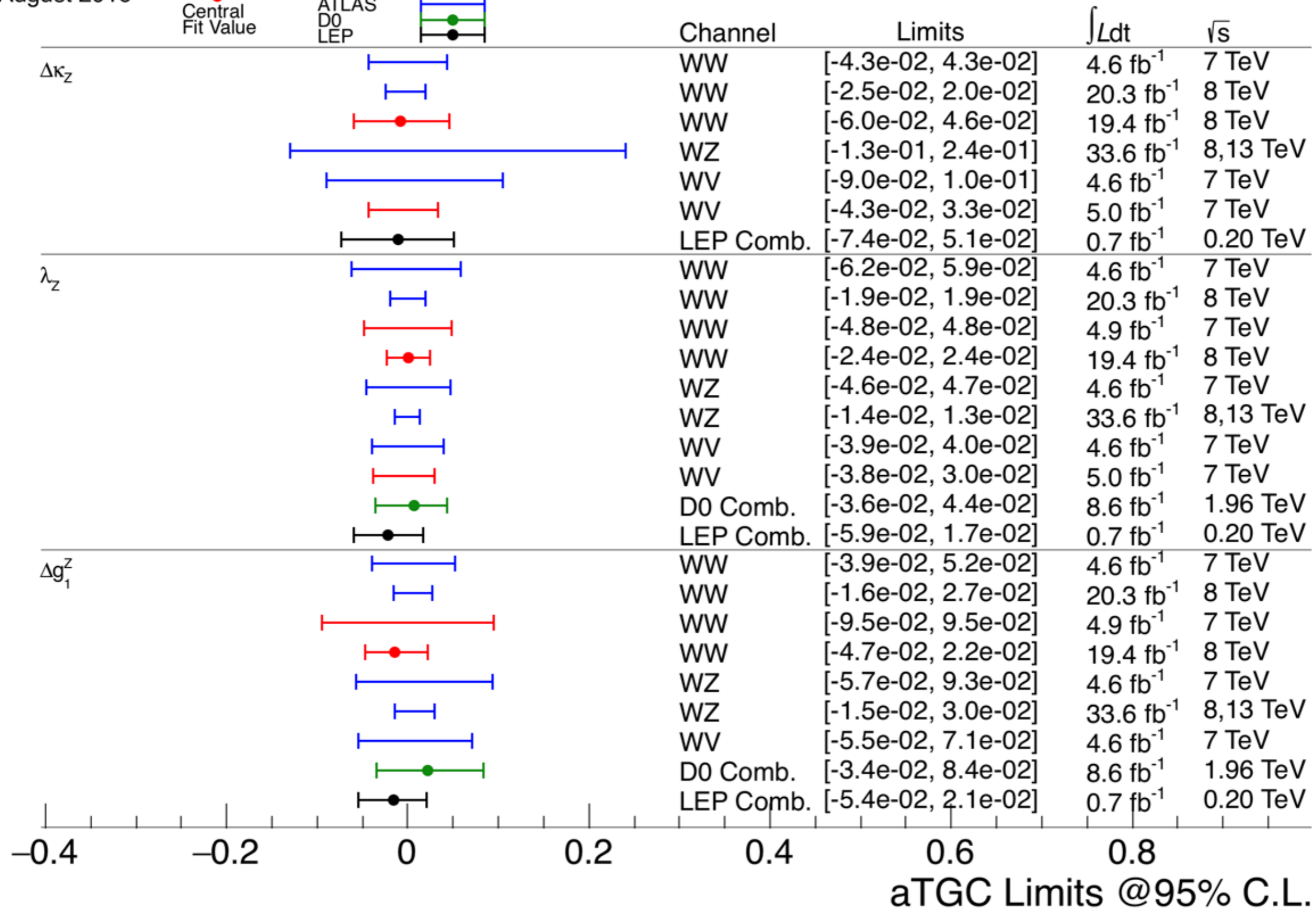
- Example:  
CMS W + W/Z semi-leptonic
- Isolated lepton + MET  
→ leptonic W candidate
- Fat jet with substructure  
→ hadronic W candidate
- Search for excess at high diboson invariant masses  
→ high aTGC contributions
- Extract limits from likelihood contours in signal+background fit



[CMS-PAS-SMP-16-012]

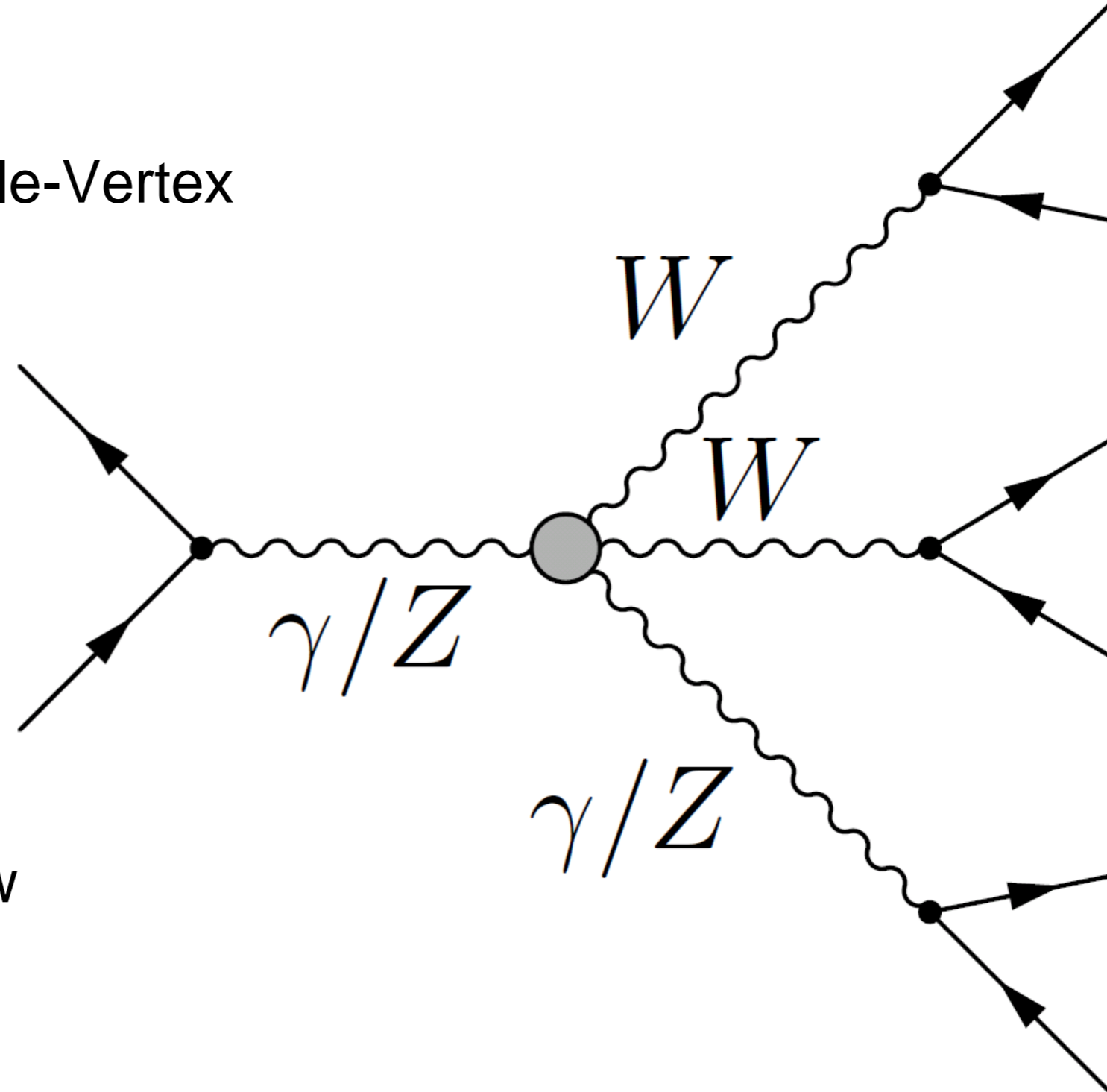
# aTGC limits

August 2016



# Triple Boson Production

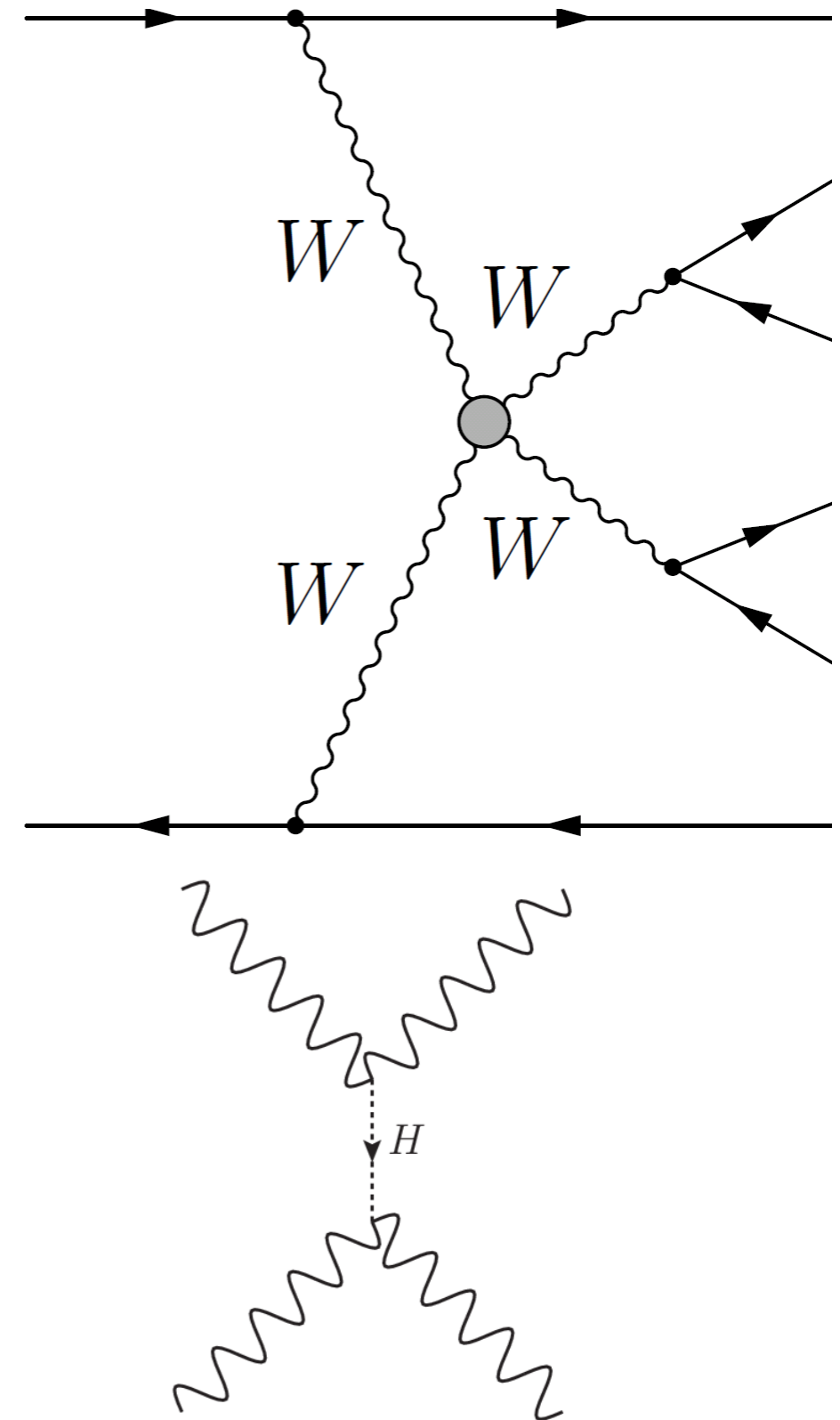
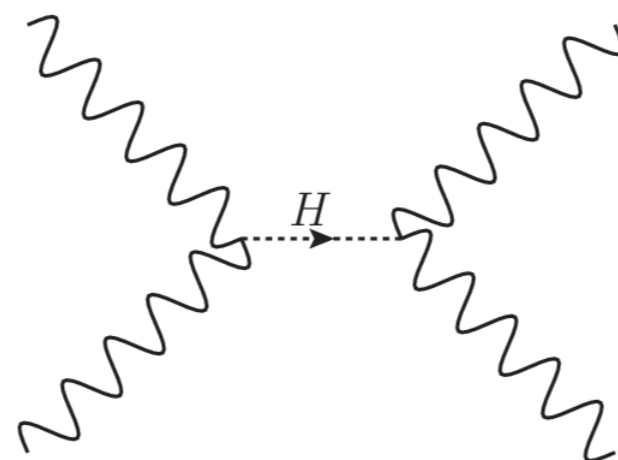
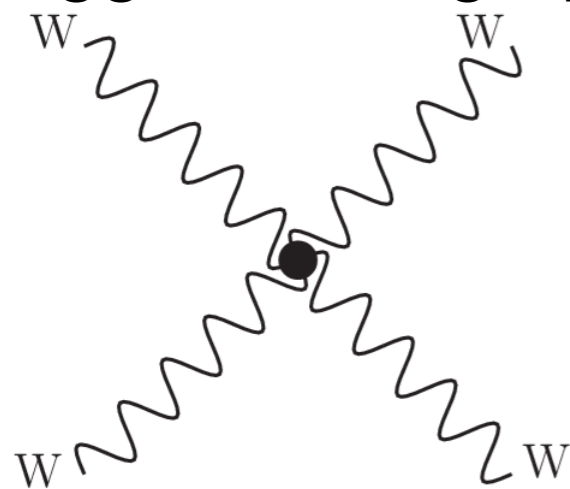
- Quartic Vertex similar to triple-Vertex
- SM:
  - $WWWW$
  - $W^+W^-ZZ$
  - $W^+W^-Z\gamma$
  - $W^+W^-\gamma\gamma$
  - 4x neutral forbidden
- Problem:  
cross sections extremely low





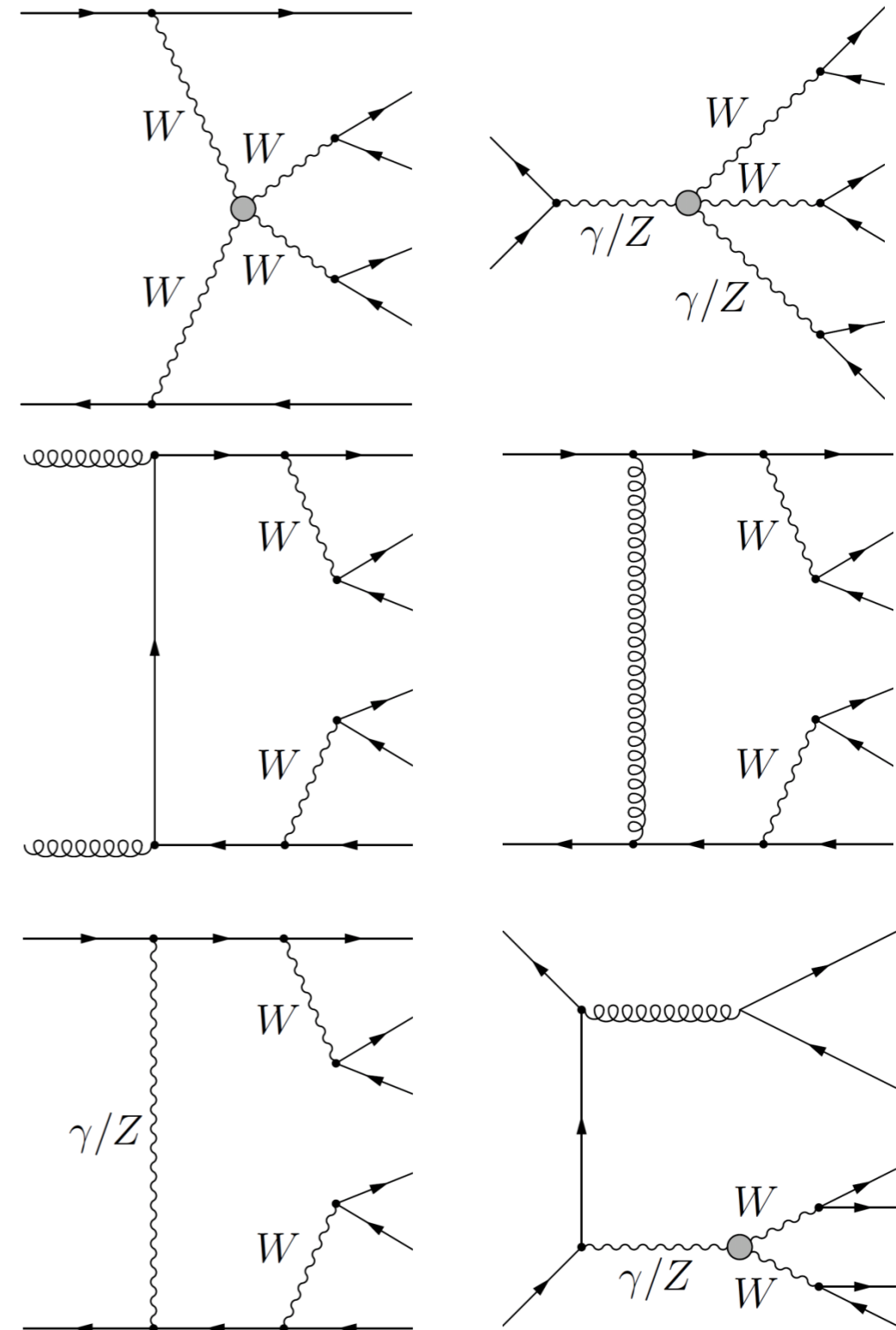
# Vector-Boson Scattering

- Study quartic vertex in vector boson scattering
- Similar to VBF process in Higgs boson physics
- Scattering cross section with longitudinally polarized bosons not unitary at high energies
- Regularised in SM by interference with Higgs boson graphs



# Vector-Boson Scattering

- Detailed test of the Higgs mechanism
- $2W + 2\text{jet}$  processes „common“ even without quartic vertex
- Enhance VBS with suitable selections:
  - jets with high dijet-mass
  - large difference in rapidity
- Only look at  $W^{+/-}W^{+/-}$   
 => no gluons in the initial state





# Quartic Couplings

- Measurement in  $pp \rightarrow W^+W^+jj$
- Limits on anomalous couplings

[Atlas-CONF-2014-013]

