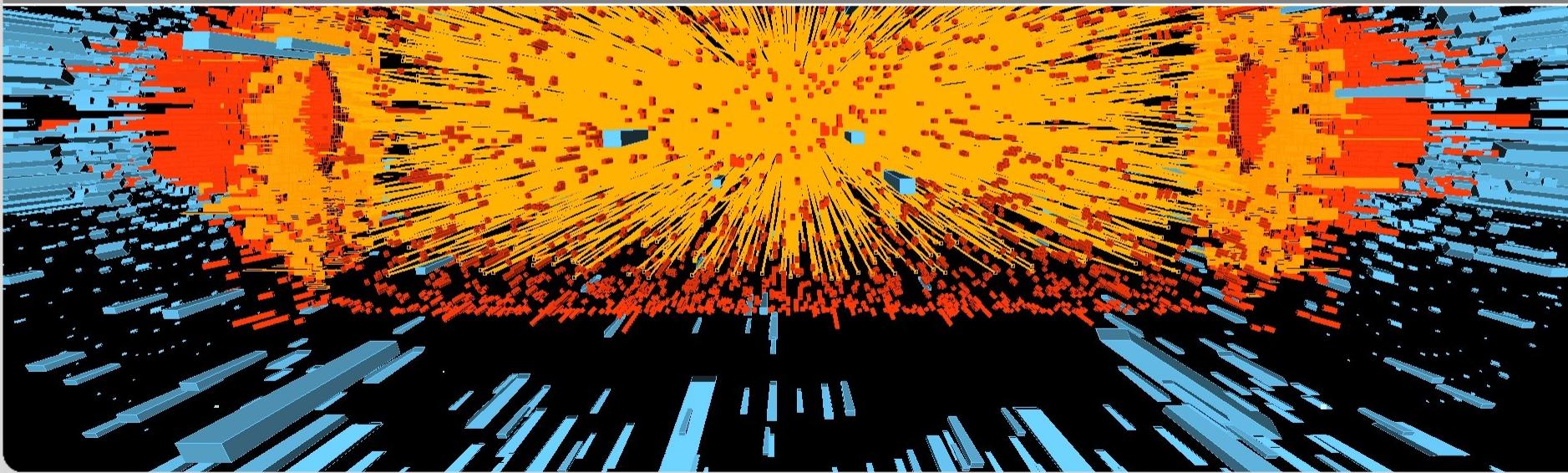


MSSM $\phi \rightarrow \tau\tau$

Patrick Kirchgaeßner
07. Januar 2016

INSTITUTE OF EXPERIMENTAL PARTICLE PHYSICS (IEKP) – PHYSICS FACULTY



Agenda

Standardmodel

- Gauge theories
- Higgs mechanism
- Yukawa coupling

Higgs discovery

Higgs searches $\phi \rightarrow \tau\tau$

- Model independent
- Model dependent (MSSM)

Extensions of the SM

- SUSY
- MSSM

Recap – The Standardmodel

- QED Lagrangian and Gauge Invariance

$$L_{Dirac} = \bar{\Psi} (i\gamma^\mu \partial_\mu - m) \Psi$$

Invariant under global U(1) transformation

$$L \rightarrow L' = L \quad \checkmark$$

$$\Psi \rightarrow \Psi' = \exp(i\Theta)\Psi$$

$$\bar{\Psi} \rightarrow \bar{\Psi}' = \bar{\Psi} \exp(-i\Theta)$$

Demand invariance under local U(1) transformation!

$$\partial_\mu \rightarrow D_\mu = \partial_\mu + iqA_\mu$$

$$A_\mu \rightarrow A'_\mu = A_\mu - \frac{1}{q}\partial_\mu\Theta(x)$$

$$\Psi \rightarrow \Psi' = \exp(i\Theta(\textcolor{red}{x}))\Psi$$

$$\bar{\Psi} \rightarrow \bar{\Psi}' = \bar{\Psi} \exp(-i\Theta(\textcolor{red}{x}))$$

$$L_{QED} = \bar{\Psi}(i\gamma^\mu D_\mu - m)\Psi = \bar{\Psi}(i\gamma^\mu \partial_\mu)\Psi - m\bar{\Psi}\Psi - q(\bar{\Psi}\gamma^\mu\Psi)A_\mu + \frac{1}{4}F_{\mu\nu}F^{\mu\nu}$$

$$L \rightarrow L' = L \quad \checkmark$$

Full QED lagrangian

Recap – The Standardmodel

The demand of gauge invariance under local $U(1)$ transformation gives rise to the covariant derivative D_μ and a new field A_μ which works as a massless messenger particle between different points in spacetime.

Massless?

- Terms like $m^2 A_\mu A^\mu$ are not gauge invariant
 - Euler-Lagrange equation for A_μ leads to massless Klein-Gordon equation
$$(\partial_\mu \partial^\mu) A_\mu = 0$$
- Gauge field is a boson with zero mass

Recap – The Standardmodel

SpecialUnitary

- U(1) use same procedure to **non-abelian** Lie groups SU(N) (**generators of the group don't commute**)
- SM : $SU(3)_C \times SU(2)_L \times U(1)_Y$
- $SU(3)$: QCD
 - 8 massless gluons
 - No need for spontaneous symmetry breaking
- $SU(2) \times U(1)$: Electroweak sector
 - Parity violation (weak force couples only to lh particles and rh antiparticles)
 - Mass terms of the form $m^2 \bar{\Psi} \Psi / m^2 W^\mu W_\mu$ not invariant under symmetry transformations (lh and rh fields transform differently)

$$G \in SU(N)$$

$$G_{fin} = (I + i \frac{\vartheta_{fin}^a}{m} T^a)^m \xrightarrow{m \rightarrow \infty} e^{i \vartheta^a T^a}$$

ϑ^a Continuous parameter

T^a Generator of the group

$(N^2 - 1)$ Generators

Solution → Yukawa Coupling

Solution → Higgs Mechanism

Higgs Mechanism

- Spontaneous symmetry breaking + local Gauge theory
 - Groundstate has less symmetries than the corresponding e.o.m
 - Breaking of global symmetries → Goldstone theorem

There is one massless scalar particle (goldstone boson) for every spontaneously broken symmetry

Higgs Mechanism

- e.g. Lagrangian for complex scalar field (global U(1) symmetry)

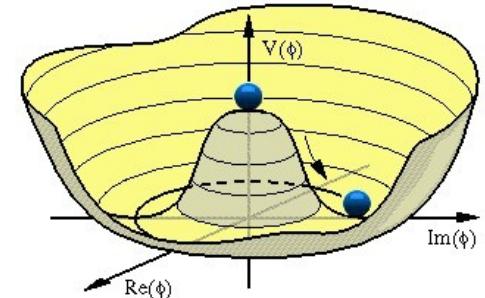
$$L = (\partial_\mu \Phi)^* (\partial^\mu \Phi) - \mu^2 \Phi^* \Phi - \lambda (\Phi^* \Phi)^2$$

- Groundstate for $\mu^2 < 0 \rightarrow \Phi^* \Phi = -\frac{\mu^2}{2\lambda}$

- Expand around minima $|\Phi| = \sqrt{-\frac{\mu^2}{2\lambda}} = v$

$$\Phi = v + \frac{1}{\sqrt{2}}(\phi_1 + i\phi_2)$$

$$\rightarrow L = \frac{1}{2}(\partial_\mu \phi_1)^2 + \frac{1}{2}(\partial_\mu \phi_2)^2 - 2\lambda v^2 \phi_1^2 - \sqrt{2}v\lambda\phi_1(\phi_1^2 + \phi_2^2) - \frac{\lambda}{4}(\phi_1^2 + \phi_2^2)^2$$



Interaction terms: $\phi^4 \quad \phi^3$

Massterms: $m_{\phi_1} = 2v\sqrt{\lambda}$ $m_{\phi_2} = 0$ (Goldstone Boson)

Higgs mechanism for U(1) gauge theory

$$L = (D_\mu \phi)^* (D^\mu \phi) - \mu^2 \phi^* \phi - \lambda (\phi^* \phi)^2 - \frac{1}{4} F_{\mu\nu} F^{\mu\nu}$$

- Spontaneous symmetry breaking: expand ϕ around $v = \sqrt{-\frac{\mu^2}{2\lambda}}$

$$\phi(x) = v + \frac{1}{\sqrt{2}}(\varphi_1 + i\varphi_2) = \left(v + \frac{H(x)}{\sqrt{2}}\right) \exp\left(i\frac{\chi(x)}{\sqrt{2}v}\right)$$

- Kinetic term changes to

$$|D_\mu \phi|^2 = \frac{1}{2} \partial_\mu H \partial^\mu H + e^2 v^2 A'_\mu A^{\mu'} \left(1 + \frac{H}{v\sqrt{2}}\right)^2 \quad \text{with} \quad A'_\mu = A_\mu + \frac{\partial_\mu \chi}{\sqrt{2}ve}$$

- Which leads to the lagrangian

$$L = \frac{1}{2}(\partial_\mu H)(\partial^\mu H) - 2\lambda v^2 H^2 - \lambda \sqrt{2}v H^3 - \frac{\lambda}{v} H^4 - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} + e^2 v^2 A'_\mu A^{\mu'} + e^2 A'_\mu A^{\mu'} \left(\sqrt{2}vH + \frac{H^2}{2}\right)$$

Massive scalar particle (Higgs)

Massive gauge boson
In this case a massive photon

Higgs Mechanism

- Spontaneous symmetry breaking + local Gauge theory
 - Groundstate has less symmetries than the corresponding e.o.m
 - Breaking of global symmetries → Goldstone theorem
 - No Goldstone bosons but one more d.o.f (longitudinal polarization) for the gauge fields
 - In $SU(2)\times U(1)$ gauge theory W and Z gauge bosons acquire mass
 - Photon stays massless
- This shuffling of d.o.f is the Higgs mechanism

Yukawa coupling

- $m\bar{\Psi}\Psi$ not gauge invariant under $SU(2)_L \times U(1)_Y$ (different charges)

$$m\bar{\Psi}\Psi = m(\bar{\Psi}_L\Psi_R + \bar{\Psi}_R\Psi_L)$$
- Idea is to write interaction between Ψ_L , Ψ_R and ϕ (for simple down type electron case)

$$L_Y = g \left(\overbrace{\bar{\Psi}_L \phi}^{\text{U(1)}_Y \text{ invariant}} e_R + h.c \right)$$

SU(2)_L invariant

Singlet under SU(2)_L

Charges w.r.t $U(1)_Y$

$$Y_R = -2$$

$$Y_\phi = 1$$

$$Y_L = -1$$

- L_Y invariant under $SU(2)_L \times U(1)_Y$
- May become a mass term after ssb

$$\phi = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix}$$

Lorentz invariant
Gauge invariant
Renormalizable
Dimension 4



Yukawa coupling

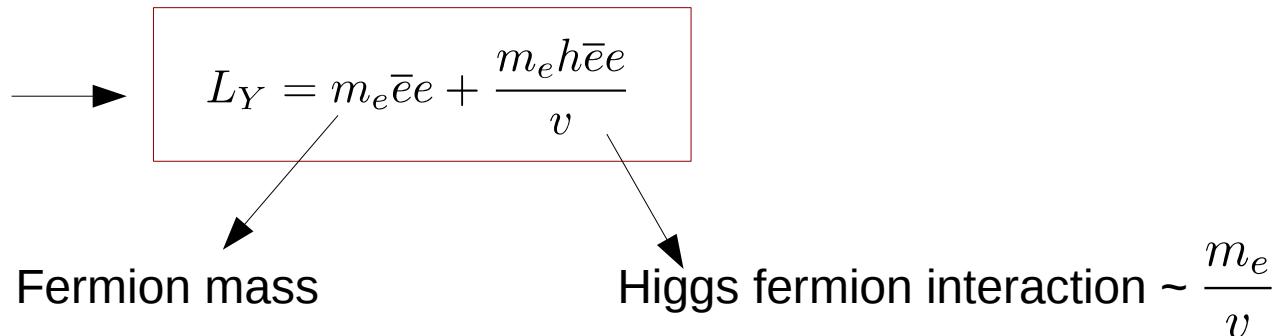
$$\phi = \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} \Rightarrow$$

$$L_Y = g[(\bar{\nu}_L \bar{e}_L) \begin{pmatrix} 0 \\ \frac{v+h}{\sqrt{2}} \end{pmatrix} e_R + h.c] = g(\bar{e}_L \cdot e_R + h.c) \frac{v+h}{\sqrt{2}}$$

$$= \frac{gv}{\sqrt{2}}(\bar{e}_L e_R + \bar{e}_R e_L) + \frac{gh}{\sqrt{2}}(\bar{e}_L e_R + \bar{e}_R e_L)$$

$$= m_e(\bar{e}_L e_R + \bar{e}_R e_L) + \frac{m_e}{v}h(\bar{e}_L e_R + \bar{e}_R e_L)$$

→
$$L_Y = m_e \bar{e} e + \frac{m_e h \bar{e} e}{v}$$



Fermion mass Higgs fermion interaction $\sim \frac{m_e}{v}$

- Quark masses: same procedure but need Higgs doublet with $Y=-1$ for down type quarks ϕ^\dagger (later)

SM Lagrangian

$$L_{SM} = L_F + L_{gauge} + L_\phi + L_Y$$

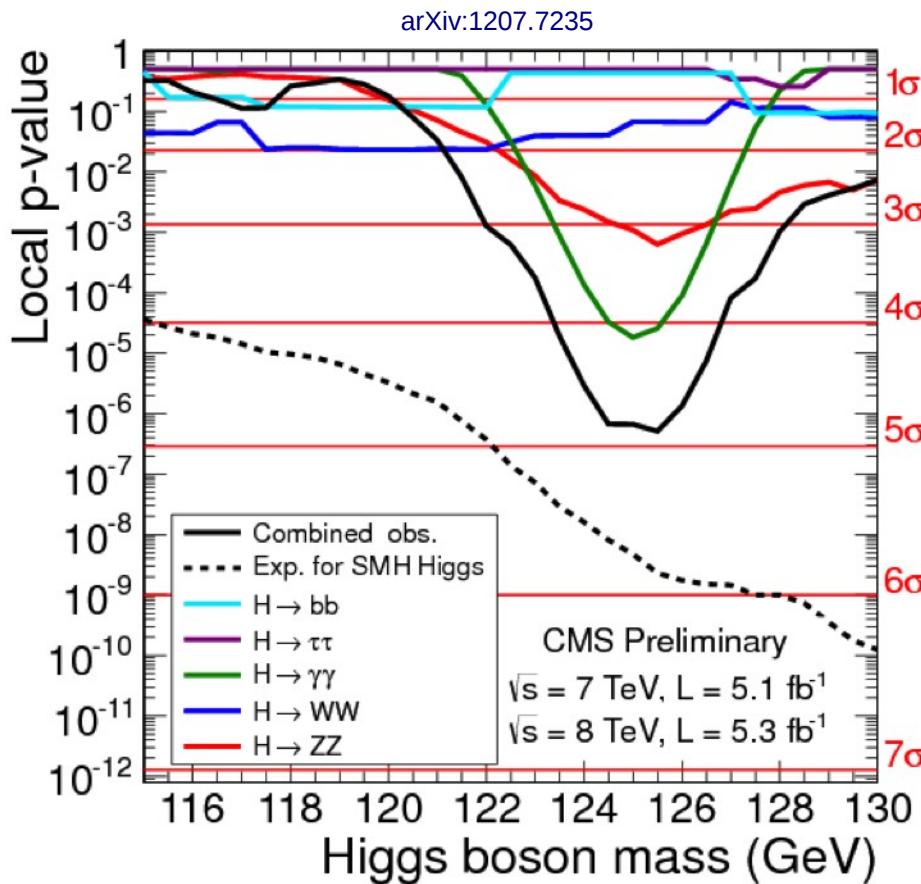
$$L_F = \sum_{\Psi} \bar{\Psi} i \gamma^\mu D_\mu \Psi \quad D_\mu \Psi = (\partial_\mu - \underbrace{ig_s T^a G_\mu^a}_{\text{SU(3)}} - \underbrace{ig \frac{\tau^i}{2} W_\mu^i}_{\text{SU(2)}} - \underbrace{ig' \frac{1}{2} B_\mu}_{\text{U(1)}}) \Psi$$

$$L_{gauge} = -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} - \frac{1}{4} G_{\mu\nu}^a G^{a\mu\nu}$$

$$L_\phi = (D_\mu \phi)^\dagger (D^\mu \phi) - V(\phi^\dagger \phi)$$

$$D_\mu \phi = (\partial_\mu - \underbrace{ig \frac{\tau^i}{2} W_\mu^i}_{\text{SU(2)}} - \underbrace{ig' \frac{1}{2} B_\mu}_{\text{U(1)}}) \phi$$

Higgs Discovery



P-value:

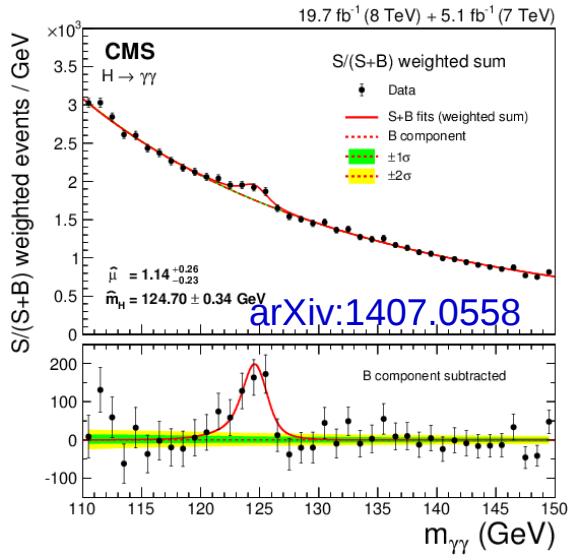
$$p = \int_{t_m}^{\infty} g(t|H_0) dt$$

Probability to measure values $t > t_m$ if H_0 is true

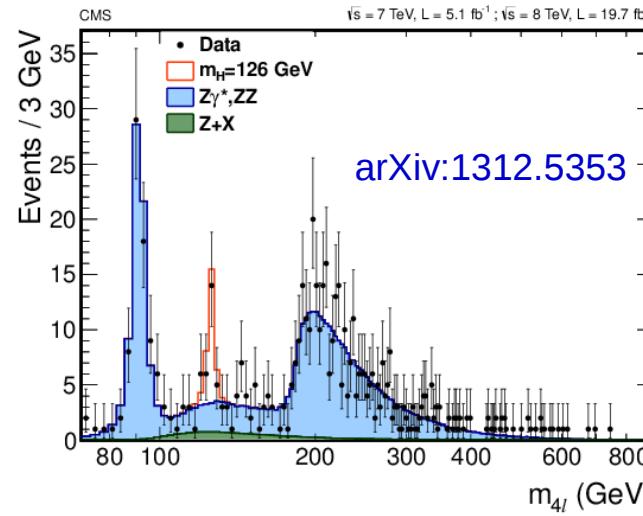
..so there's a chance of less than 10^{-6}

First LHC run 2010-2012

$H \rightarrow \gamma\gamma$



$H \rightarrow ZZ$



- It is a boson
- Spin 0 (Landau Yang Theorem)
- Mass at $\sim 125 \text{ GeV}$
- CP even : $J^P=0^+$ (very likely)
- BUT: Is it **THE** SM Higgs Boson or could it be something else?

Problems of the SM

- Higgs mechanism “deus ex machina”
- Gravitation not included
- Dark Matter
- Neutrino masses
- Matter anti-matter asymmetry
- No strong & weak & em unification
- ...

Extensions of the SM - SUSY

- every boson as a fermion as superpartner and vice versa
- Same mass, same quantum numbers (except spin)
- Must be **broken** (same mass particles not observed)

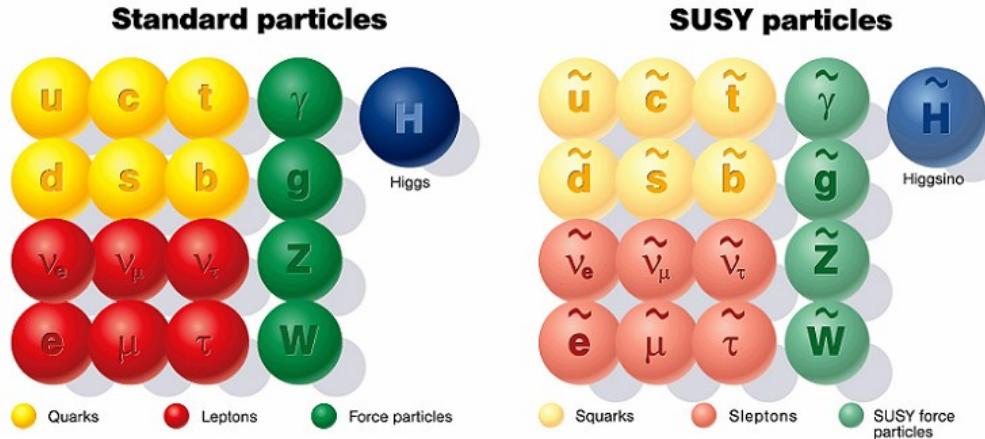


Illustration by CERN & IES de SAR

- Hidden sector and visible sector → what is the messenger?
- R-Parity: LSP possible DM candidate

MSSM

- Same symmetry group, $SU(3) \times SU(2) \times U(1)$, as SM
- Need second Higgs doublet with $Y=-1$ for down type quark masses in Yukawa coupling

$$L_Y = g \bar{\Psi} \Phi \Psi \quad H_2 = \begin{pmatrix} H_2^+ \\ H_2^0 \end{pmatrix} \quad H_1 = \begin{pmatrix} H_1^0 \\ H_1^- \end{pmatrix}$$

$\text{VEV}_1=v_1$, $\text{VEV}_2=v_2$

- In SM H_2^\dagger gives rise to down type quark masses. But is not allowed in SUSY.
- 8 d.o.f – 3 (W, Z) → **5 physical states**
- 2 CP-even neutral Higgs bosons: H, h
- 1 CP-odd neutral Higgs boson: A
- 2 charged Higgs bosons: H^+, H^-

- Two free parameters: $\tan \beta = \frac{v_1}{v_2}$ m_A

$$\tan \beta = \frac{v_2}{v_1}, \quad v_1^2 + v_2^2 = v^2 = 4 \frac{m_Z^2}{g^2 + g'^2} \approx 246 \text{ GeV}$$

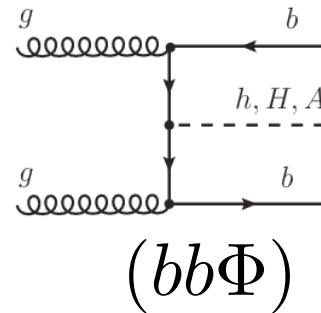
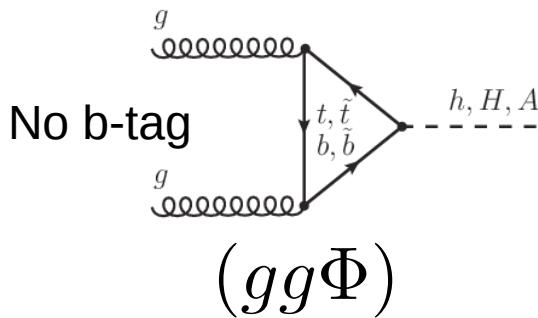
- All MSSM Higgs masses can be expressed through $\tan \beta = \frac{v_1}{v_2}$ m_A

$$m_{H^{+-}}^2 = m_A^2 + m_W^2 \quad m_{H, h}^2 = \frac{1}{2} \left(m_A^2 + m_Z^2 \pm \sqrt{(m_A^2 + m_Z^2)^2 - 4m_A^2 m_Z^2 \cos^2 2\beta} \right)$$

- Other parameters fixed to **benchmark scenarios**
- **Tree level:** e.g. upper bound on m_h (light scalar Higgs boson mass)
 - $m_h \leq m_Z \cos 2\beta$ After radiative corrections: $m_h \approx 135 \text{ GeV}$
 - e.g. Benchmark scenario m_h^{\max} : allow m_h to reach 135 GeV
 - More benchmark scenarios..(e.g. m_H, m_h compatible with SM Higgs mass)

Production and decay

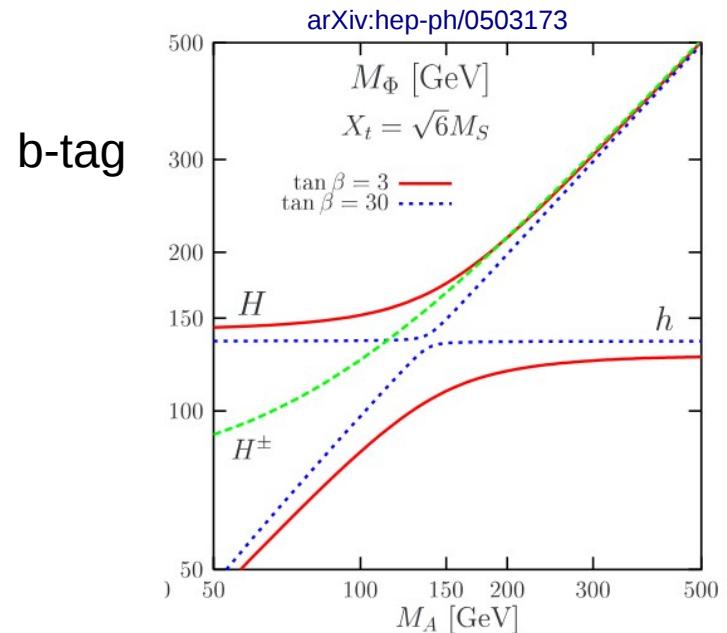
- LHC: Upper mass bound on SM like Higgs (h) with higher order corrections
 $m_h^2 \approx M_Z^2 \cos^2(2\beta) + \Delta m_h^2 \quad m_h \approx 125\text{GeV} \rightarrow \Delta m_h \approx 85\text{GeV} \rightarrow \text{large } \tan \beta$
- Gluon fusion dominant at small $\tan \beta$
- Large $\tan \beta (>>1)$ → stronger Yukawa coupling to down type fermions → b-quark associated production dominant



- Interesting decay channels (for large $\tan \beta$)

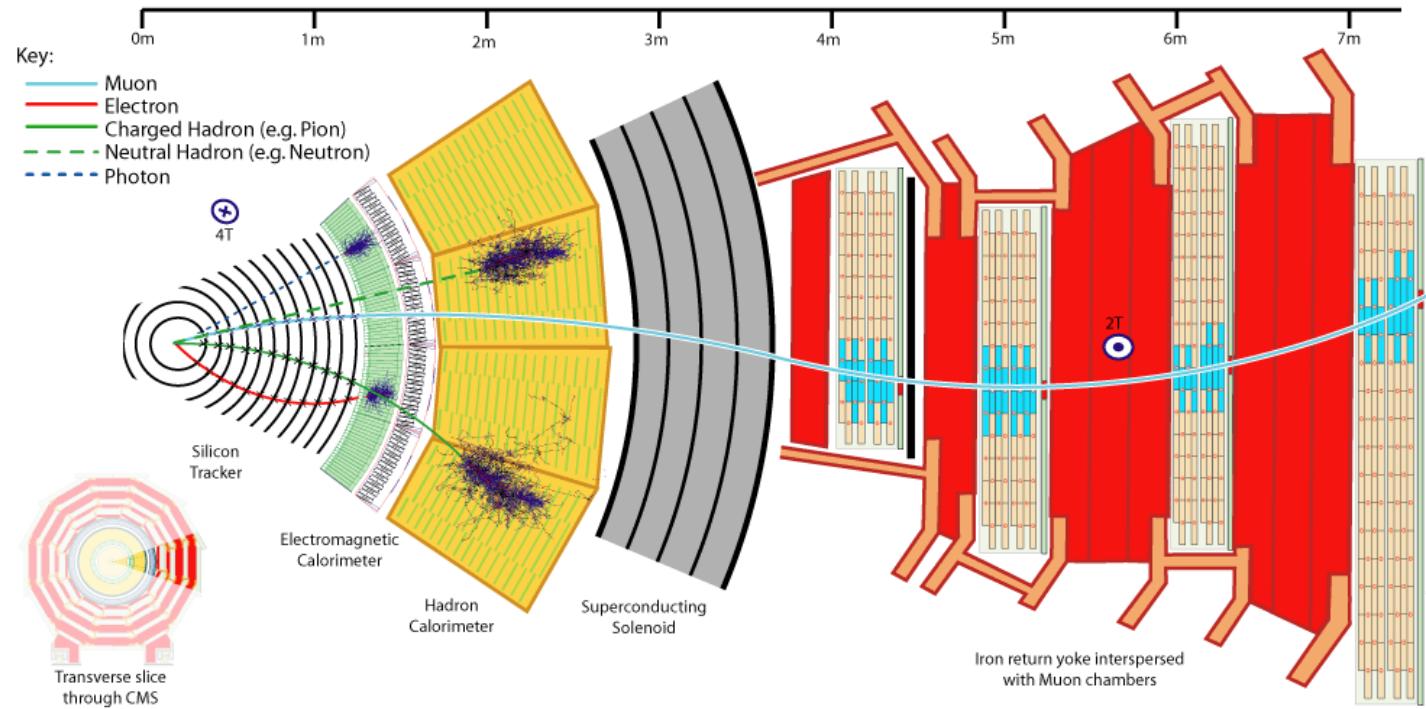
$H \rightarrow \tau\tau$

$H \rightarrow bb$



Experimental setup Compact MUON Selenoid

- CMS detector can detect $e, \mu, p, n, \gamma, K, \pi \rightarrow \text{no } \tau$



CMS-doc-4172-v2

- One needs to reconstruct τ events from decay products

τ decays

- Decays in lighter leptons and hadrons $m_\tau \approx 1776$ GeV

$$\tau \rightarrow e + \nu_e + \nu_\tau$$

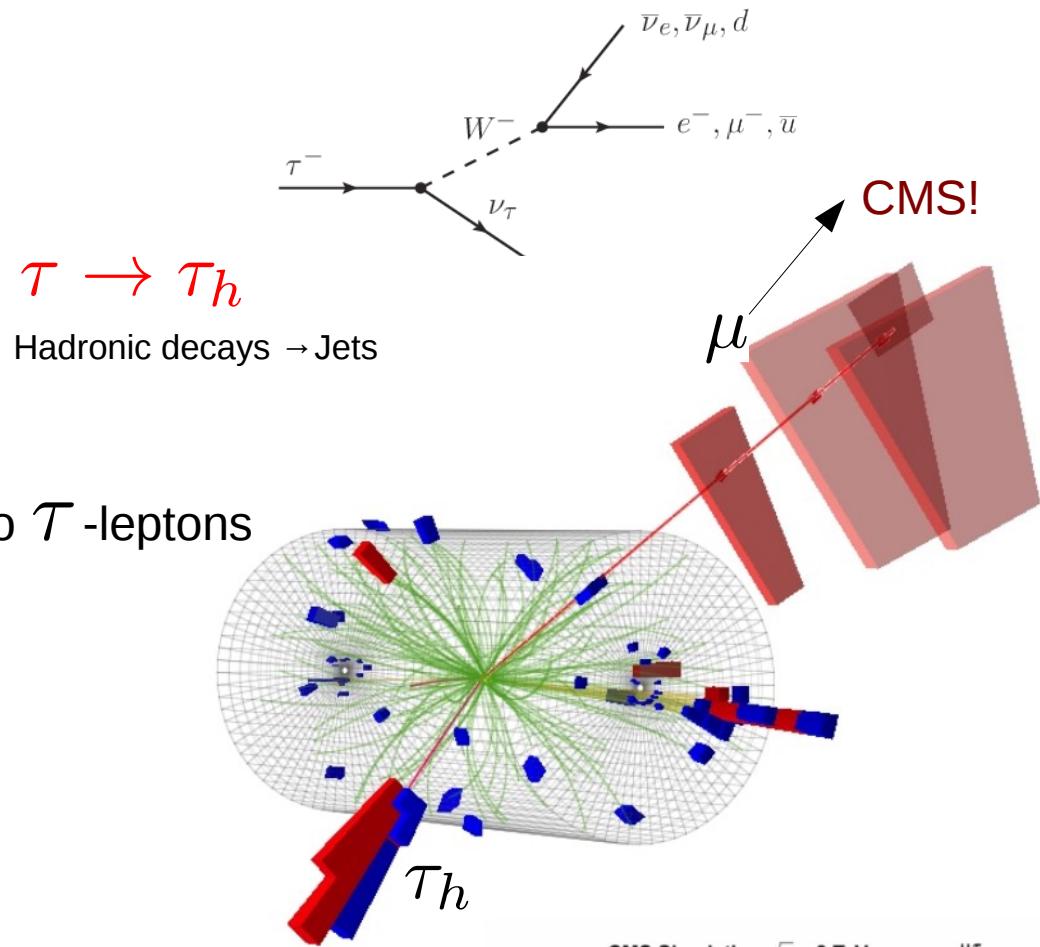
$$\tau \rightarrow \mu + \nu_\mu + \nu_\tau$$

$$\begin{aligned} \tau^- &\rightarrow \pi^- + \pi^0 + \nu_\tau \\ \tau^- &\rightarrow \pi^- + \nu_\tau \end{aligned} \quad \left. \right\}$$

...

- Important decay modes for two τ -leptons

$\tau_h \tau_h$, $\mu \tau_h$, $e \tau_h$,
 $e \mu$, $\mu \mu$, ee



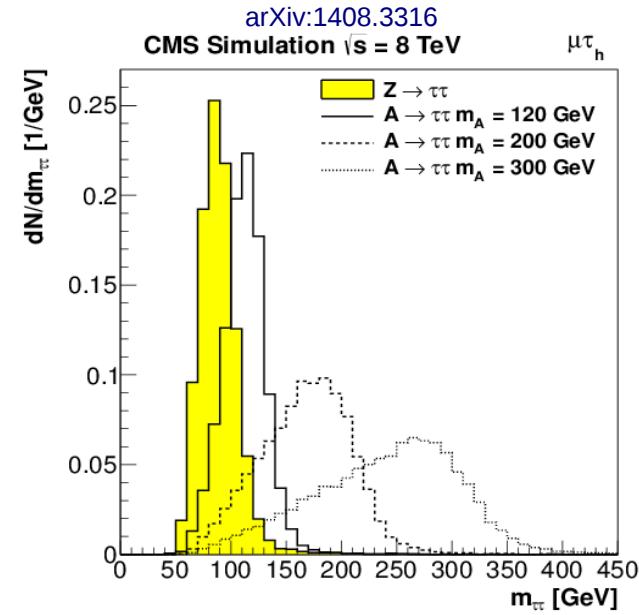
DESY-Seminar 2014 Roger Wolf

Searches for $A/H/h \rightarrow \tau\tau$

- Expect two isolated high p_T leptons $(\underbrace{e, \mu, \tau_h}_{\text{Trigger objects}})$ τ From Higgs decays should be isolated (not inside jets)

- Reduce backgrounds

- Reconstruct $m_{\tau\tau}$
 - ML technique
 - Distinguish Higgs signal from bkg



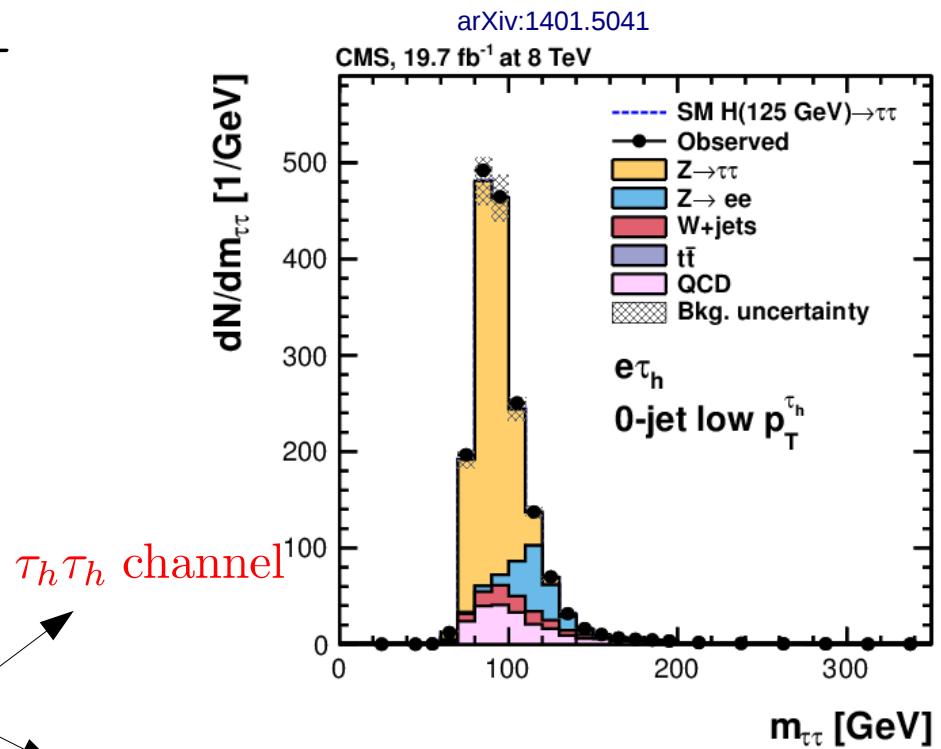
- Enhance sensitivity to **MSSM Higgs bosons** with b-tag associated Higgs production (large $\tan \beta$)

Background

- Largest source of bkg $Z \rightarrow \tau\tau$
- Embedding method

Take $Z \rightarrow \mu\mu$ from data
 Replace reconstructed μ by simulated τ decays
 (lepton universality)

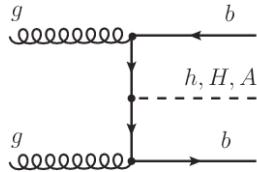
- QCD multijet events:
 - 2J misidentified as τ_h decays
 - 1J misidentified as τ_h decay
- W+Jets: contributes to $e\tau_h$ and $\mu\tau_h$ channel
- Drell-Yan production of μ pairs



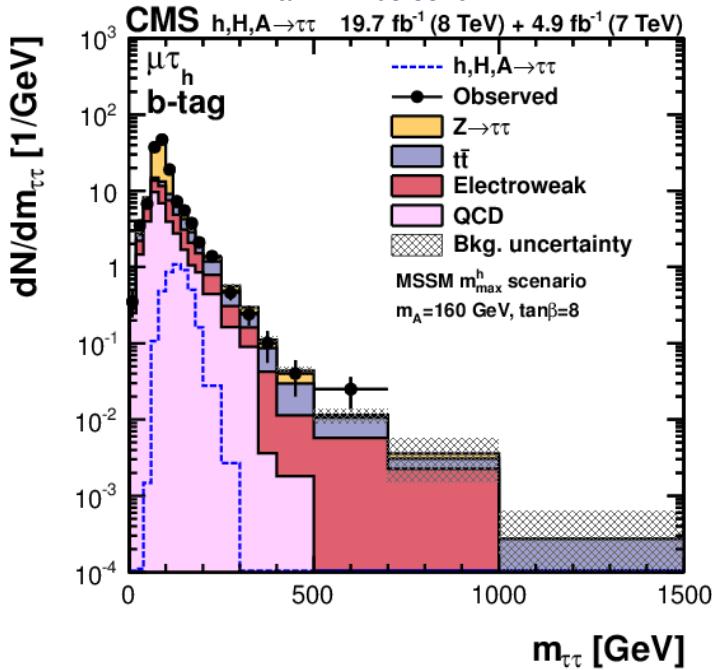
Process	$\mu\tau_h$ channel			
	$\sqrt{s} = 7 \text{ TeV}$		$\sqrt{s} = 8 \text{ TeV}$	
	no b-tag	b-tag	no b-tag	b-tag
$Z \rightarrow \tau\tau$	26838 ± 244	284 ± 8	87399 ± 497	1118 ± 31
QCD	5495 ± 258	131 ± 18	18056 ± 811	552 ± 62
W+jets	2779 ± 201	55 ± 14	12845 ± 793	237 ± 52
$Z + \text{jets} (\text{e}, \mu \text{ or jet faking } \tau)$	716 ± 109	11 ± 2	3704 ± 454	54 ± 9
$t\bar{t}$	82 ± 6	36 ± 5	564 ± 41	194 ± 22
Di-bosons + single top	94 ± 11	12 ± 2	506 ± 51	60 ± 7
Total background	36004 ± 205	530 ± 18	123075 ± 407	2214 ± 44
$A + H + h \rightarrow \tau\tau$	226 ± 23	17 ± 2	929 ± 85	67 ± 9
Observed data	36055	542	123239	2219
Efficiency \times acceptance				
gluon fusion Higgs	$2.34 \cdot 10^{-2}$	$2.49 \cdot 10^{-4}$	$1.78 \cdot 10^{-2}$	$2.32 \cdot 10^{-4}$
b-quark associated Higgs	$1.96 \cdot 10^{-2}$	$3.54 \cdot 10^{-3}$	$1.53 \cdot 10^{-2}$	$2.66 \cdot 10^{-3}$

arXiv:1408.3316

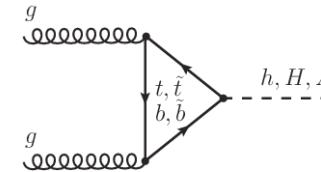
Signal extraction



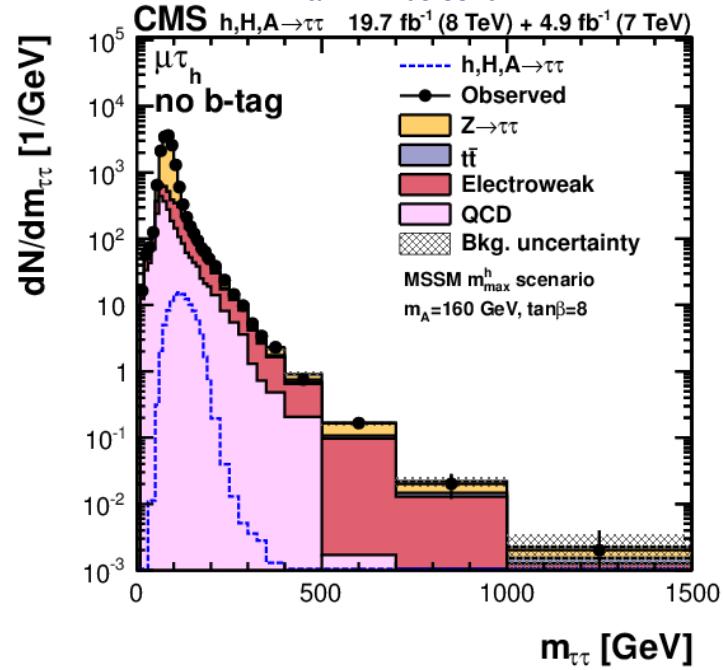
arXiv:1408.3316



b-tag



arXiv:1408.3316



No b-tag

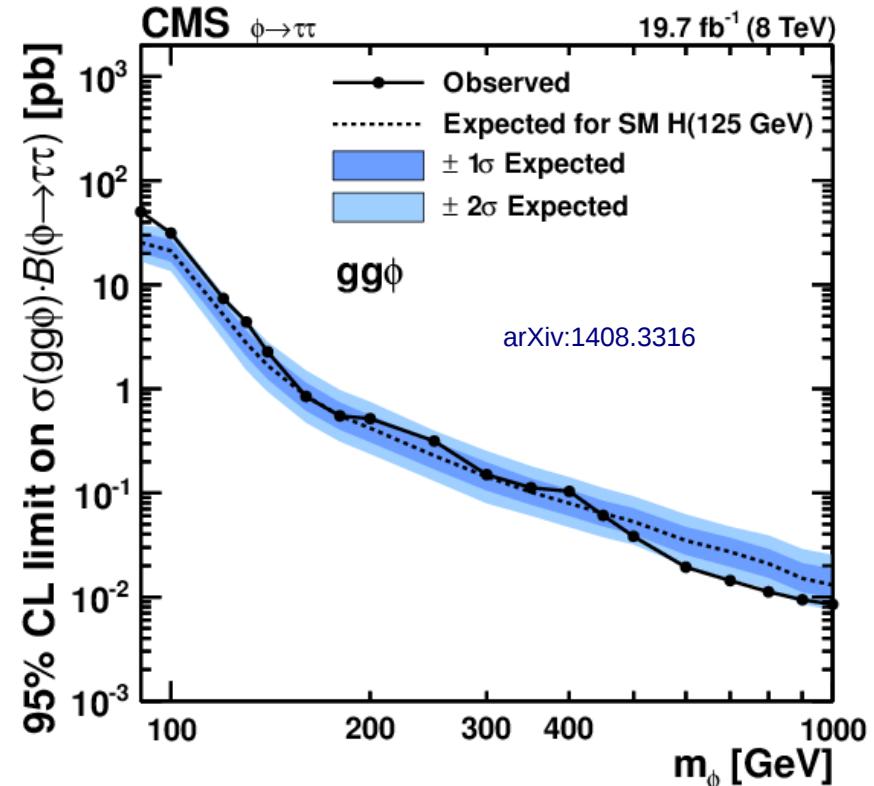
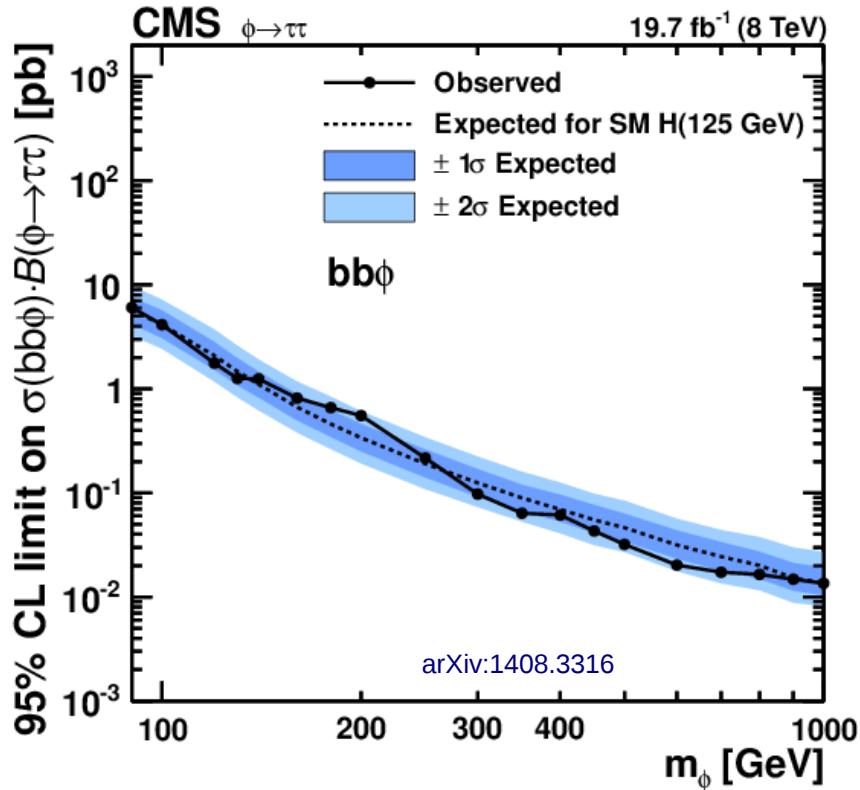
Model independent searches

- Search for a narrow ϕ resonance
- Test statistic q based on profile likelihood ratio Signal or bkg like data?

$$q_\mu = -2 \ln \frac{L(N_{obs} | \mu \cdot s + b, \hat{\theta}_\mu)}{L(N_{obs} | \hat{\mu} \cdot s + b, \hat{\theta})} \quad , \quad 0 \leq \hat{\mu} \leq \mu$$

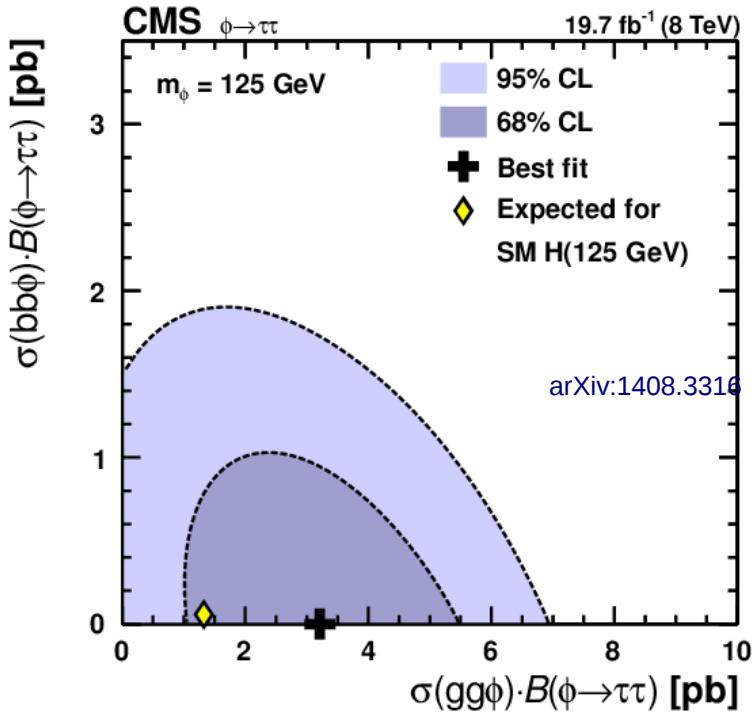
- $\hat{\theta}_\mu$ maximizes likelihood in the numerator for given μ
 - $\hat{\theta}$ and $\hat{\mu}$ define the point where the likelihood reaches its global maximum
- Upper limits on $\sigma \cdot B(\phi \rightarrow \tau\tau)$ for $\sigma(gg\phi)$ and $\sigma(bb\phi)$

Model independent searches 1D



- Treat other production channel as nuisance parameter

Model independent searches 2D



- Likelihood contour plots for SM Higgs mass
- Result compatible with SM Higgs

MSSM model dependent searches

- Modified CL approach (MSSM vs bkg only is not valid anymore)
- Test compatibility of the data to h , H , A signal compared to SM Higgs signal

$$M(\mu) = [\mu \cdot s(\text{MSSM}) + (1 - \mu) \cdot s(\text{SM})] + b$$

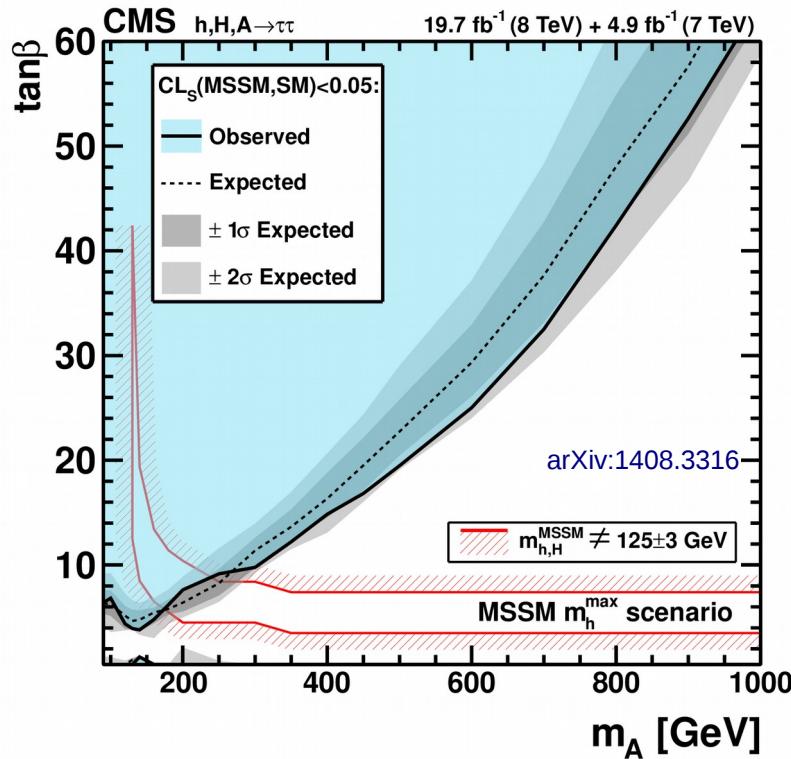
Physical model

$$q_{MSSM/SM} = -2 \ln \frac{L(N_{obs}|M(1), \hat{\theta}_\mu)}{L(N_{obs}|M(0), \hat{\theta}_0)}$$

Maximized by finding the
Corresponding nuisance parameters for
 $M(1)$ and $M(0)$

- Expectation for every benchmark scenario is determined at each point of the parameter space $\tan\beta$, m_A

MSSM model dependent searches



Uncertainties

- **Experimental uncertainties**
 - Integrated Luminosity ~2%
 - Jet energy scale 1-10%
 - Identification and trigger efficiencies ~2%
 - τ Uncertainty ~8%
 - B-tagging 2-7%
 - Mistag for light flavor partons 10-20%
- **Theoretical uncertainties**
 - σ depends on $\tan\beta$, m_A and benchmark scenario
 - up to 20%

Summary

- No BSM physics in run 1
- Run 2?
- No evidenz in run 2 → What will happen to SUSY?

Backup

