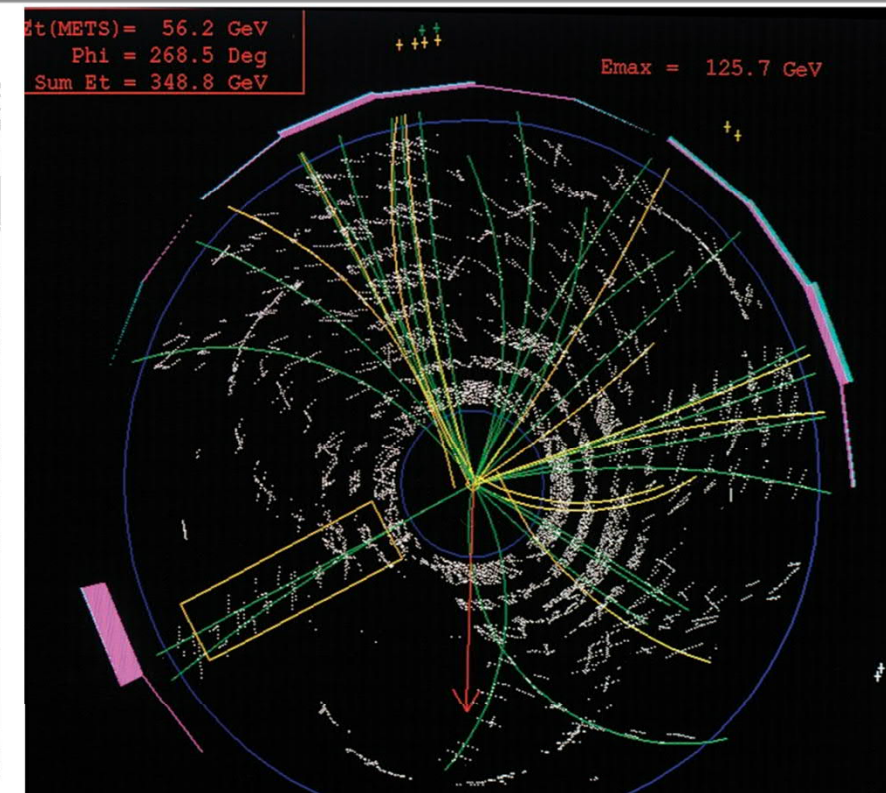
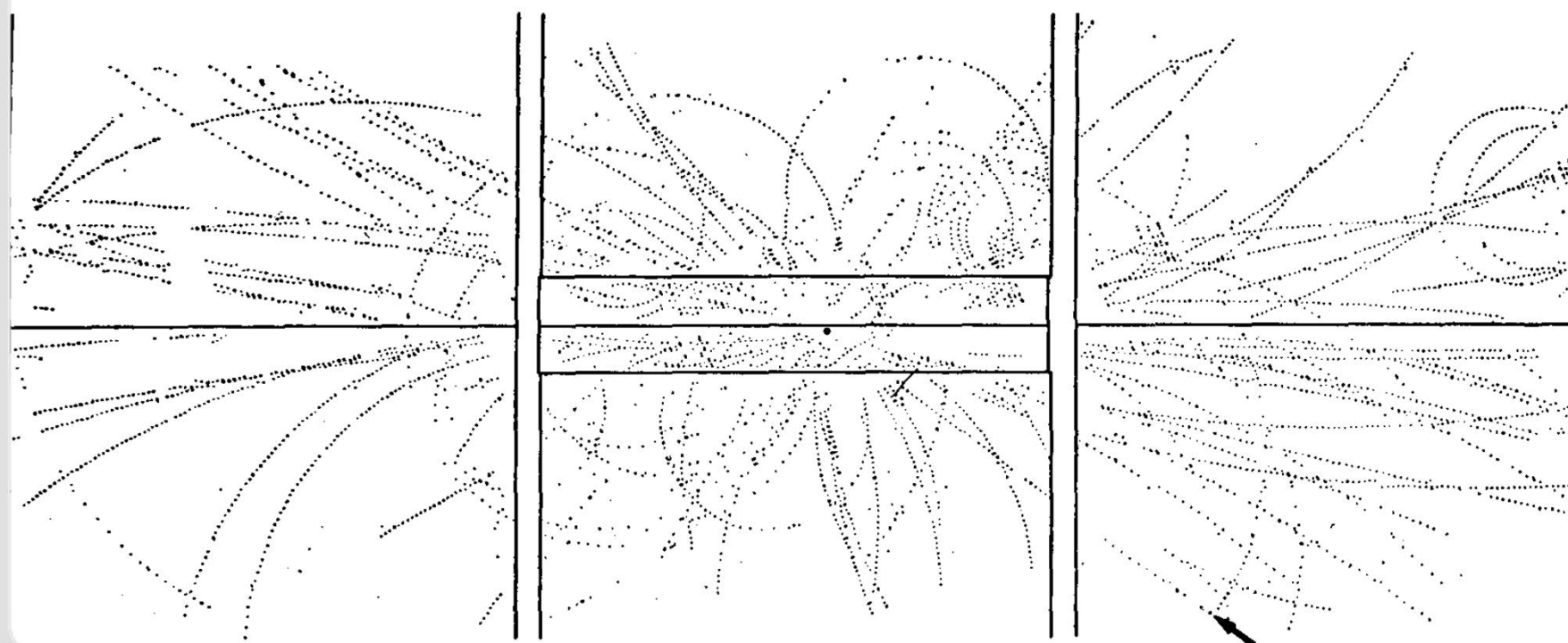


# KSETA-Course: Accelerator-Based Particle Physics

## Flavor- and Top physics

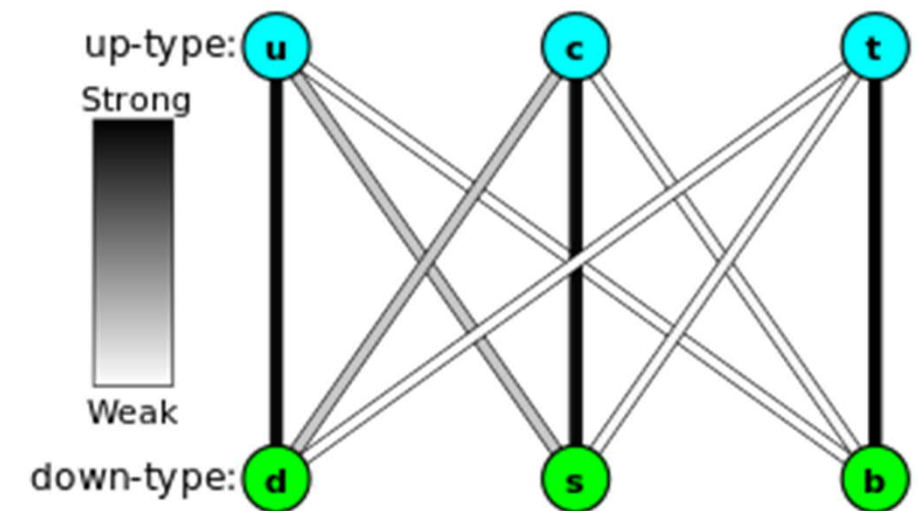
Matthias Mozer, Roger Wolf  
Institut für Experimentelle Kernphysik, Karlsruher Institut für Technologie

EVENT 2958. 1279.



# Reminder: what is flavor?

- Quarks and quantum numbers
  - six different flavors  
→ six different quantum numbers
  - conserved in strong and EM interaction
  - can change in weak interaction
  - three up-type (charge  $2/3$ )  
three down-type (charge  $-1/3$ )
- Why flavor physics?
  - classic flavor physics:  
hadrons with s,c,b quarks
  - top quark too unstable to form hadrons  
→ mostly considered its own field



# Reminder: History

## 1953: Gell-Mann and Nishijima:

- Explain “strange particles” with new flavor quantum number *strangeness (S)*
- strangeness conserved in strong and EM interaction changes in weak interaction

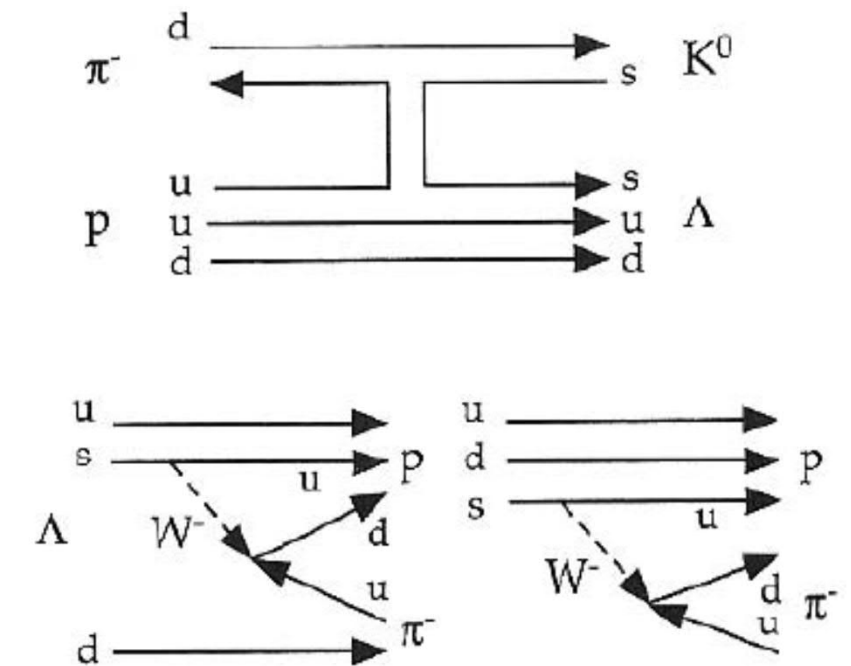
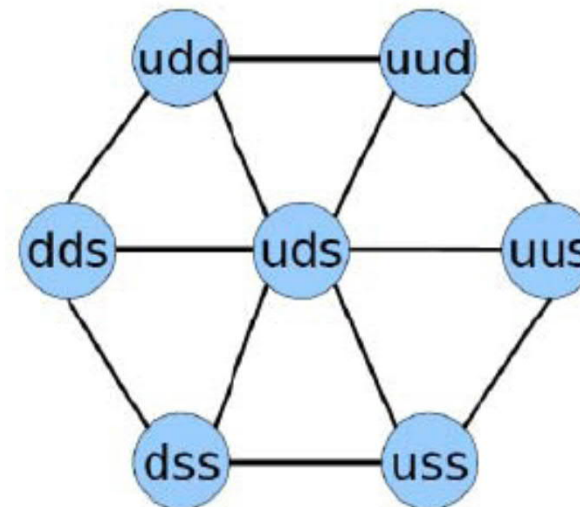
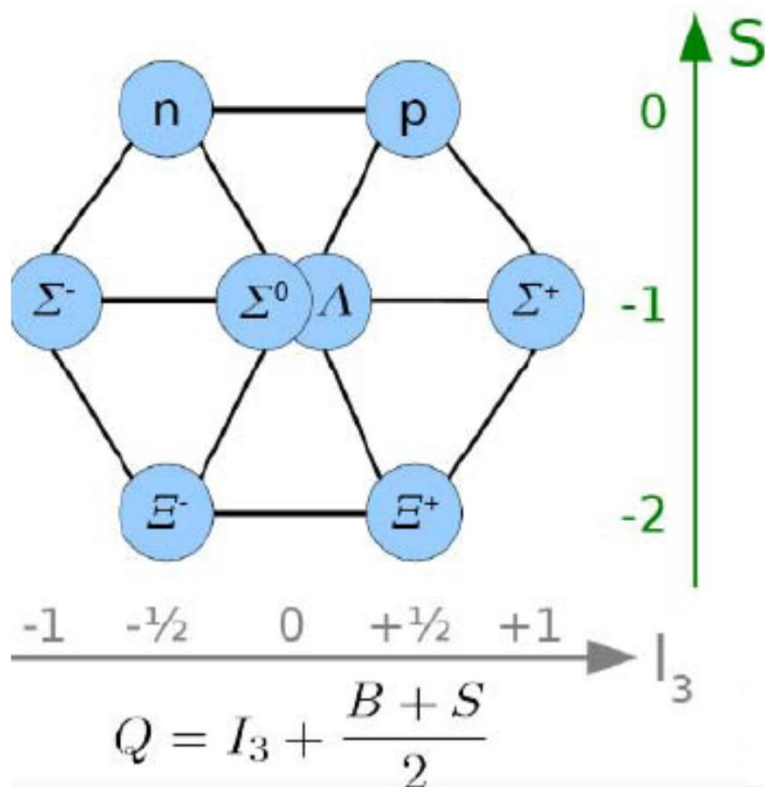


*Murray Gell-Mann*

Nobel price  
1969

## 1964: Gell-Mann

- particle zoo (hadrons) explained in the quark model (using u,d,s quarks)

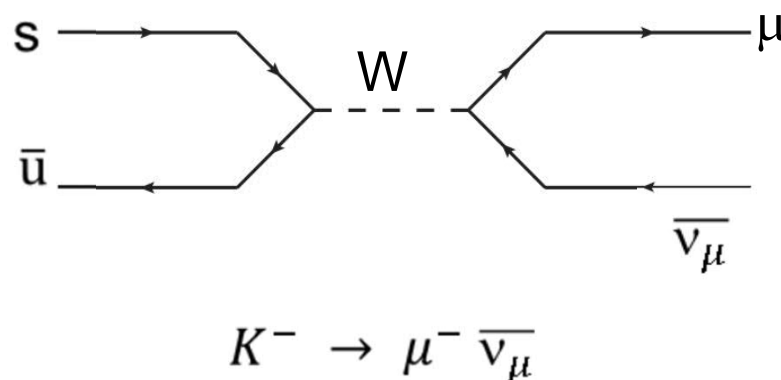
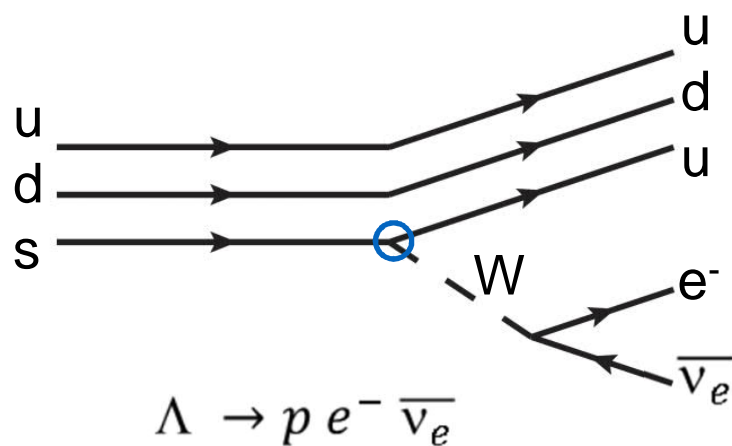
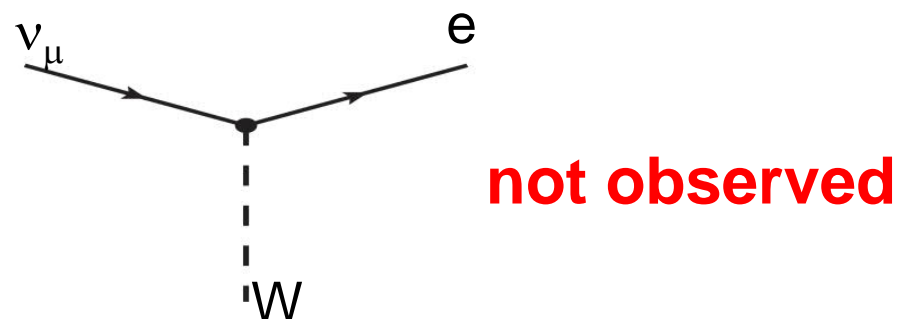
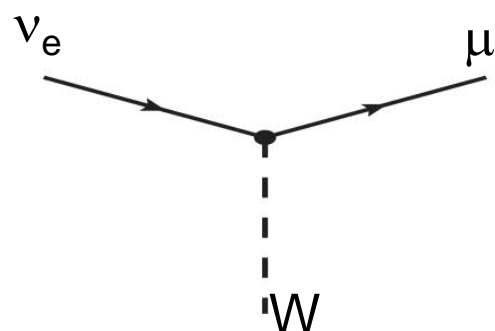
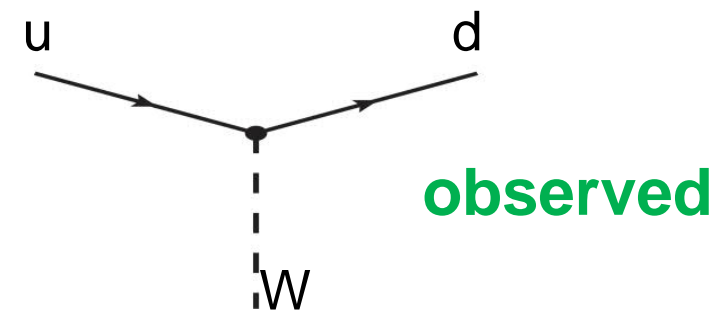
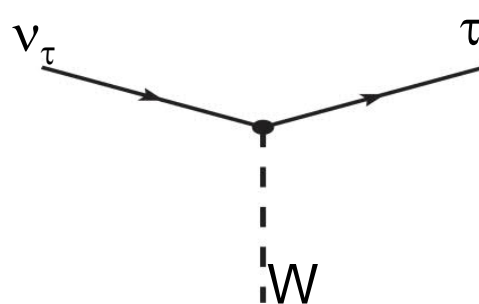
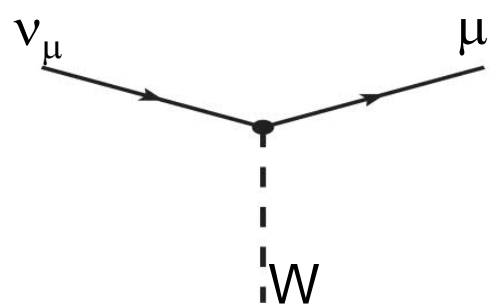
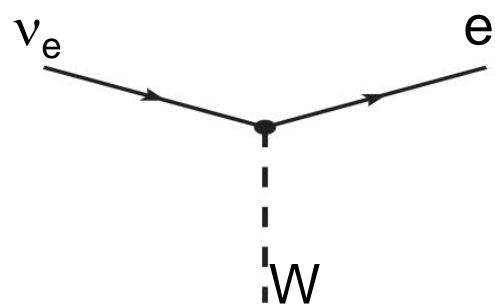


# Weak interaction of quarks

Nucl.  $\beta$ -decays, meson- decays,  $\nu N$ -scattering:

→ universal coupling of weak interaction to leptons and quarks

observations:



**observed**

i.e. quarks  
change family



# Cabibbo theory

Observation from  $n, \mu$  decays  $G_F(n)/G_F(\mu) = 0.98 \neq 1$

**Nicola Cabibbo:** quarks mix  $\rightarrow$  mass-eigenstates  $\neq$  flavor-eigenstates

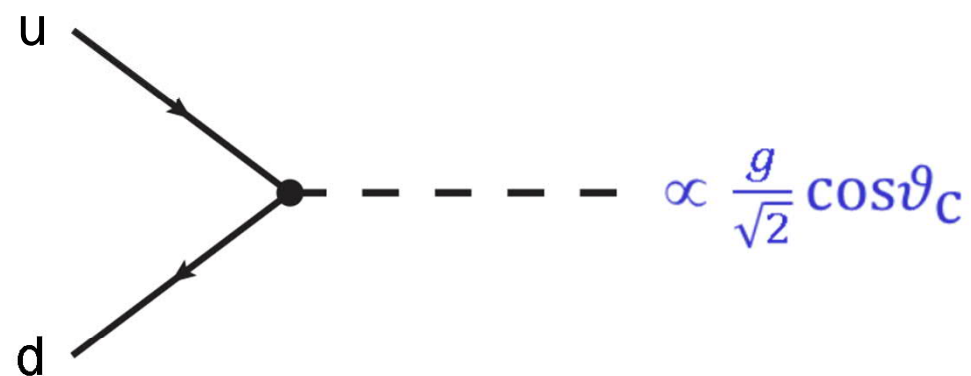
$$\begin{pmatrix} u \\ d' \end{pmatrix} = \begin{pmatrix} u \\ d \cdot \cos\vartheta_C + s \cdot \sin\vartheta_C \end{pmatrix}$$

weak isospin doublet

$\swarrow$  convention

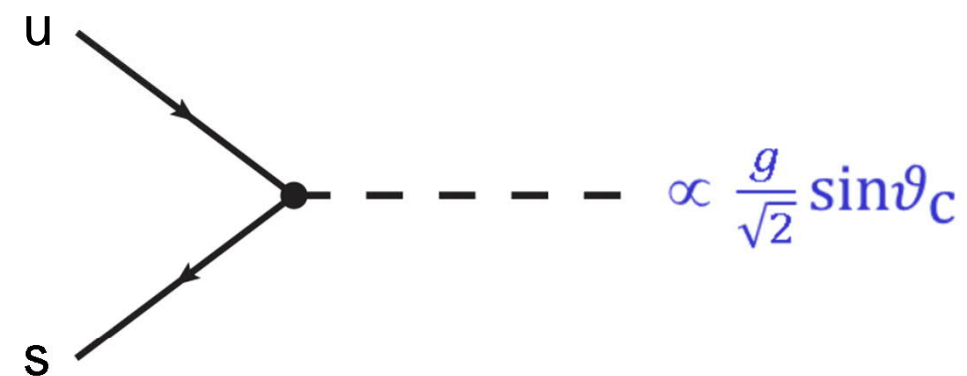
mass eigenstates  $d, s, b$   $u, c, t$

$\Rightarrow$



$$\rightarrow G_F(n)/G_F(\mu) = \cos\vartheta_C = 0.98$$

flavor-eigenstates  $d', s', b'$   $u, c, t$

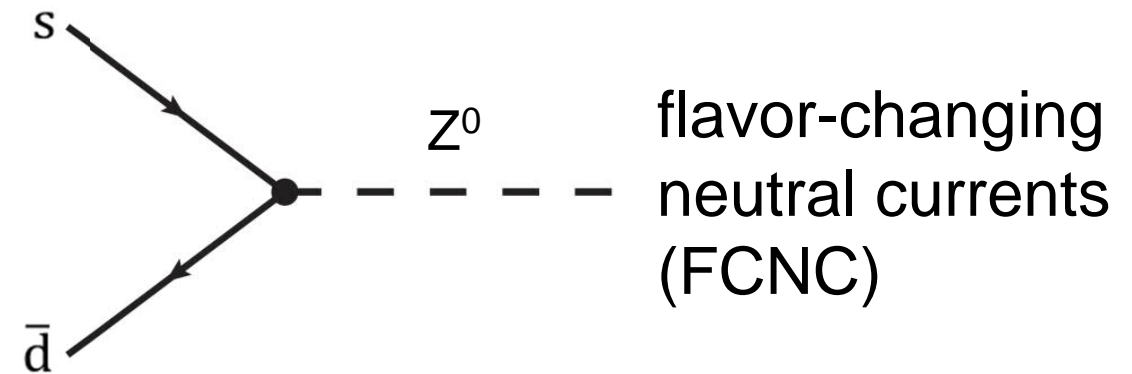


$\vartheta_C$  : Cabibbo-angle

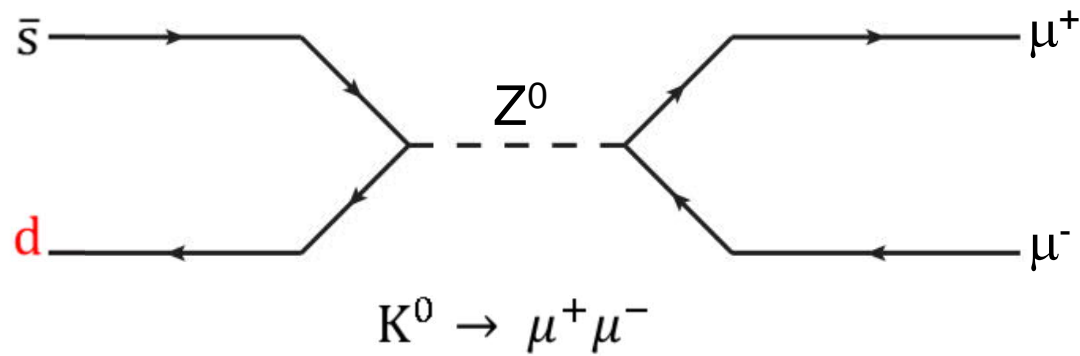
$$\vartheta_C = 12.9^\circ$$

# GIM Mechanism

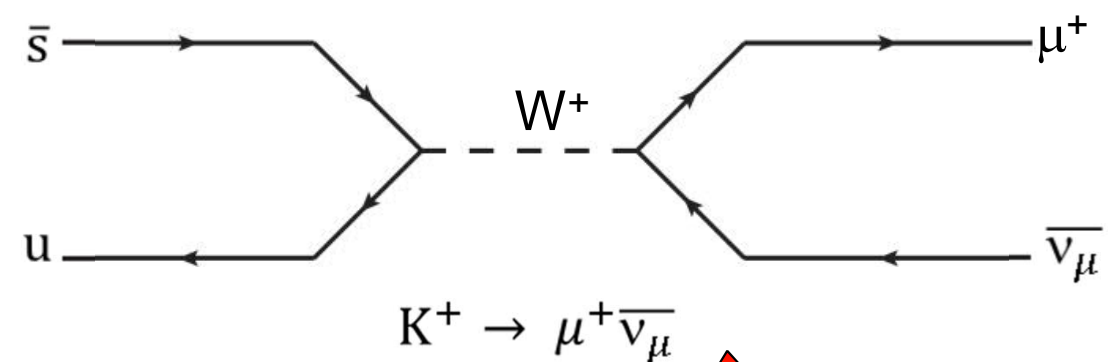
Expected transitions:



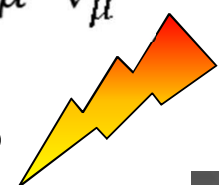
i.e. decays like:



analogous to observed decays:



Observation:  $BR(K^0 \rightarrow \mu^+ \mu^-) = 7 \cdot 10^{-9}$

$BR(K^+ \rightarrow \mu^+ \nu_\mu) = 64\%$  

proposal by GIM (1970): additional weak doublet  
(Glashow, Iliopoulos, Maiani)  $\Rightarrow$  c-quark prediction  
(observed 1970)

$$\begin{pmatrix} c \\ s' \end{pmatrix} = \begin{pmatrix} c \\ s \cdot \cos\vartheta_c - d \cdot \sin\vartheta_c \end{pmatrix}$$

Sheldon L.  
Glashow

Nobel price  
1979



# GIM Mechanism

Mixing matrix:  $\begin{pmatrix} d' \\ s' \end{pmatrix} = \begin{pmatrix} \cos \vartheta_c & \sin \vartheta_c \\ -\sin \vartheta_c & \cos \vartheta_c \end{pmatrix} \begin{pmatrix} d \\ s \end{pmatrix}$  ← mass eigenstates

electroweak eigenstates

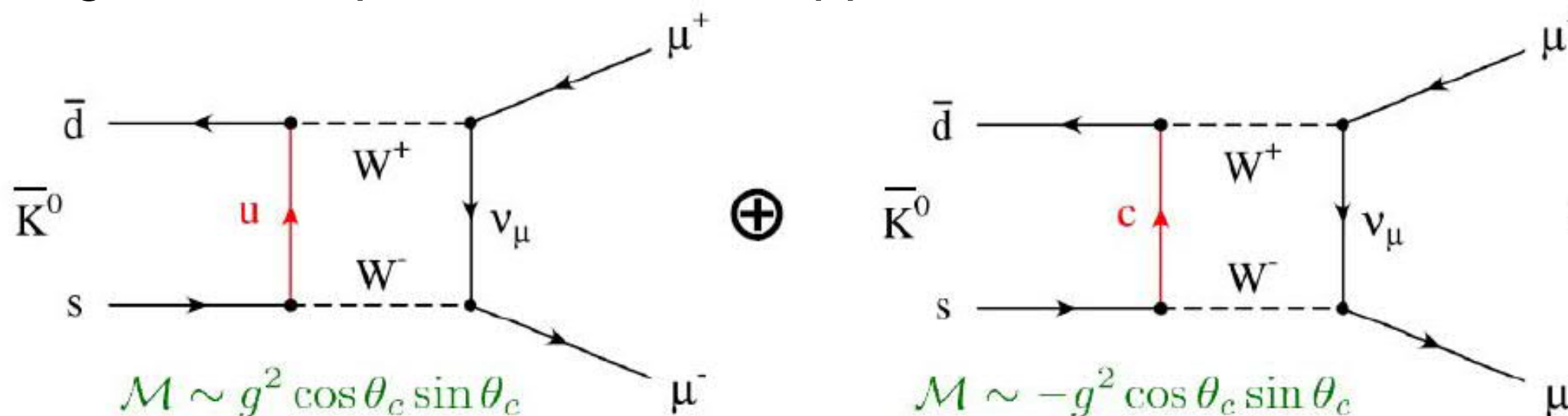
Interference cancels mixed terms ( $d \rightarrow s$ ) in the Lagrangian. Only flavor-conserving neutral currents remain:

$$\bar{d}' d' + \bar{s}' s' + \bar{u} u + \bar{c} c = \dots = \bar{d} d + \bar{s} s + \bar{u} u + \bar{c} c$$

no mixed terms  $\bar{d}s$   
→ no FCNC

← short for  $\bar{u} \gamma_\mu (c_v - c_A \gamma^5) u$

higher order processes also suppressed



$\Sigma=0$  if  $m_u=m_c$   
⇒ amplitude  $\neq 0$   
due to different quark masses

# 3-Doublet Extension

Today: 3 flavor-families with CKM-matrix  
(Cabibbo-Kobayashi-Maskawa)

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = M_{\text{CKM}} \begin{pmatrix} d \\ s \\ b \end{pmatrix} \quad M_{\text{CKM}}: \text{unitary } 3 \times 3 \text{ matrix}$$

$$M_{\text{CKM}} = \begin{pmatrix} \boxed{C_1} \approx 1 & C_3 S_1 & S_1 S_3 \\ -C_2 S_1 & \boxed{C_1 C_2 C_3 - S_2 S_3 e^{i\delta}} & C_1 C_2 S_3 + C_3 S_3 e^{i\delta} \\ -S_1 S_2 & C_1 C_3 S_2 + C_2 S_3 e^{i\delta} & \boxed{C_1 S_2 S_3 - C_2 C_3 e^{i\delta}} \approx 1 \end{pmatrix}$$

with:

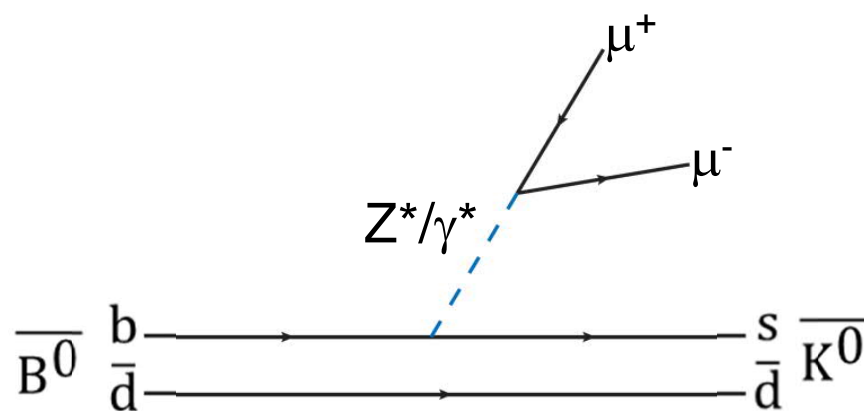
$$c_i = \cos \theta_i \quad s_i = \sin \theta_i$$

$e^{i\delta}$ : phase

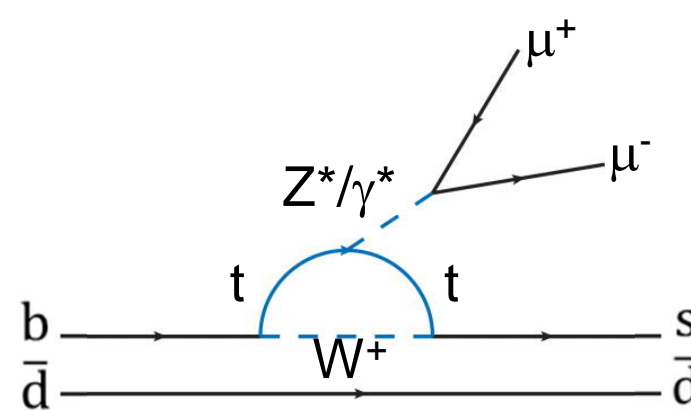
→ CP-violation

Test the SM: search for FCNC

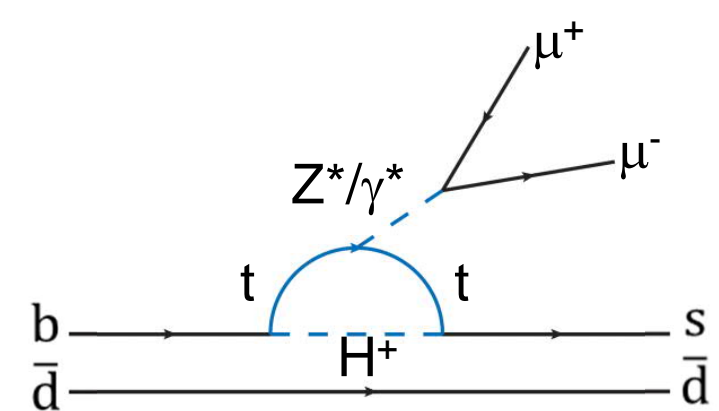
example:  $B^0 \rightarrow \mu^+ \mu^- K^0$  (SM: BR =  $5 \cdot 10^{-7}$ ),  $B^0 \rightarrow \mu^+ \mu^- K^{0*}$  (SM: BR =  $5 \cdot 10^{-6}$ )



**Not** allowed in SM  
(FCNC)



allowed in SM  
("penguin")

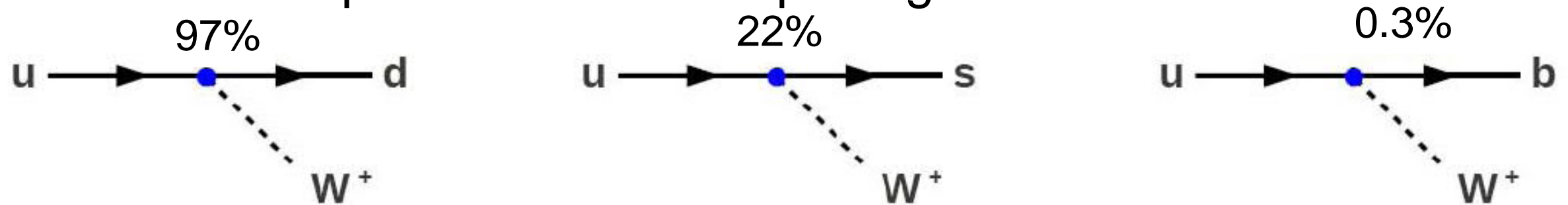


test the SM:  
possible new particles (i.e SUSY)



# CKM Matrix

- change of quark flavor only via W-boson exchange
- W-boson couples to mixture of quark generations



$$M_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- complex elements  
→ 18 parameters
  - Unitarity: ( $MM^\dagger=1$ )  
+ quark phases
- 4 free parameters  
3 angles +  
1 phase ( $\theta_P$ )

# Unitarity Triangle

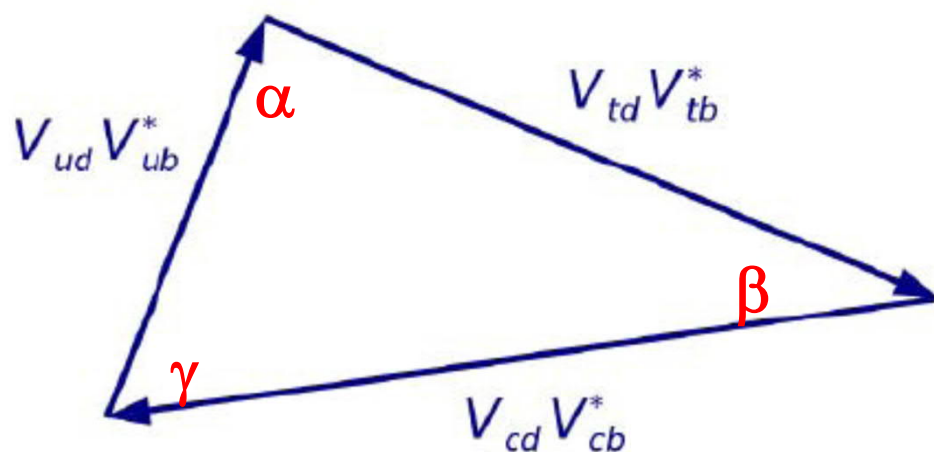
- $N > 4$  observables for 4 parameters  
 $\Rightarrow$  overconstrained system  
 $\Rightarrow$  test the SM
- Graphical representation in „unitarity triangle“  
 $\Rightarrow$  unitarity condition  $\sum_i V_{ij} V_{jk}^* = \delta_{jk}$

$$(V^\dagger V)_{21} : V_{us}^* V_{ud} + V_{cs}^* V_{cd} + V_{ts}^* V_{td} = 0$$

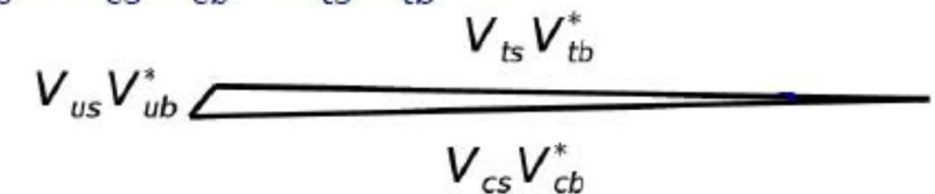
$$(V^\dagger V)_{31} : V_{ub}^* V_{ud} + V_{cb}^* V_{cd} + V_{tb}^* V_{td} = 0$$

$$(V^\dagger V)_{32} : V_{ub}^* V_{us} + V_{cb}^* V_{cs} + V_{tb}^* V_{ts} = 0.$$

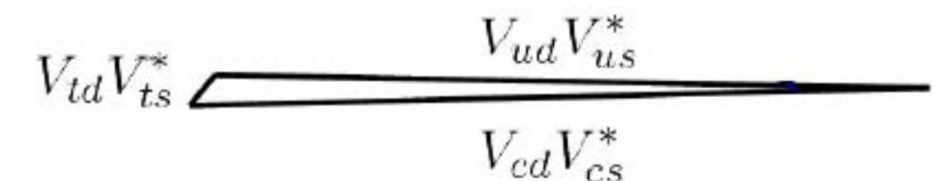
$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$



$$V_{us} V_{ub}^* + V_{cs} V_{cb}^* + V_{ts} V_{tb}^* = 0$$

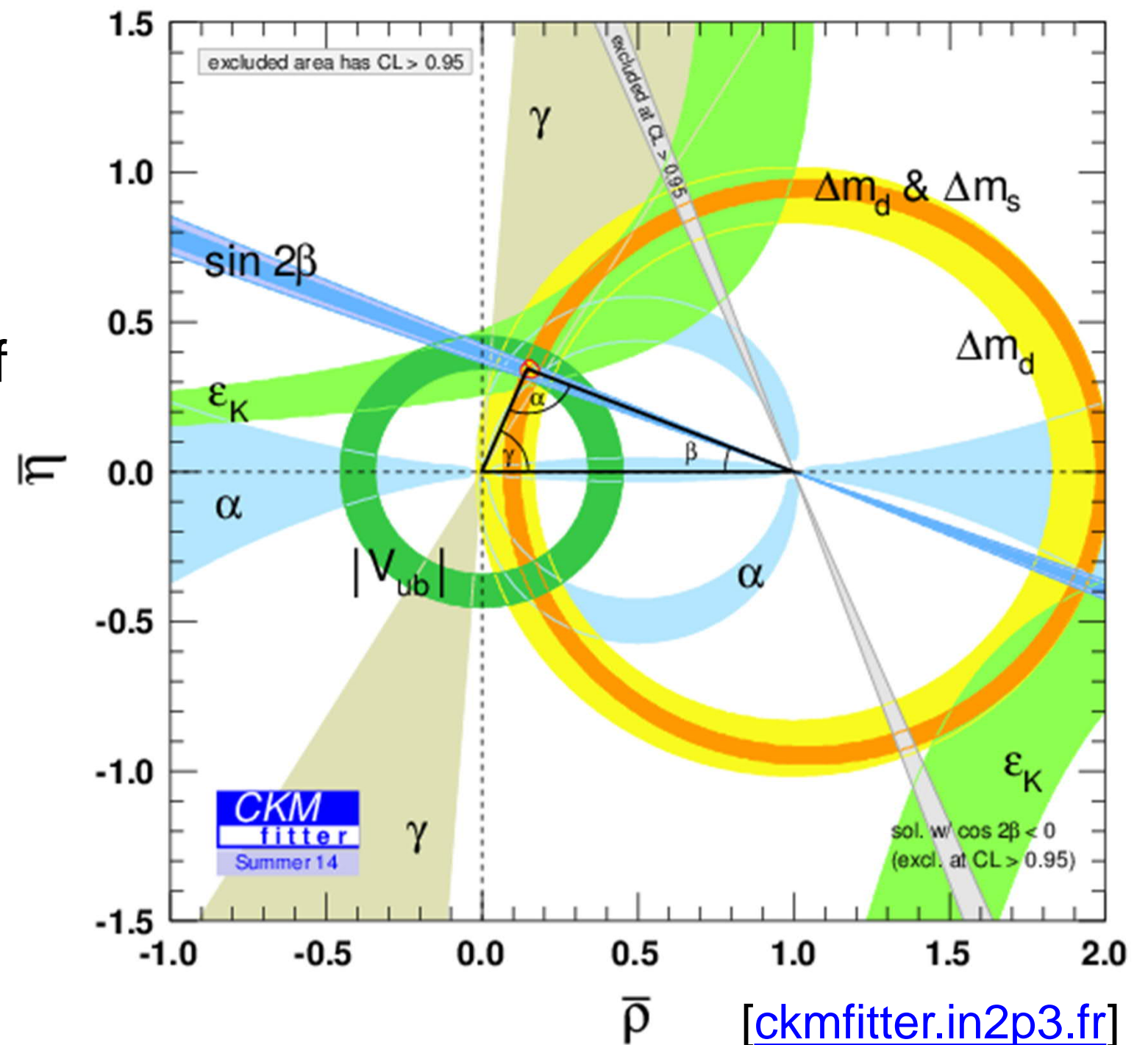


$$V_{ud} V_{us}^* + V_{cd} V_{cs}^* + V_{td} V_{ts}^* = 0$$



# Unitarity Triangle

- Idea: overconstrain with many independent measurements  
→ consistency check
- Could see non-unitarity if  
→ quarks mix with additional generations  
→ quarks couple to additional bosons  
→ ...
- so far consistent



# Flavor Oscillations

## Quantum numbers of hadrons

- hadrons produced in strong interactions  
→ eigenstates of the **strong interaction**
- Not necessarily eigenstates of the **weak interaction**
- Flavor-changing process in neutral mesons:  
transition between particles and anti-particles  
→ **flavor oscillations** (also called: flavor mixing)

$$|P\rangle \leftrightarrow |\bar{P}\rangle$$

widely studied particle-anti-particle systems with oscillations

neutral Kaons:  $|K^0\rangle = |\bar{s} d\rangle \leftrightarrow |\bar{K}^0\rangle = |s\bar{d}\rangle$

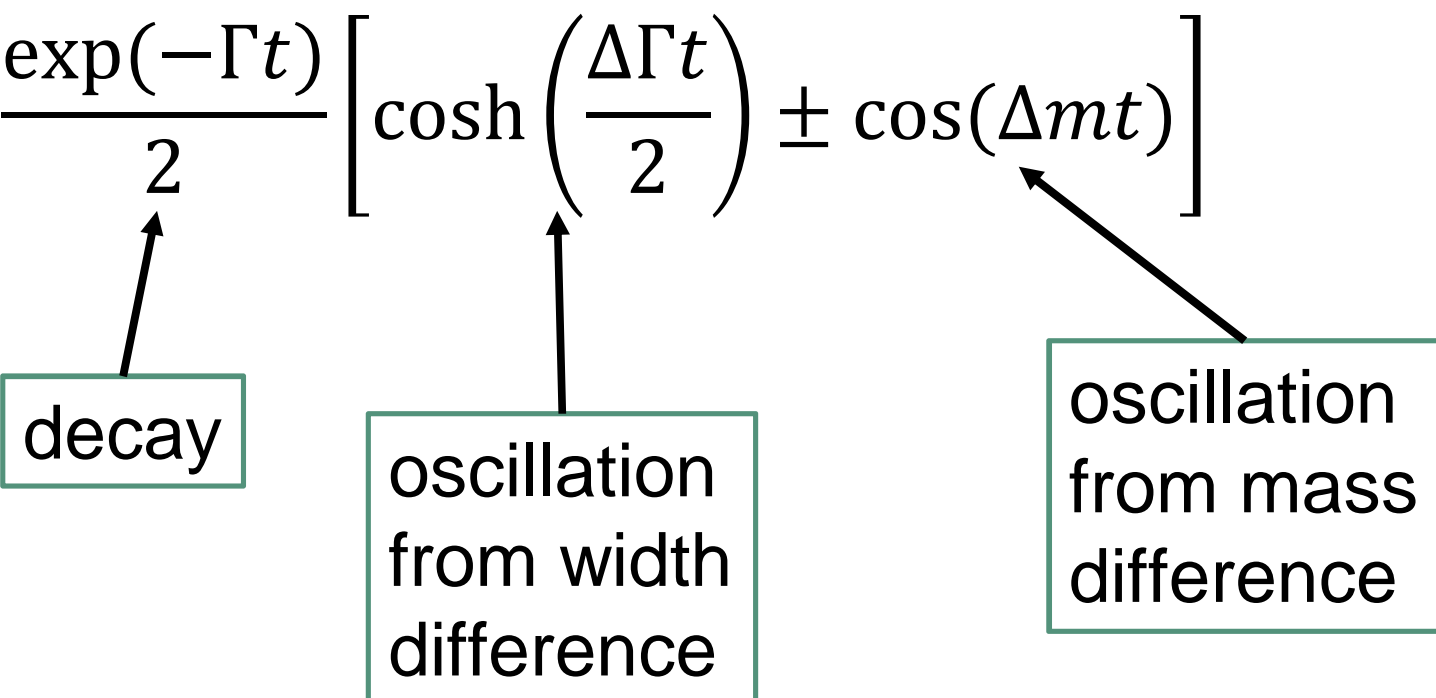
neutral B-mesons:  $|B_d^0\rangle = |\bar{b}d\rangle \leftrightarrow |\bar{B}_d^0\rangle = |b\bar{d}\rangle$   
 $|B_s^0\rangle = |\bar{b}s\rangle \leftrightarrow |\bar{B}_s^0\rangle = |b\bar{s}\rangle$

# Time Evolution

Calculation equivalent to neutrino-oscillations

Difference: Mesons are unstable, additional oscillations caused by **difference in decay width**

transition probabilities:

$$|g_{\pm}(t)|^2 = \frac{\exp(-\Gamma t)}{2} \left[ \cosh\left(\frac{\Delta\Gamma t}{2}\right) \pm \cos(\Delta mt) \right]$$


decay

oscillation from width difference

oscillation from mass difference

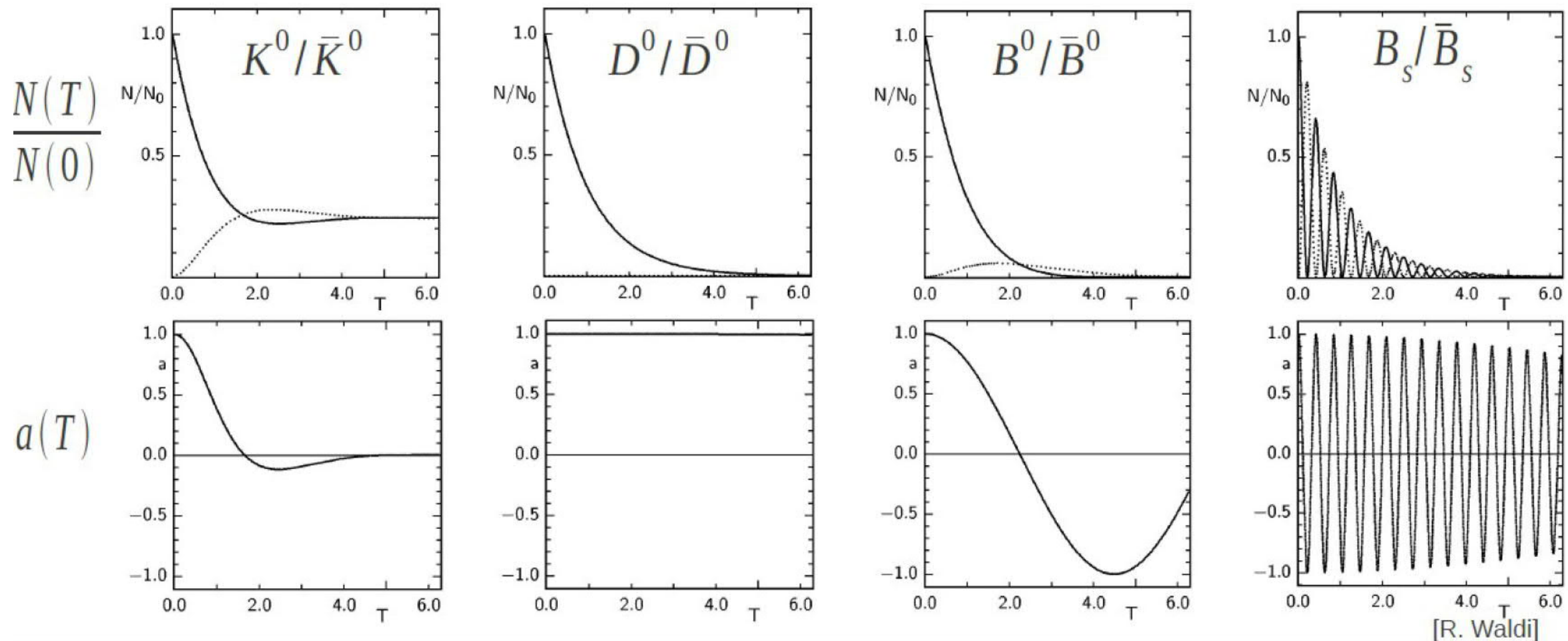


# Different Oscillating Systems

Mass difference and decay widths

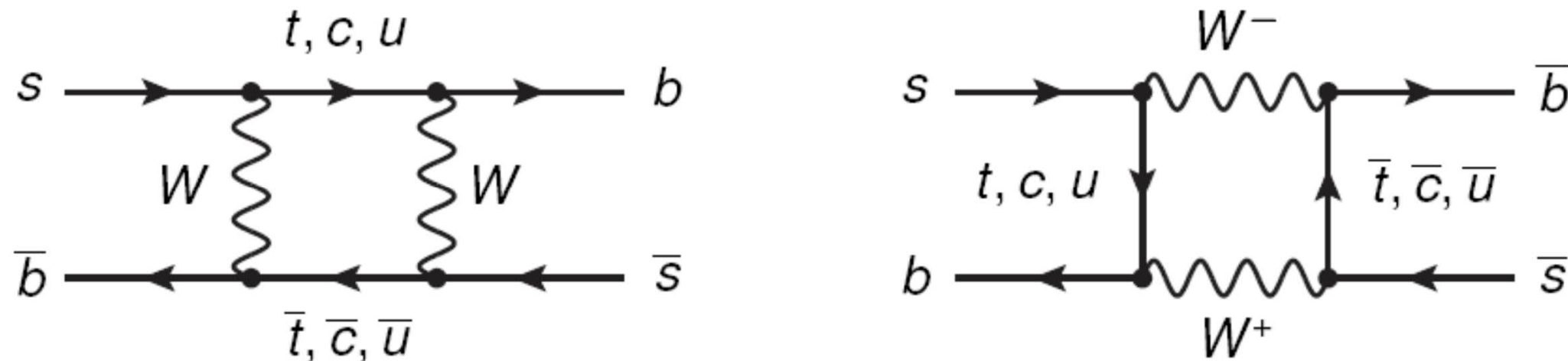
|                                    | $K^0/\bar{K}^0$      | $D^0/\bar{D}^0$ | $B^0/\bar{B}^0$ | $B_s/\bar{B}_s$ |
|------------------------------------|----------------------|-----------------|-----------------|-----------------|
| $\tau$ [ps]*                       | 89                   | 0.4             | 1.6             | 1.5             |
| $\Gamma$ [ps <sup>-1</sup> ]       | 51700                | 2.4             | 0.64            | 0.62            |
| $y = \frac{\Delta\Gamma}{2\Gamma}$ | -0.997               | 0.01            | $ y  < 0.01$    | $0.03 \pm 0.03$ |
| $\Delta m$ [ps <sup>-1</sup> ]     | $5.3 \times 10^{-3}$ | 0.02            | 0.5             | 17.8            |
| $x = \frac{\Delta m}{\Gamma}$      | 0.95                 | 0.01            | 0.8             | 26              |

\*) at LHCb energies lifetime in ps  $\sim$  decay length in cm



# Learning from Oscillations

Compute mass differences from **box diagrams**

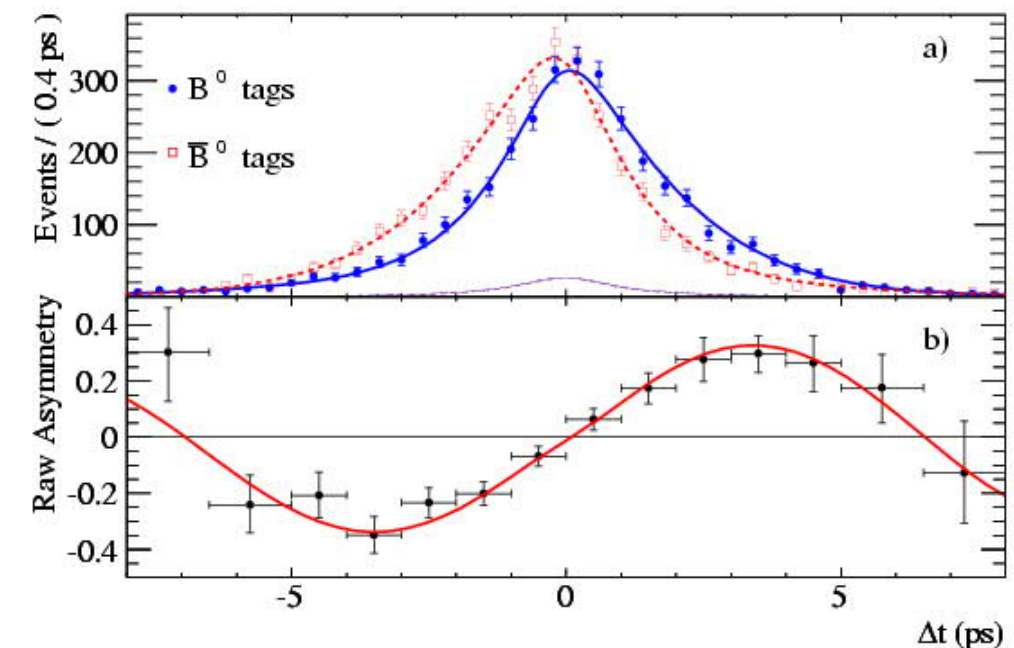
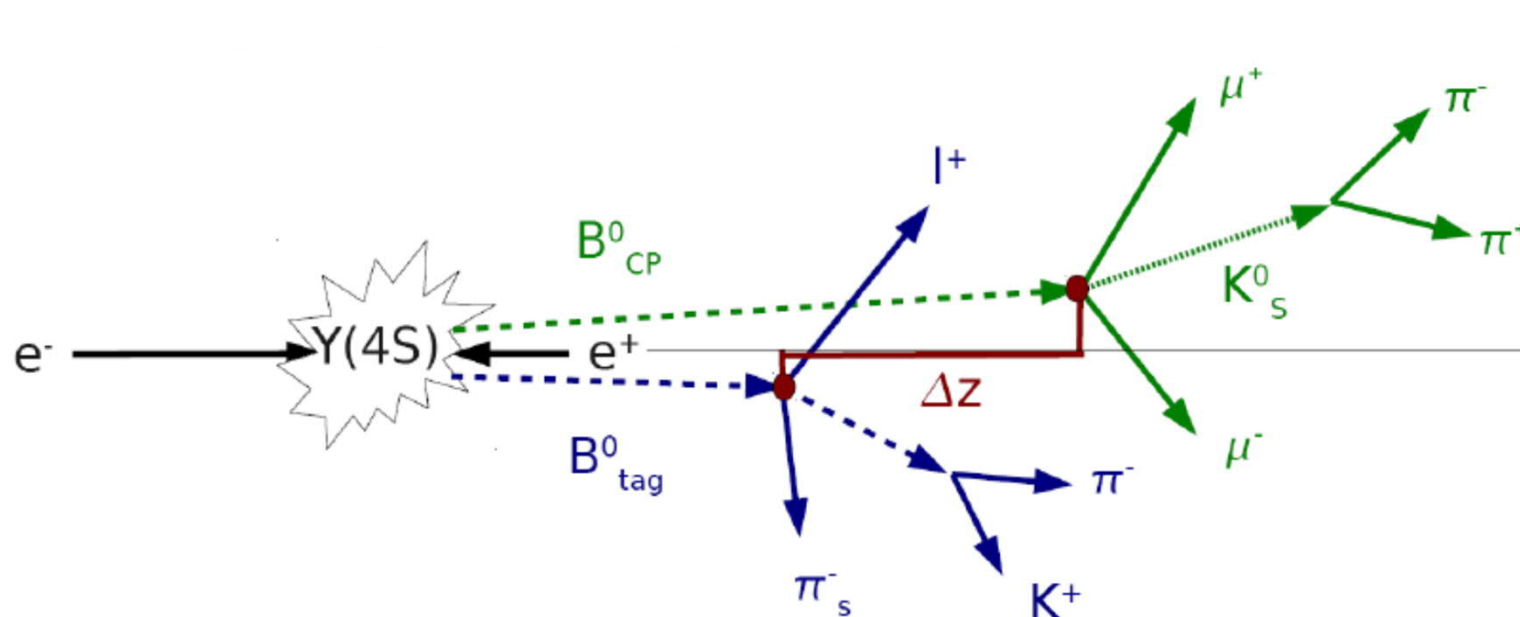


- approximations:  $m_t$  only relevant quark mass,  $V_{tb} \approx 1$
- Result:  $\Delta m_{d,s} \approx 2|M_{12}| \sim G_F^2 m_W^2 S \left( \frac{m_t^2}{m_W^2} \right) (V_{td}^* V_{ts} V_{tb})^2$
- Measurement of  $|V_{td}|$  and  $|V_{ts}|$  from **oscillation frequency**
- First results in  $B_d$  at ARGUS (DESY) and UA1 (CERN) 1987  
→ large  $\Delta m_d$  hints at high top quark mass

# Oscillations Measurements

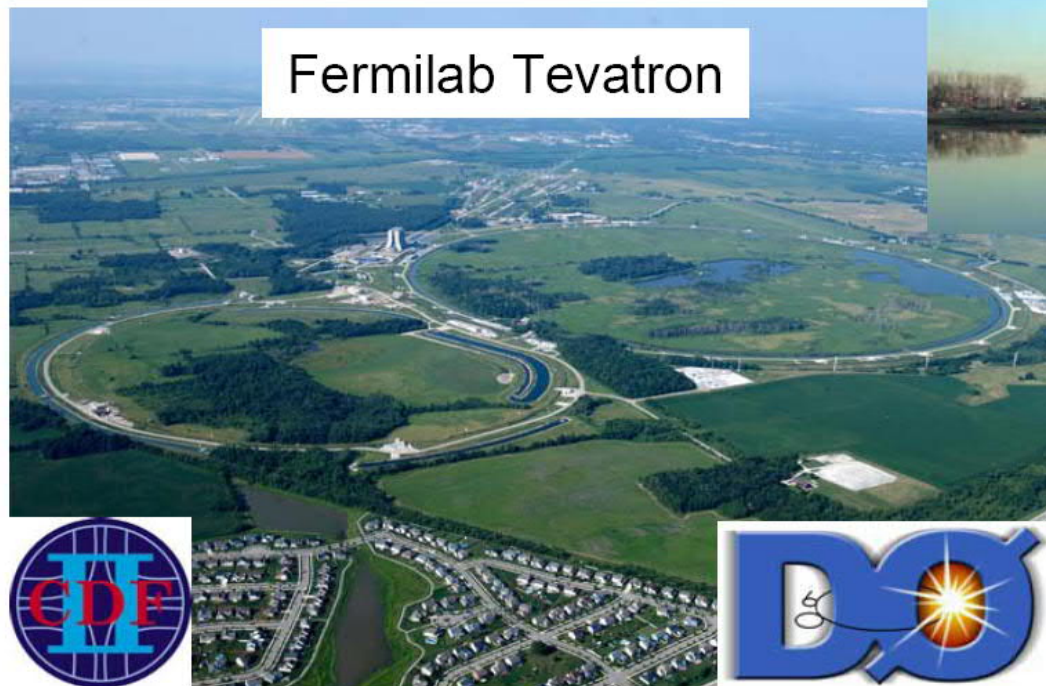
B-factories: electron positron colliders with asymmetric beam energy

- tuned to  $Y(4S)$  resonance:  $B\bar{B}$  pairs  $\sim$  at rest in  $e^+e^-$  system
- $B\bar{B}$  system moving relative to laboratory frame  
→ better measurement of decay length
- $B\bar{B}$  system is an entangled quantum system  
→ first decay as  $B$  or  $\bar{B}$  determines second decay
- Measure flavor as function in **difference** of decay length

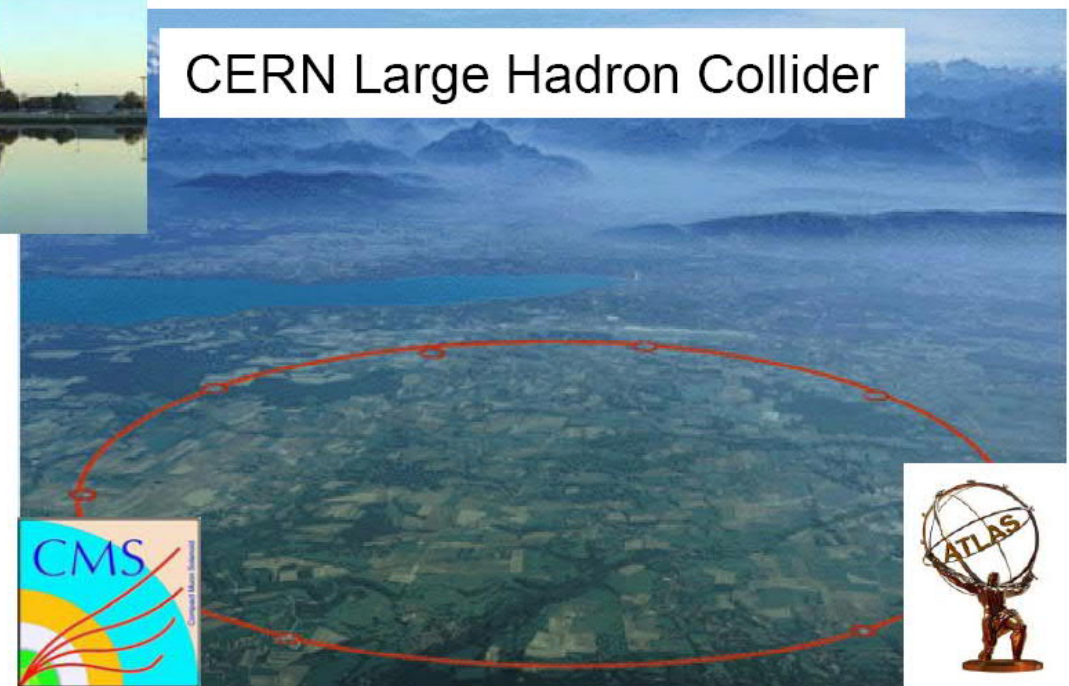




# Where to find top quarks



CERN Large Hadron Collider



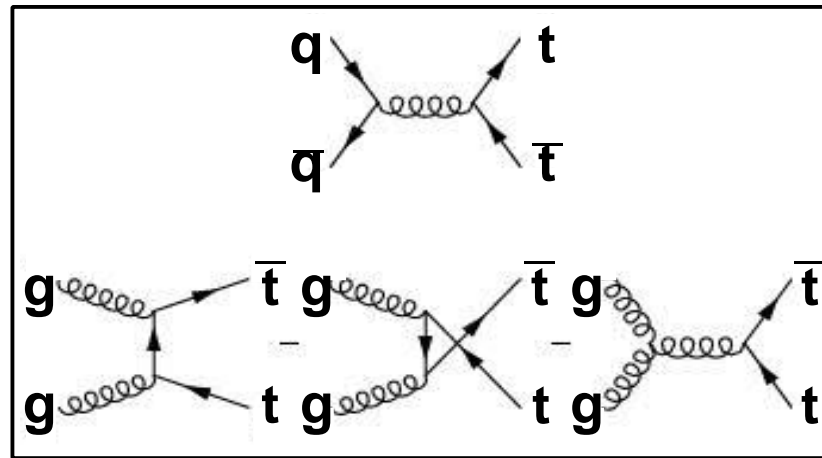
## Tevatron:

- Run 1:  $\sqrt{s} = 1.8 \text{ TeV}$  (1992-1996)  
65  $\text{pb}^{-1}$ : top quark discovered  
(~20 events per experiment)
- Run 2:  $\sqrt{s} = 1.96 \text{ TeV}$  (2001-2011)  
12  $\text{fb}^{-1}$  first precision top physics

## LHC:

- $\sqrt{s} = 7 \text{ TeV}$  (2010-2011)  
5  $\text{fb}^{-1}$ : 1M top pairs produced ~60k reco  
re-establish top quark
- $\sqrt{s} = 8 \text{ TeV}$  (2012)  
20  $\text{fb}^{-1}$  precision top physics  
statistical uncertainties become irrelevant
- $\sqrt{s} = 13 \text{ TeV}$  (2015-...)  
>20  $\text{fb}^{-1}$  more precision studies  
very rare processes

# Producing top quarks

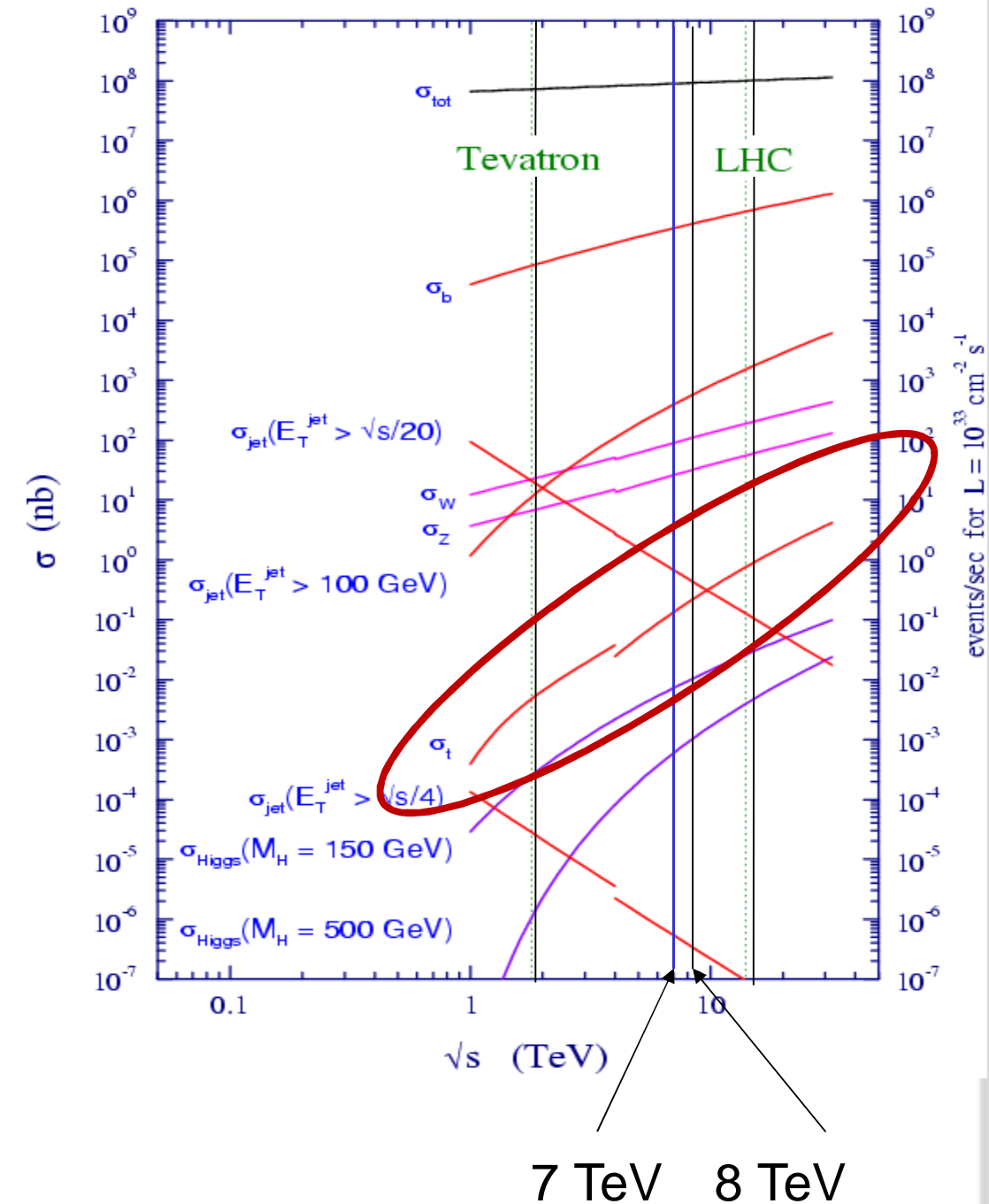


← ~15%

← ~85%

- $\sqrt{s} = 7 \text{ TeV}$  (2010-2011)  
5 fb<sup>-1</sup>: 1M top pairs produced ~60k reco  
re-establish top quark
- $\sqrt{s} = 8 \text{ TeV}$  (2012)  
20 fb<sup>-1</sup> precision top physics  
statistical uncertainties become irrelevant
- $\sqrt{s} = 13 \text{ TeV}$  (2015-....)  
>20 fb<sup>-1</sup> more precision studies  
very rare processes

proton - (anti)proton cross sections

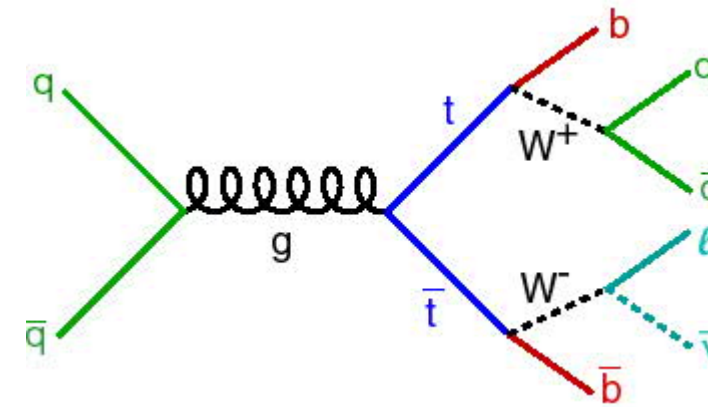




# Top quark decays

## Top Pair Decay Channels

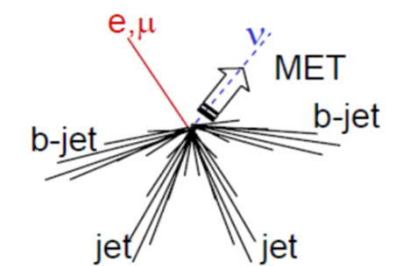
|            |               |           |            |               |            |
|------------|---------------|-----------|------------|---------------|------------|
| $c\bar{s}$ | electron+jets | muon+jets | tau+jets   | all-hadronic  |            |
| $u\bar{d}$ |               |           |            |               |            |
| $\tau^-$   | $e\tau$       | $\mu\tau$ | $\tau\tau$ | tau+jets      |            |
| $\mu^-$    | $e\mu$        | $\mu\mu$  | $\mu\tau$  | muon+jets     |            |
| $e^-$      | $e\mu$        | $e\mu$    | $e\tau$    | electron+jets |            |
| $W$ decay  | $e^+$         | $\mu^+$   | $\tau^+$   | $u\bar{d}$    | $c\bar{s}$ |



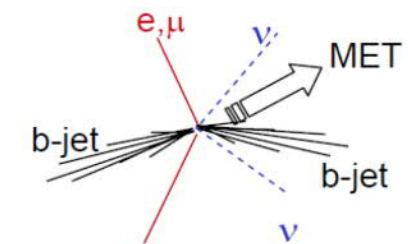
$t \rightarrow Wb \sim 100\%$

classify by W decay

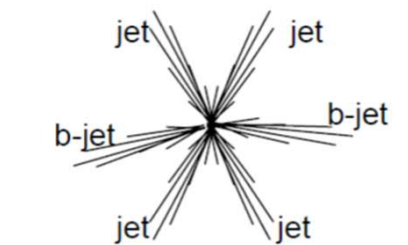
- "Lepton [e,μ] + jets" (34%)  
 $tt \rightarrow bl\nu bqq'$



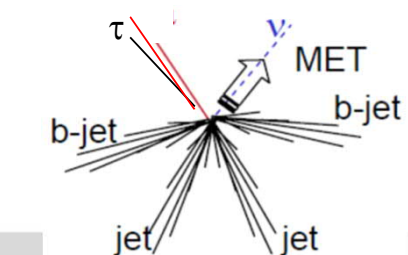
- "Dilepton [e,μ]" (6%)  
 $tt \rightarrow bl\nu bl\nu$



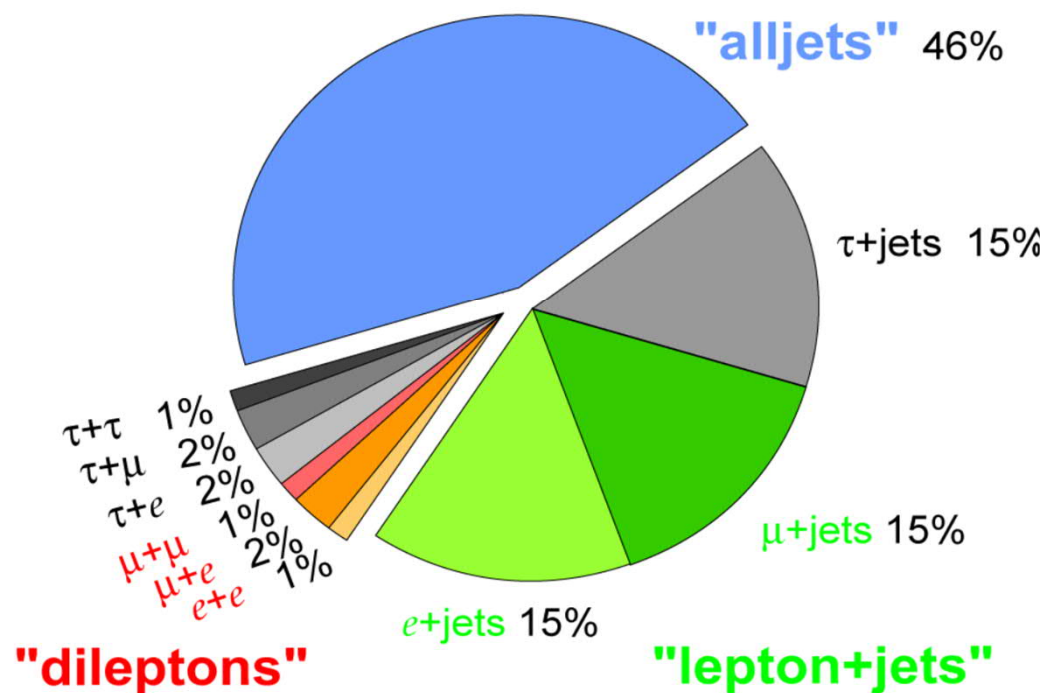
- "All jets" (46%)  
 $tt \rightarrow bqq'bqq'$



- "Tau + jets" (15%)  
 $tt \rightarrow b\tau\nu bqq'$



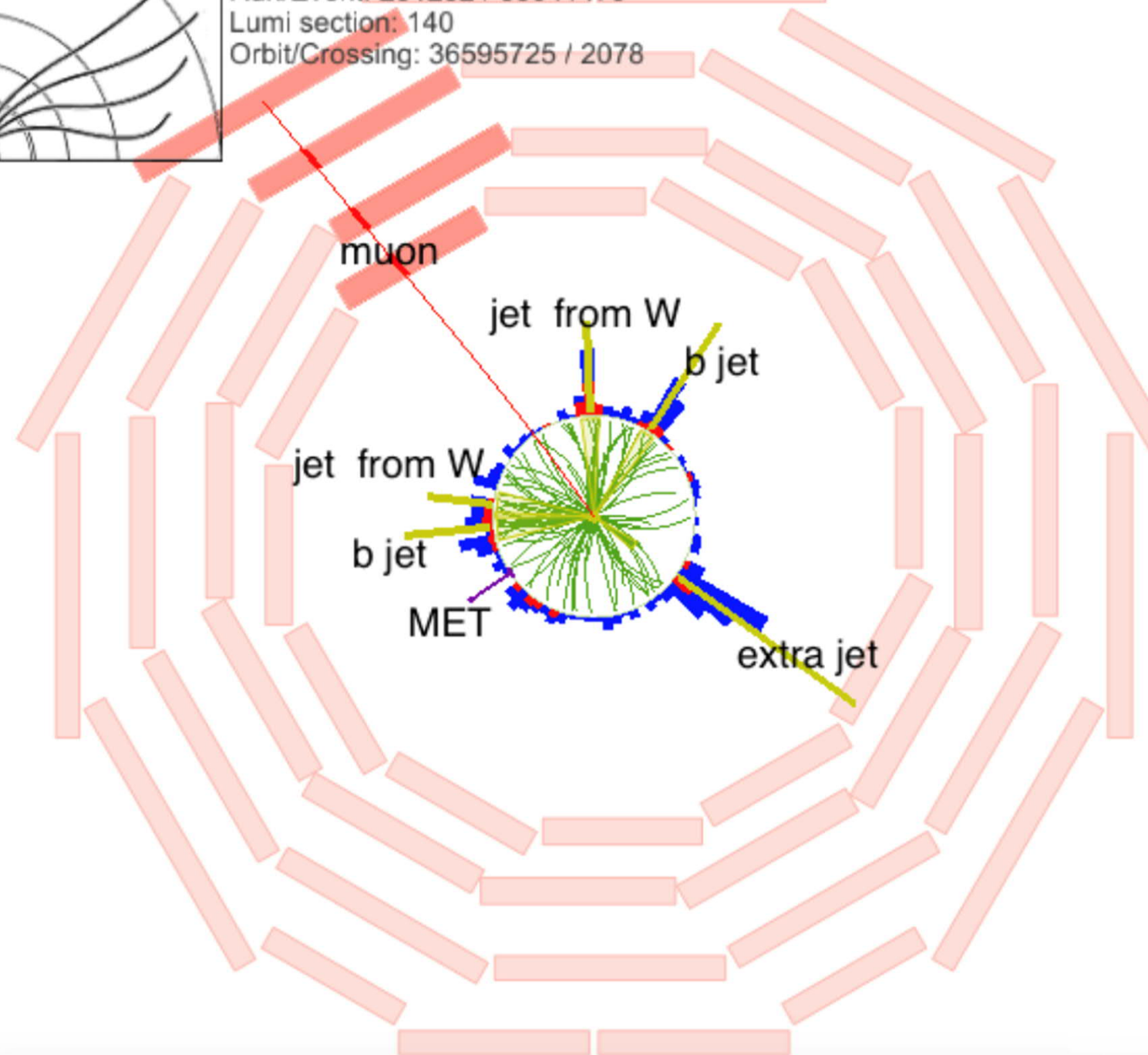
## Top Pair Branching Fractions



# Detector View



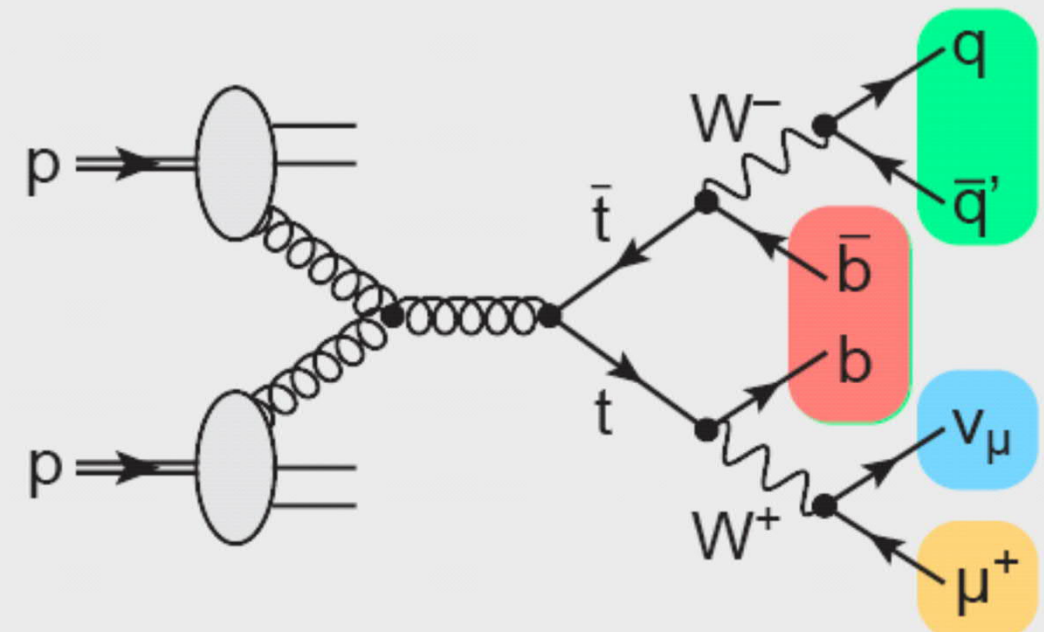
CMS Experiment at LHC, CERN  
Data recorded: Thu Jul 9 01:29:29 2015 CEST  
Run/Event: 251252 / 85041479  
Lumi section: 140  
Orbit/Crossing: 36595725 / 2078



# Selecting Top events

- Event selection:
  - enrich signal over backgrounds
  - simplest method: „cuts“
- Optimize selection :
  - Signal to background  $N^{sig} / N^{bkg}$
  - signal significance  $N^{sig} / \sqrt{N^{sig} + N^{bkg}}$
  - optimized on simulation to avoid bias

Example: lepton + jets channel



Lepton with  $p_T > 20-30$  GeV

Neutrino: MET > 30 GeV

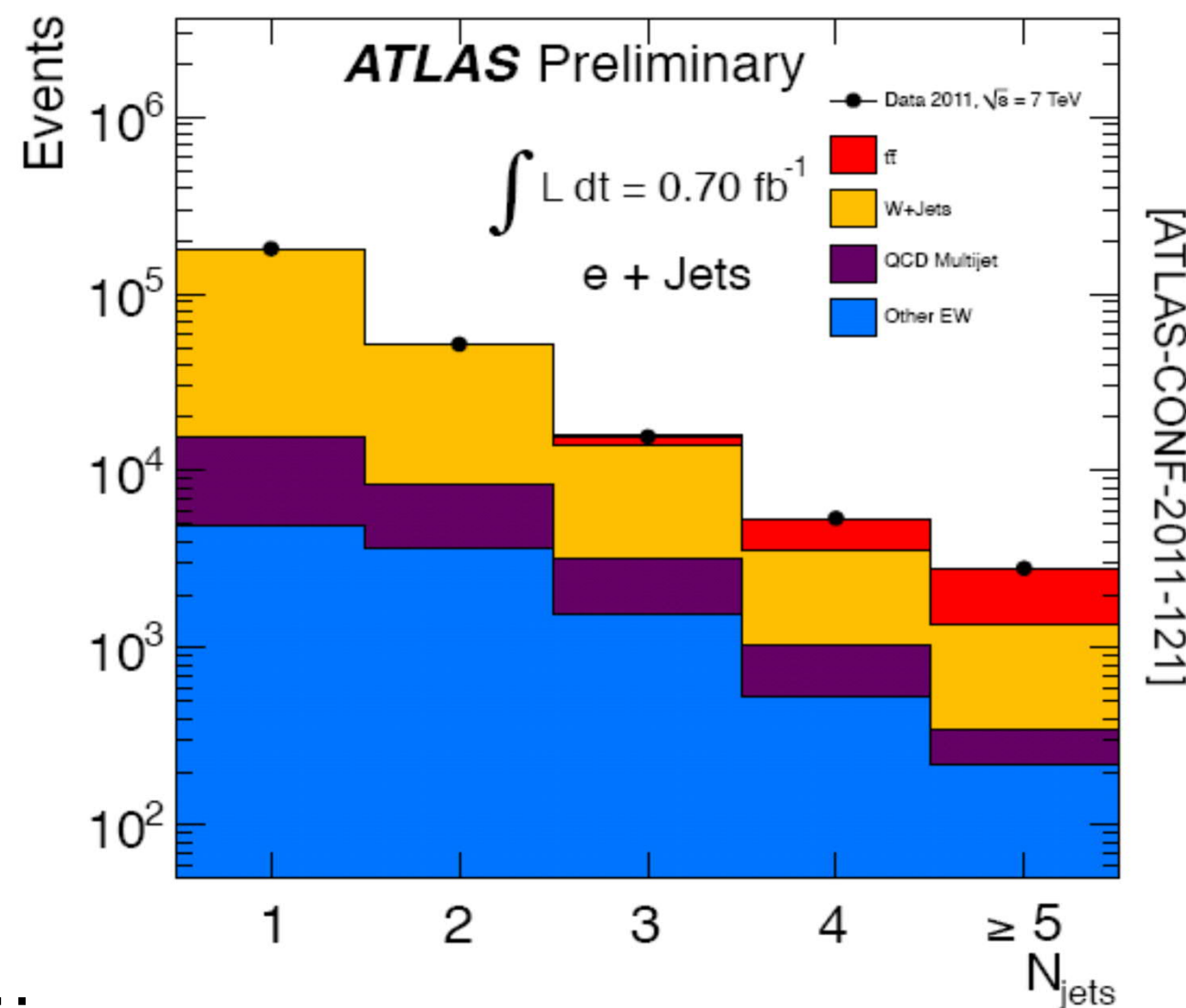
4 Jets with  $p_T > 40$  GeV

2 jets from B-decays (b-tag)

# Backgrounds

- Which backgrounds are distinguishable from signal  
→ **reducible** backgrounds
- **Instrumental** background  
→ detector noise  
→ misidentifications („fakes“)  
e.g. jet fakes an electron
- Important backgrounds for top  
→ lepton + jets: W-boson production in association with jets (W+ jets)  
→ Di-lepton: Z+ jets  
→ also: multijets, single-top, ...

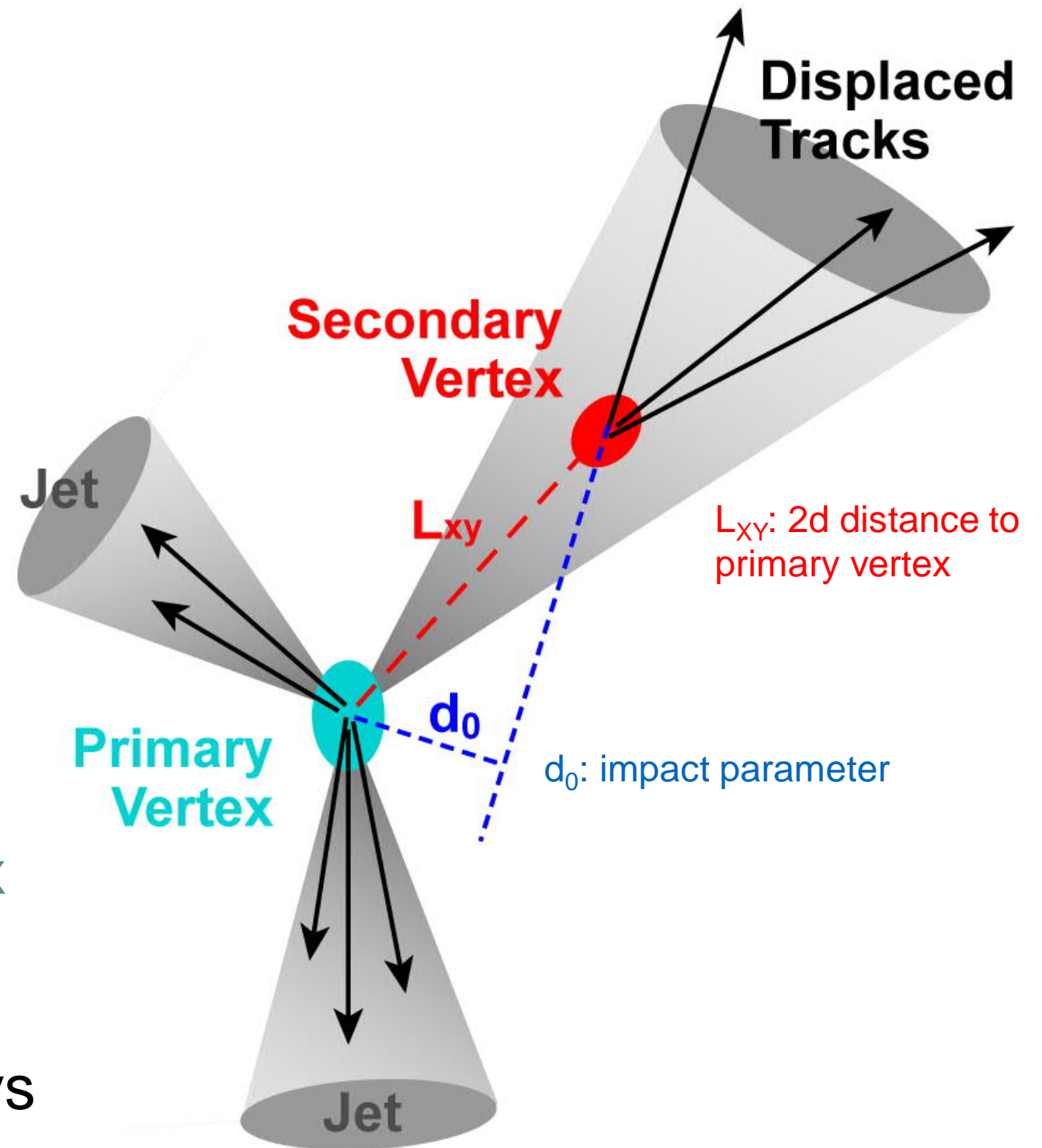
## Jet multiplicity in e+jets events





# B-tagging

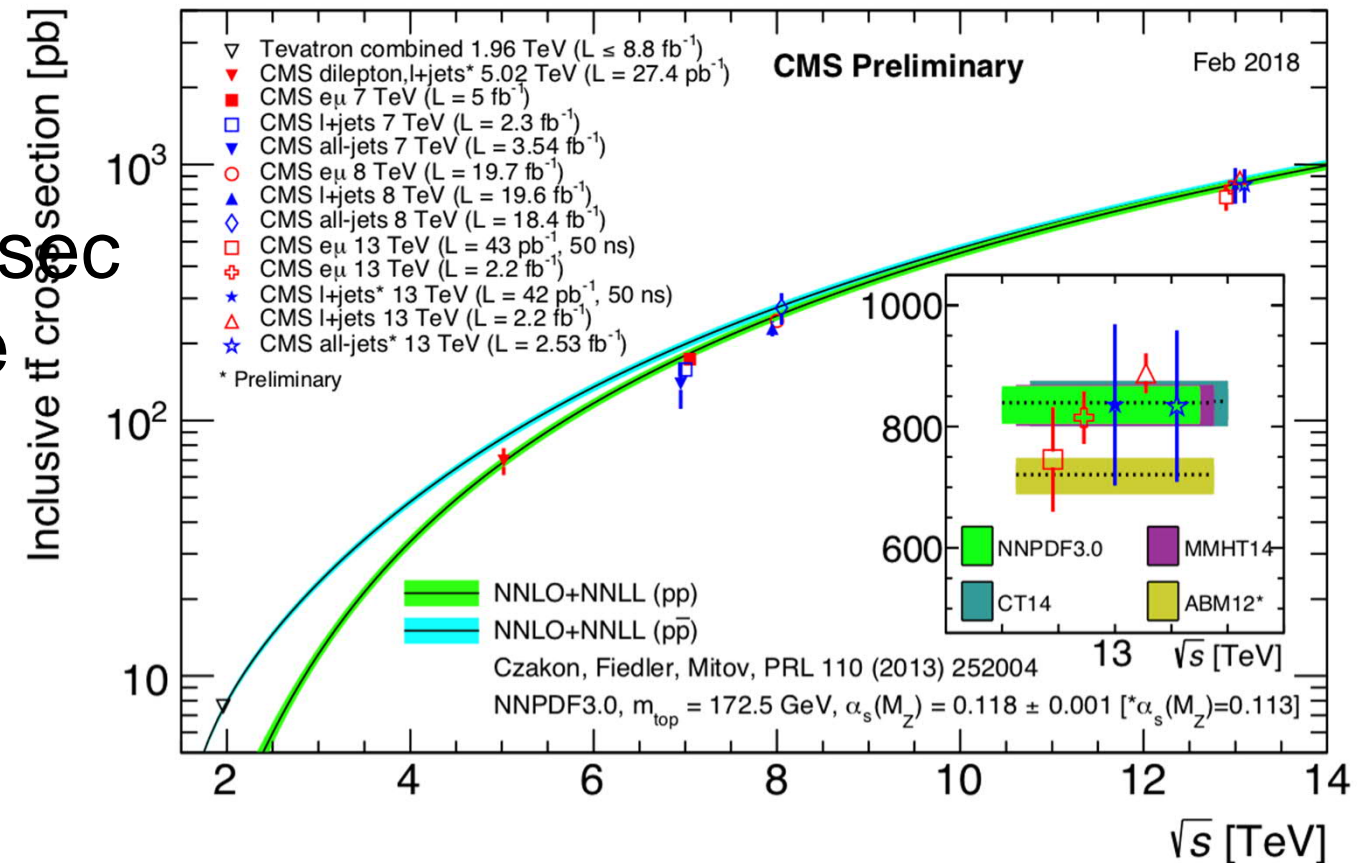
- Many interesting processes with b-quarks
  - ⇒  $H \rightarrow bb$ ,  $tt \rightarrow WbWb$
  - ⇒ identify jets with B-hadrons
- B-tag I (hadrons)
  - B-mesons are massive and long lived ( $c\tau \sim 0.5\text{mm}$ )
  - ⇒ B-mesons are massive **large impact parameter tracks**
  - ⇒ **displaced massive vertex**
- B-tag II (leptons)
  - look for semi-leptonic B decays
  - ⇒ **soft leptons**





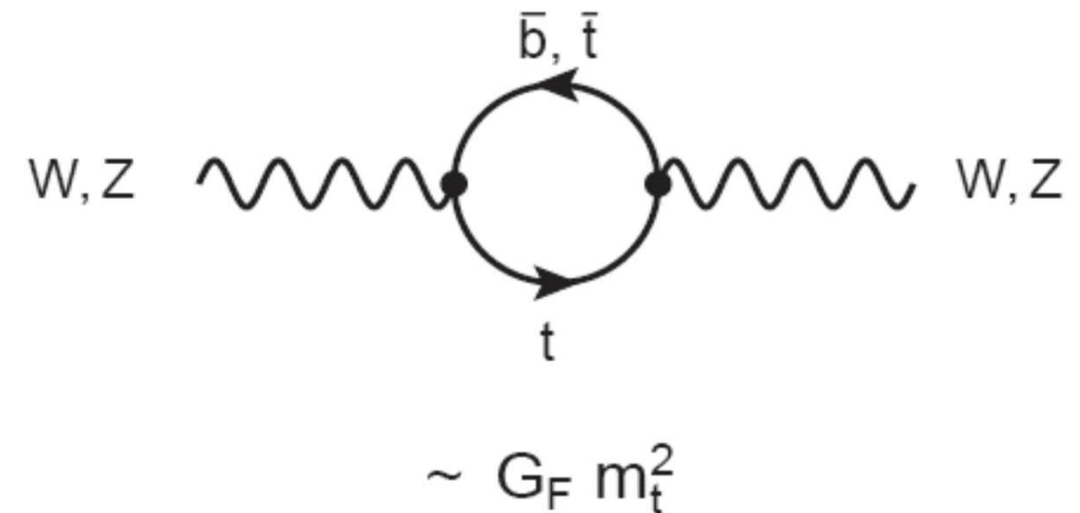
# Top Cross Section

- Theory for top-pairs (2015)  
NNLO + NNLL  
⇒ few % uncertainty
  
- Compare Tevatron ↔ LHC  
⇒ LHC: 20-100 x tevatron xsec  
⇒ Tevatron: large difference between pp and p-anti-p tops produced from valence-quarks  
⇒ LHC: small difference between pp and p-anti-p tops produced from gluons and sea-quarks  
→ skip complicated antiproton generation



# Top Quark Mass

- Reminder:  $M_W$ ,  $m_t$ ,  $M_H$  connected via loop diagrams



- How to define the top mass?
  - usual definition: **pole-mass**  
= mass term in the **propagator**

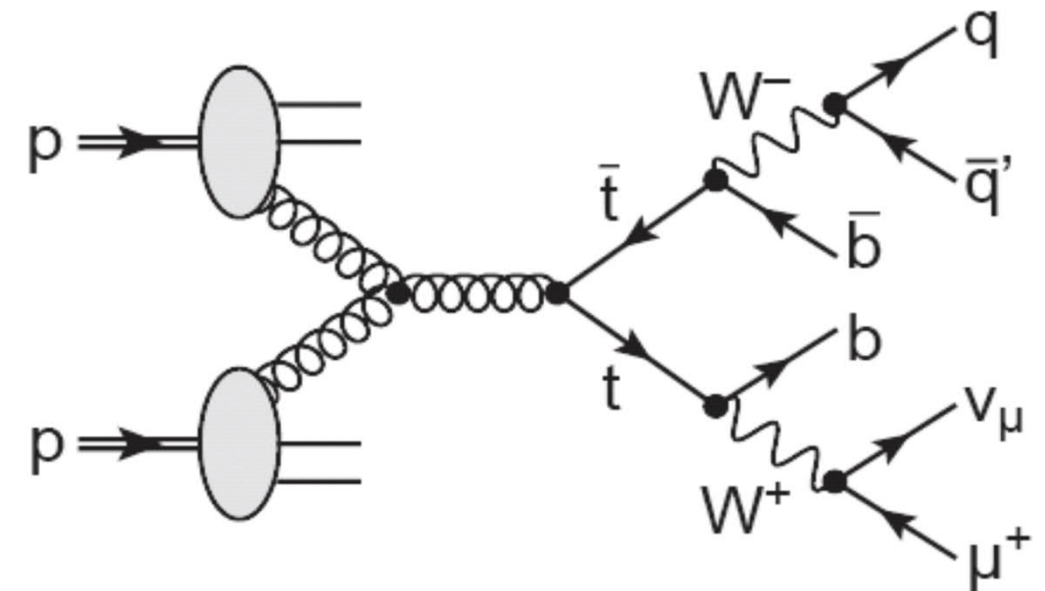
$$\frac{1}{p^2 - m_t^2 - i\Gamma_t m_t}$$

- Problem: non-perturbative effects for color charged particles of  $O(\Lambda_{\text{QCD}})$
- Experimentally: use **mass-parameter** of Monte-Carlo-Simulation  $\Rightarrow$  roughly equal to pole mass (within unc.)
- Theoretically cleaner: scale-dependent „**running mass**“  
 $\Rightarrow$  well defined within a given calculation scheme (e.g. MS-bar)

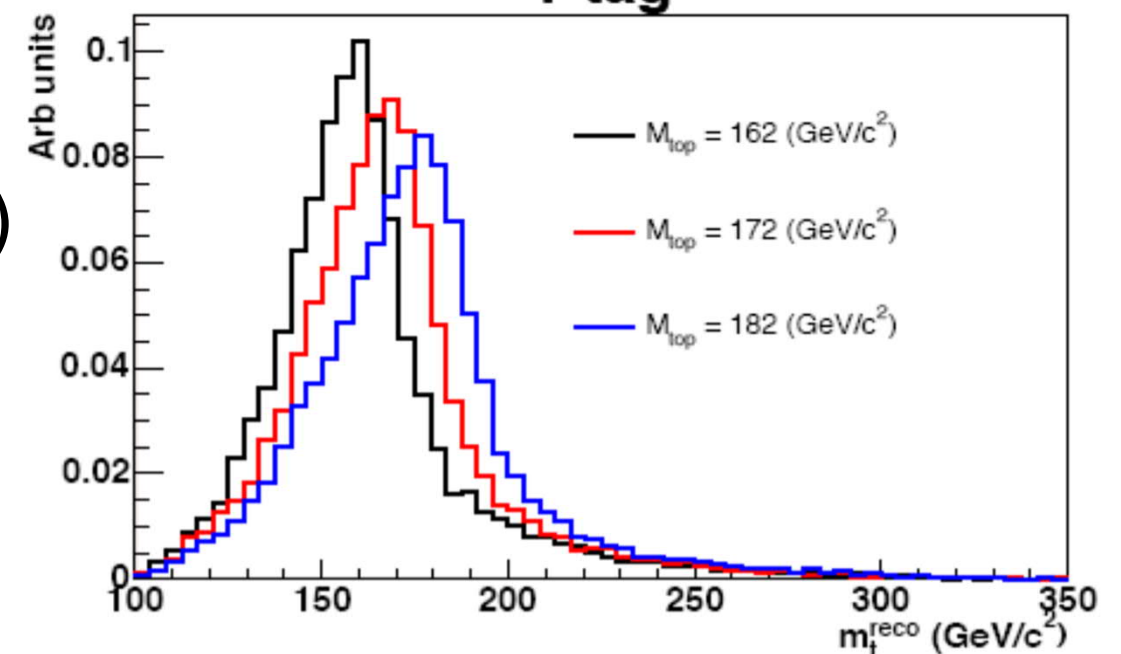
$$m_t^{\overline{\text{MS}}}(m_t) = \frac{m_t}{1 + 4\alpha_s(m_t)/3}$$

# Measuring the Top Mass

- **Direct** measurement of top mass use event **kinematics**
- Lepton + Jets: kinematics **overconstrained**
  - one unknown: neutrino  $p_z$
  - possible **constraints**:  
W-mass,  $m_t = m_{\text{anti-}t}$
- **Combinatorics**: associate jets to partons (4 jets  $\Rightarrow$  24 combinations)
  - find „best“ combination
- Measurement method at Tevatron and LHC
  - **template** fit (like W-mass)
  - **matrix-element methods**



Schablonen für drei Top-Massen

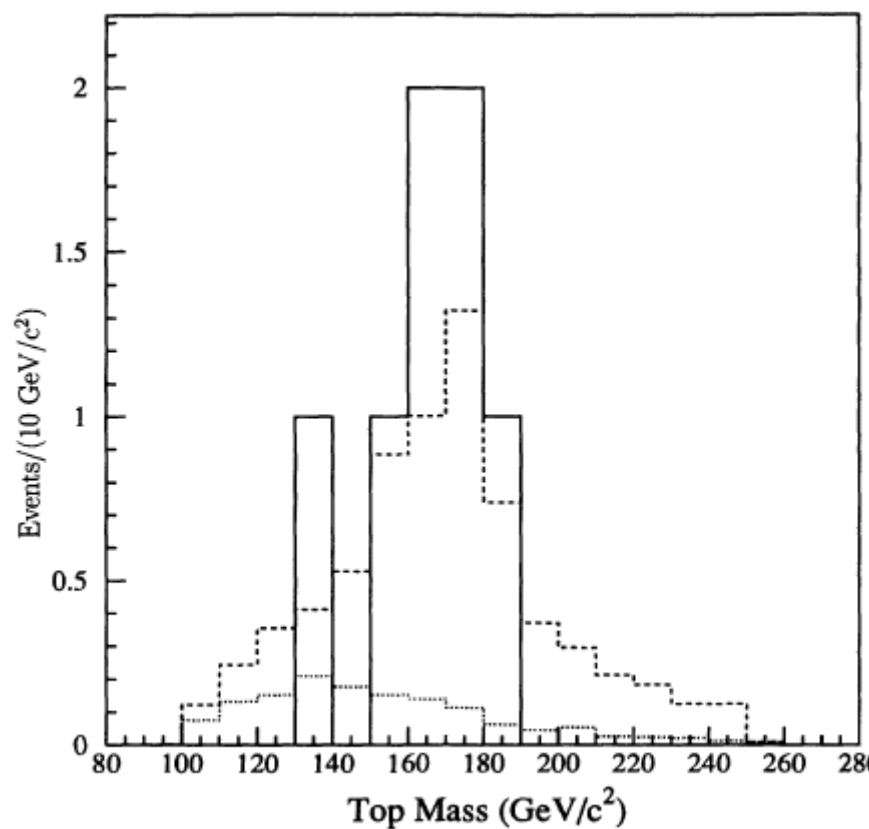


[[http://www-cdf.fnal.gov/physics/new/top/2010/mass/TMT\\_p28\\_public/](http://www-cdf.fnal.gov/physics/new/top/2010/mass/TMT_p28_public/)]

# Top Quark Mass

**first measurement**  
(CDF, 1994, 7 events)

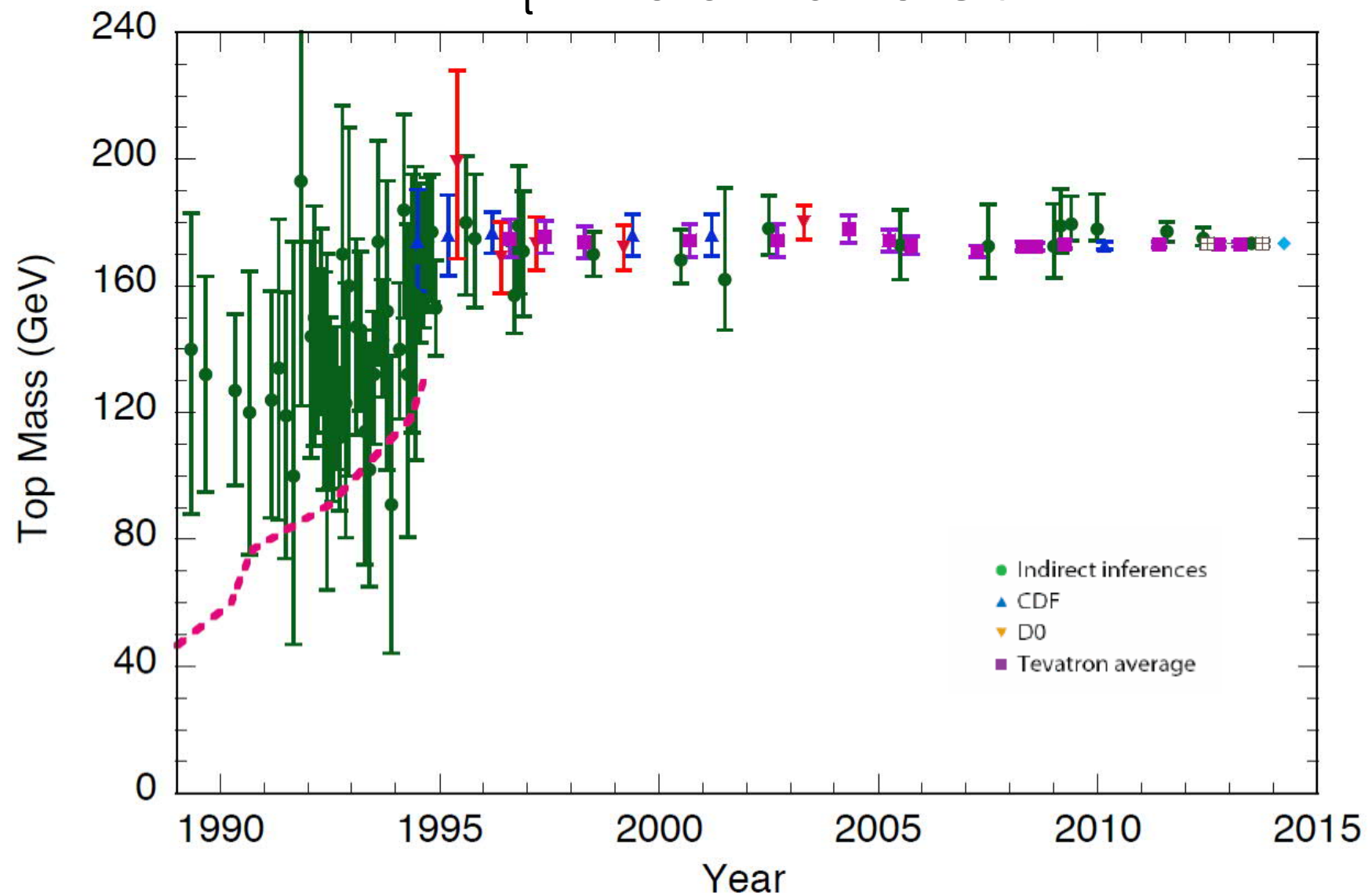
$$M_t = 170 \pm 10^{+13}_{-12} \text{ GeV}$$



**now**

(world average 2014)

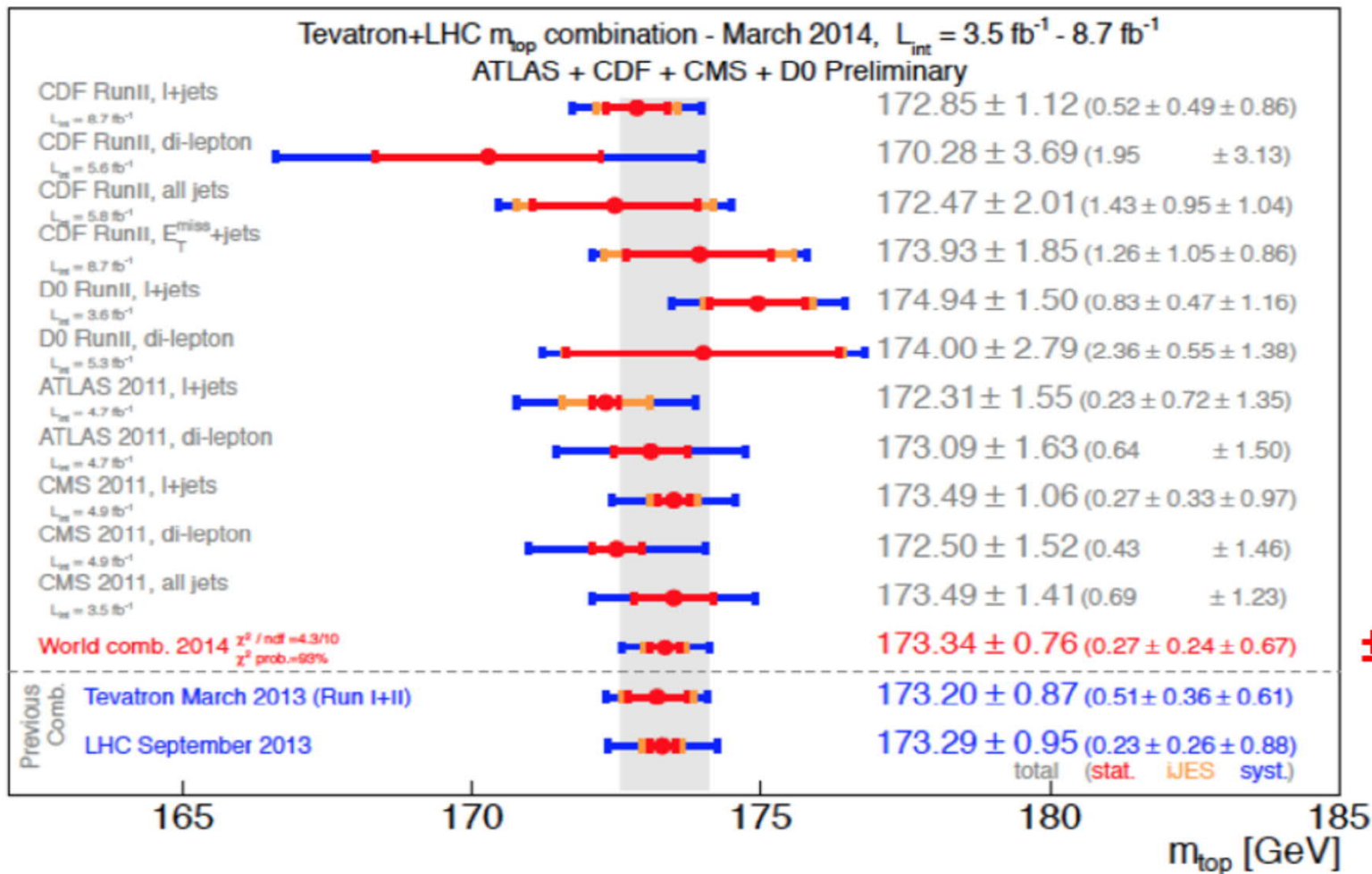
$$M_t = 173.34 \pm 0.76 \text{ GeV}$$





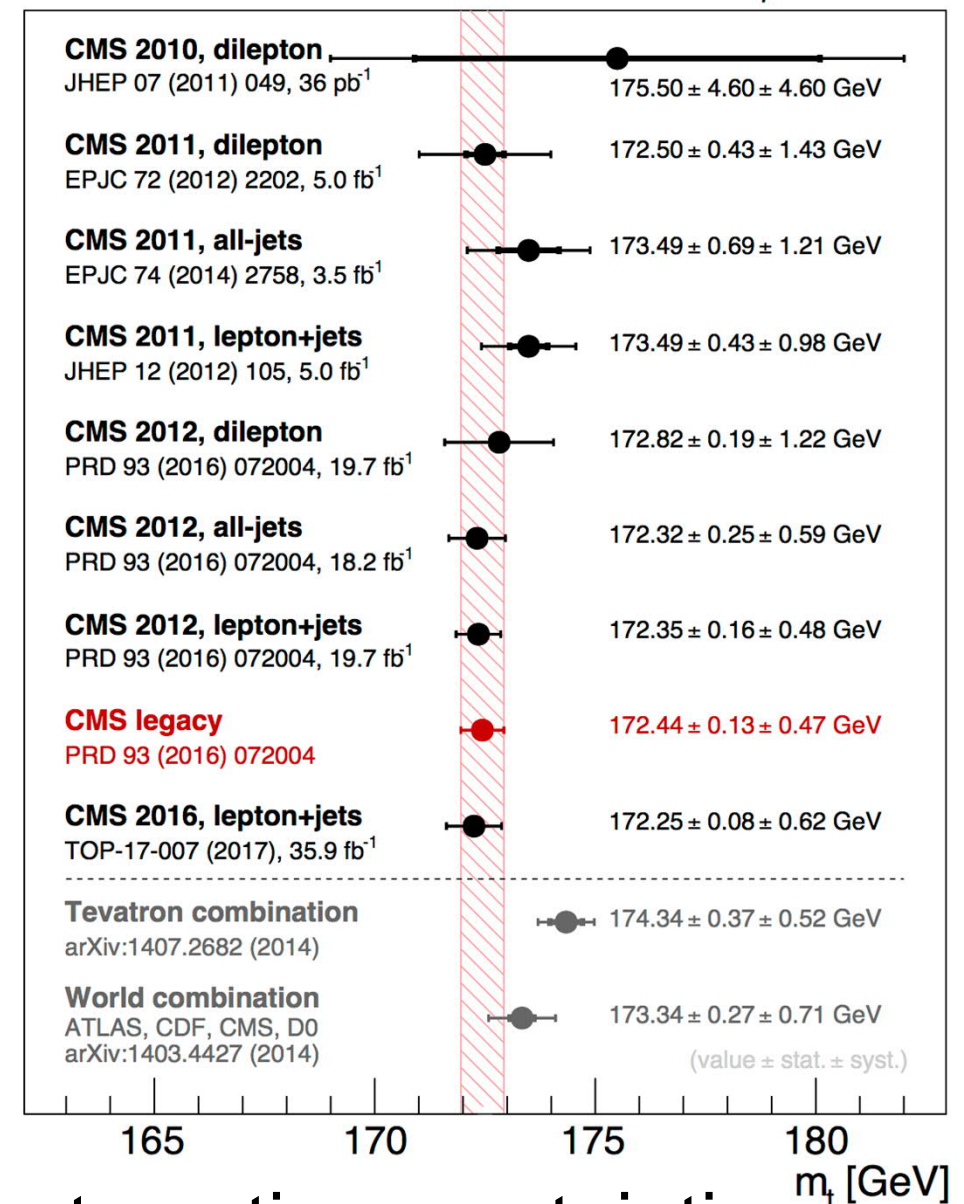
# Measuring the Top Mass

World Combination



CMS by channel

September 2017

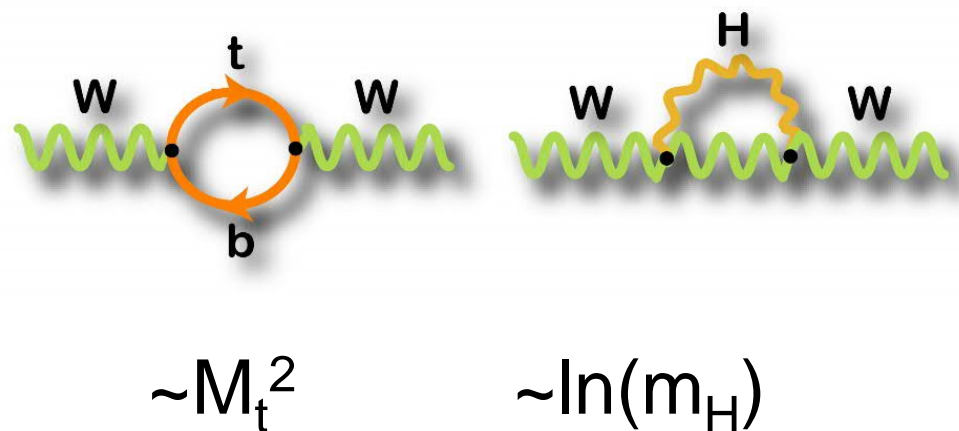


- uncertainties < 1%
- newer LHC measurements limited by systematic uncertainties
- Visible tension between tevatron and LHC

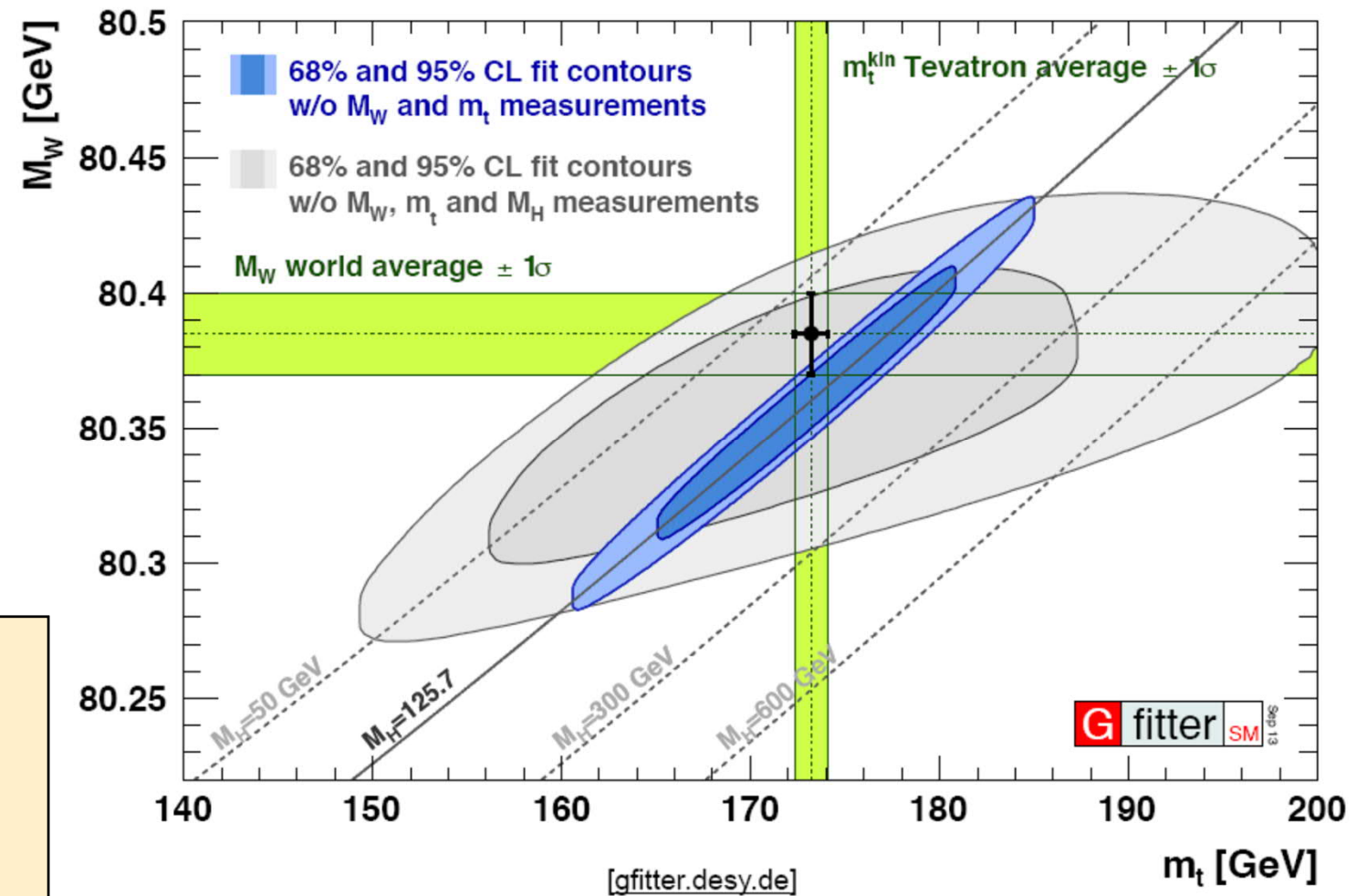


# Measuring the Top Mass

$M_W, M_t, M_H$  intermixed at loop level



expect from EWK data :  
 $M_H = 90^{+36}_{-27}$  GeV  
 $M_H < 152$  GeV @ 95 % CL



- Measured  $M_W, M_H, M_t$  consistent with SM
- constrain exotic models (i.e. SUSY) instead